

ENG 234 ASSIGNMENT

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181MHS01/272

BIOMEDICAL ENGINEERING

12-9 $S = 0.5t^3 = 0.5(6)^3 = 108$

$t_1 = 6$

$t_2 = 8$

$t_3 = 10$

$v_1 = \frac{\partial S}{\partial t} \Big|_{t=6} = 1.5t^2$

$= 1.5(6)^2 = 54 \text{ m/s}$

$v_2 = \frac{\partial S}{\partial t} \Big|_{t=8} = 1.5t^2$

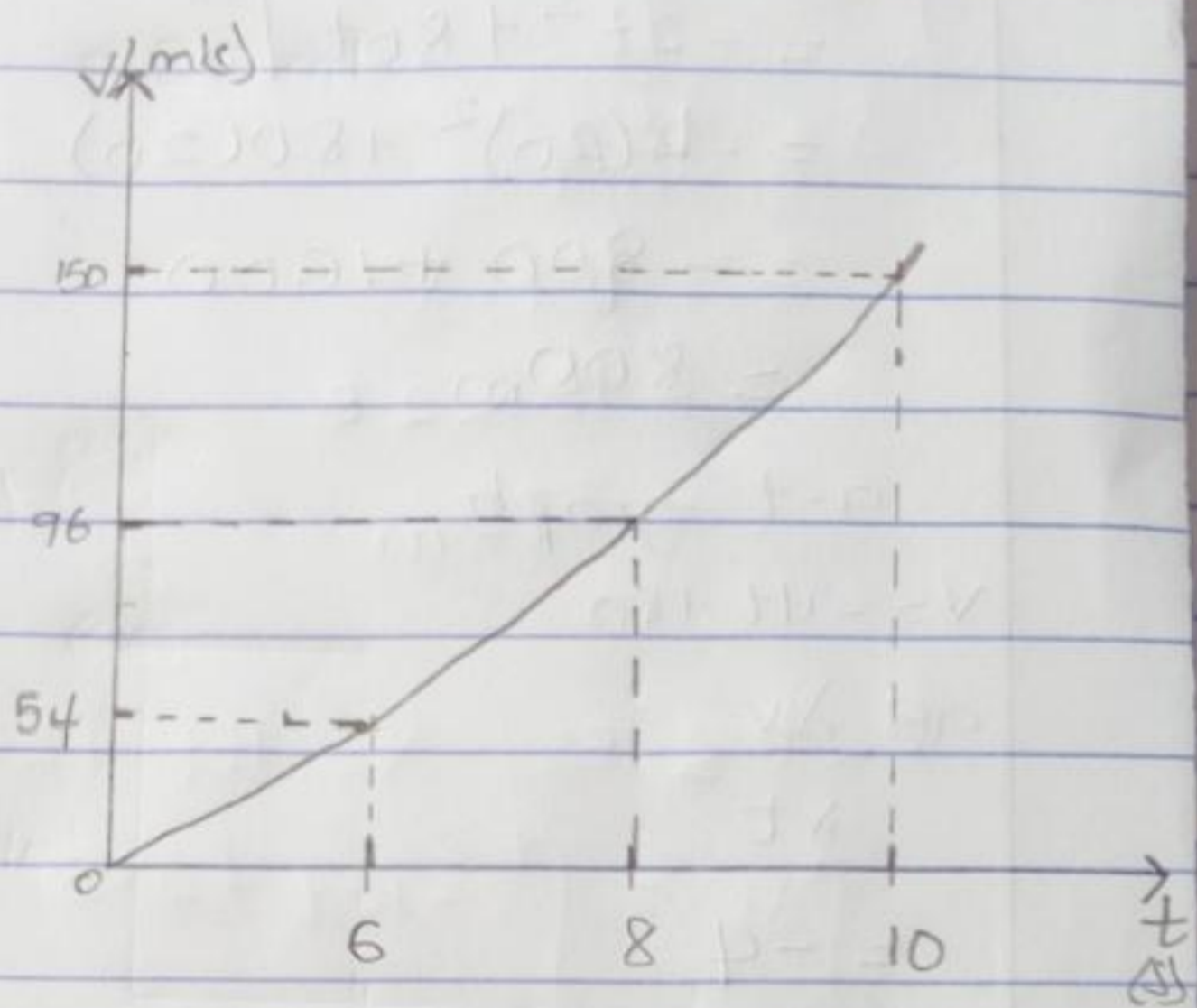
$= 1.5(8)^2$

$= 96 \text{ m/s}$

$v_3 = \frac{\partial S}{\partial t} \Big|_{t=10} = 1.5(t)^2$

$= 1.5(10)^2$

