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MAT 104 Assignment

Mechatronics Engineering

~~Q1~~

$$(1) \int \sin 7x \cos 2x dx$$

$$A = 7x \quad B = 2x$$

$$\sin A \cos B = \frac{1}{2} [\sin(A+B) - \sin(A-B)]$$

$$\sin A \cos B = \frac{1}{2} [\sin(7x+2x) - \sin(7x-2x)]$$

$$\sin A \cos B = \frac{1}{2} [\sin 9x - \sin 5x]$$

$$\int \sin 7x \cos 2x dx = \frac{1}{2} \left[\int \sin 9x - \int \sin 5x \right]$$

$$= \frac{1}{2} \left[-\frac{1}{9} \cos 9x + \frac{1}{5} \cos 5x \right]$$

$$= -\frac{1}{18} \cos 9x + \frac{1}{10} \cos 5x + C$$

$$(2) \int \cos 3x \cos x dx$$

$$A = 3x \quad B = x$$

$$\cos A \cos B = \frac{1}{2} [\cos(A+B) + \cos(A-B)]$$

$$\cos 3x \cos x = \frac{1}{2} [\cos(5x+x) + \cos(5x-x)]$$

$$\cos 3x \cos x = \frac{1}{2} [\cos 6x + \cos 4x]$$

$$\int \cos 3x \cos x \, dx = \frac{1}{2} \left[\int \cos 6x + \int \cos 4x \right]$$

$$\int \cos 3x \cos x \, dx = \frac{1}{2} \left[\frac{1}{6} \sin 6x + \frac{1}{4} \sin 4x + C \right]$$

$$= \frac{1}{12} \sin 6x + \frac{1}{8} \sin 4x + C$$

$$(3) \quad \frac{\cos x \, dx}{\sin^2 x}$$

$$\text{Let } u = \sin x \quad \text{--- (1)}$$

$$\frac{du}{dx} = \cos x$$

$$dx = du / \cos x$$

$$\int \frac{\cos x \, dx}{\sin^2 x} = \int \frac{\cancel{\cos x} \times du}{u^2 \cancel{\cos x}}$$

$$= \int u^{-2} \, du$$

$$= \frac{u^{-1}}{-1} + C = -\frac{1}{u} + C \quad \text{--- (2)}$$

Substitute $u = \sin x$ into equ (2)

$$\frac{-1}{u} + C = \frac{-1}{\sin x} + C = -\operatorname{cosec} x + C$$

$$(4) \int_1^2 \int_0^3 (9x^2y) dx dy$$

Consider the inner integral

$$\begin{aligned} & \int_0^3 (9x^2y) dx \\ &= \left[\frac{9x^3y}{3} \right]_0^3 \\ &= \left[\frac{9x^3y}{3} \right]_0^3 - \left[\frac{9x^3y}{3} \right]_0^0 \\ &= \frac{243y}{3} - 0 \\ &= 81y \end{aligned}$$

second integral

$$\begin{aligned} \int_1^2 81y dy &= \left[\frac{81y^2}{2} \right]_1^2 \\ &= \left[\frac{81y^2}{2} \right]_2^2 - \left[\frac{81y^2}{2} \right]_1^1 \\ &= \frac{81(4)}{2} - \frac{81(1)}{2} \\ &= \frac{324}{2} - \frac{81}{2} \\ &= 162 - 81/2 = \frac{243}{2} \end{aligned}$$