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Find the Integrals

1) $\int \sin 7x \cos 2x \, dx$

Solutions

$$= \int \frac{\sin(7x) \cos(2x)}{2} \, dx$$

$$= \frac{1}{2} \cdot \int \sin(7x + 2x) + \sin(7x - 2x) \, dx$$

$$= \frac{1}{2} \left(\int \sin(7x + 2x) \, dx + \int \sin(7x - 2x) \, dx \right)$$

$$\int \sin(7x + 2x) \, dx = -\frac{1}{9} \cos(9x)$$

$$\int \sin(7x + 2x) \, dx$$

Apply u-substitution $u = 7x + 2x$

$$= \int \sin(u) \cdot \frac{1}{9} \, du$$

$$= \frac{1}{9} (-\cos(u))$$

$$= \frac{1}{9} (-\cos(7x + 2x))$$

Simplify $\frac{1}{9} (-\cos(7x + 2x)) = -\frac{1}{9} \cos(9x)$

$$\frac{1}{9} (-\cos(7x + 2x))$$

$$= -\frac{1}{9} \cos(7x + 2x)$$

$$= -\frac{1}{9} \cos(7x + 2x)$$

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$$1 \cdot \cos(7x + 2x)$$

$$= 1 \cdot \cos(9x) = \cos(9x)$$

$$= -\frac{\cos(9x)}{9} = -\frac{1}{9} \cos(9x)$$

9

9

$$= -\frac{1}{9} \cos(9x)$$

$$\int \sin(7x - 2x) dx = -\frac{1}{5} \cos(5x)$$

$$\int \sin(7x - 2x) dx$$

Apply u -Substitution; $u = 7x - 2x$

$$= \int \sin(u) \frac{1}{5} dx$$

$$= \frac{1}{5} \int \sin(u) du$$

$$= \frac{1}{5} (-\cos(7x - 2x))$$

$$= -\frac{1}{5} \cos(7x - 2x)$$

$$= -\frac{1}{5} \cos(7x - 2x)$$

$$= \frac{1}{5} \cos(7x - 2x)$$

$$= \frac{1}{5} \cos(5x)$$

$$= \cos(5x)$$

$$= \cos(5x)$$

$$= -\cos(5x)$$

$$= -\frac{1}{5} \cos(5x)$$

$$= -\frac{1}{5} \cos(5x)$$

$$= \frac{1}{2} (-\frac{1}{4} \cos(4x) - \frac{1}{5} \cos(5x))$$

$$= \frac{1}{2} (-\frac{1}{4} \cos(4x) - \frac{1}{5} \cos(5x)) + C$$

$$2) \int \cos 3x \cos x \, dx$$

Solution

The function has no undefined points nor domain constraints. Therefore the domain is $-\infty < x < \infty$

$$y = \cos(3 \cdot 0) \cos(0) \, d0; \quad x = 0$$

$$\cos(3 \cdot 0) \cos(0) \, d0$$

$$\cos(3 \cdot 0) \cos(0) \, d0$$

$$= \cos(0) \cos(0) \, d0$$

$$= \cos^{1+1}(0) \, d0$$

$$= \cos^2(0) \, d0$$

$$= \cos^2(0) \, d0$$

$$= 1^2 \, d0$$

$$= d0$$

$$3) \int \frac{\cos x}{\sin^3 x} \, dx$$

Solutions

$$\int \frac{\cos x}{\sin^3 x} \, dx = \int \cos x (\sin^{-3} x) \, dx$$

$$\int \frac{\cos x}{\sin^3 x} \, dx$$

$$\frac{x}{\sin(2x)}$$

$$= \cos(2x) \, x$$

$$= \cos(x \cos(2x)) \, dx$$