$= 150 \text{ m/s}$



v-t graph

12-10 $v = -4t + 80$

$t_1 = 0 ; t_2 = 20$

$v_1 = -4(0) + 80$

$v_1 = 80$

$v_2 = -4(20) + 80$

$v_2 = 0$

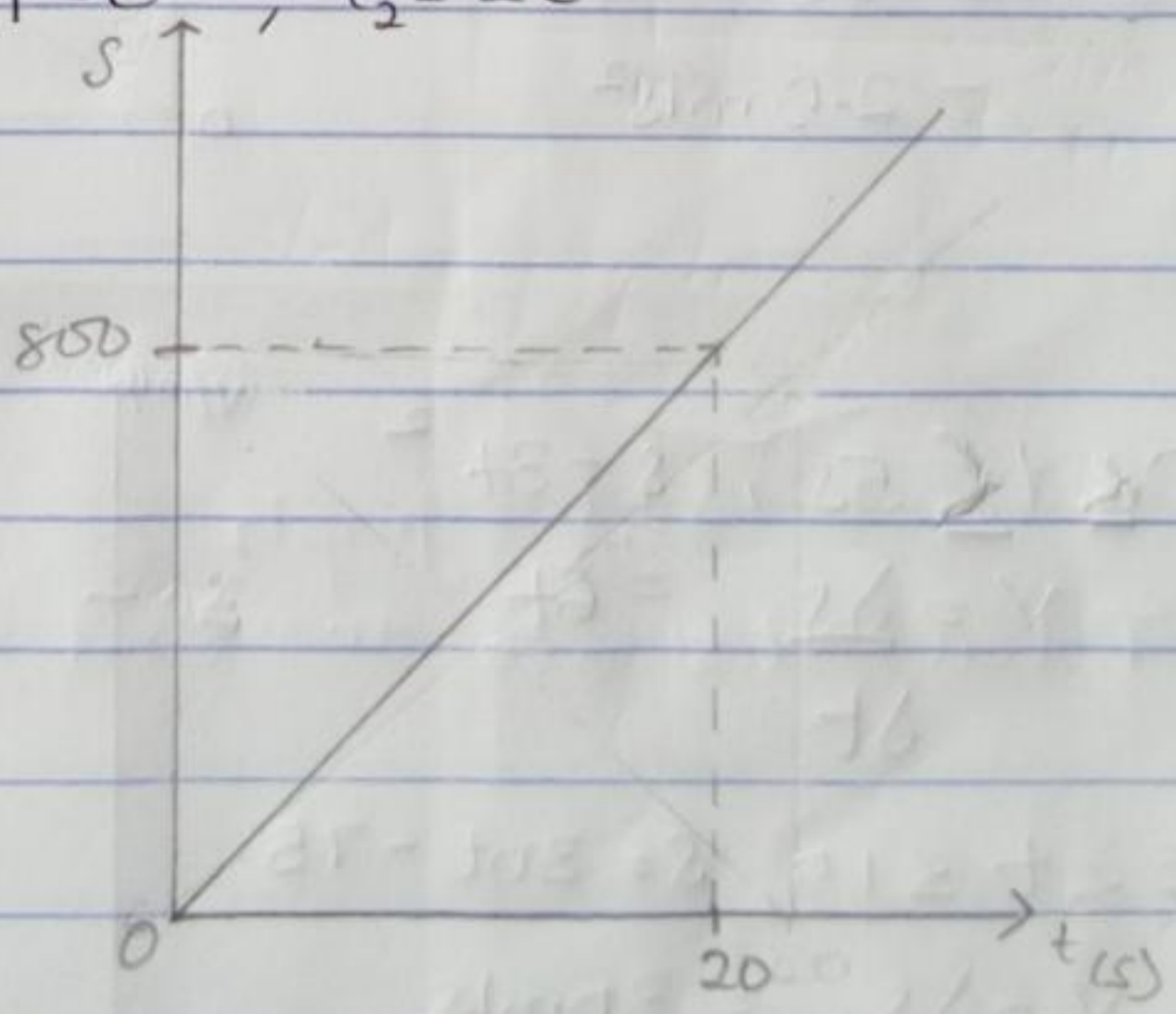
$S_1 = \int v dt$

$= \left[-\frac{4t^2}{2} + 80t \right]_0^{t_1}$

$= -2t_1^2 + 80t_1 \Big|_0^{t_1}$

$= -2(0)^2 + 80(0)$

$= 0 \text{ m}$



s-t graph

$$\begin{aligned}
 s_2 &= \int v dt \\
 &= -2t^2 + 80t \Big|_0^{t_2} \\
 &= -2(20)^2 + 80(20) \\
 &= -800 + 1600 \\
 &= 800\text{m}
 \end{aligned}$$

a-t graph

$$v = -4t + 80$$

$$a = \frac{dv}{dt}$$

$$= -4$$

12-11 $v_2 = 0.25 s$ $\frac{dv}{ds} = 0.25$

$$v_2 = 0.25(40) = 10 \text{ m/s}$$

$$v_1 = 0.25(0) = 0$$

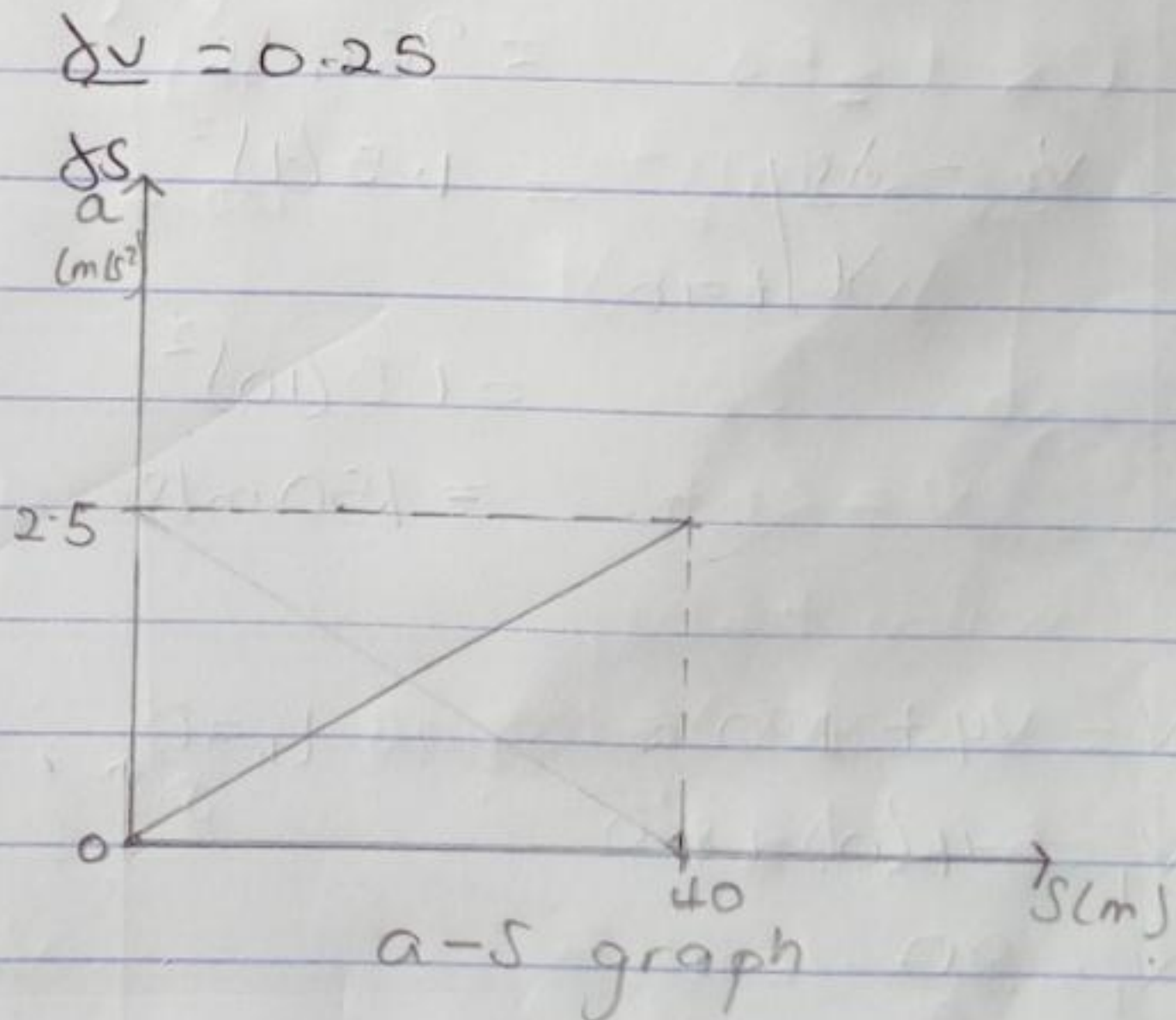
$$a_1 = v_1 \left(\frac{dv}{ds} \right)$$

$$= 0(0.25) = 0$$

$$a_2 = v_2 \left(\frac{dv}{ds} \right)$$

$$= 10(0.25)$$

$$= 2.5 \text{ m/s}^2$$

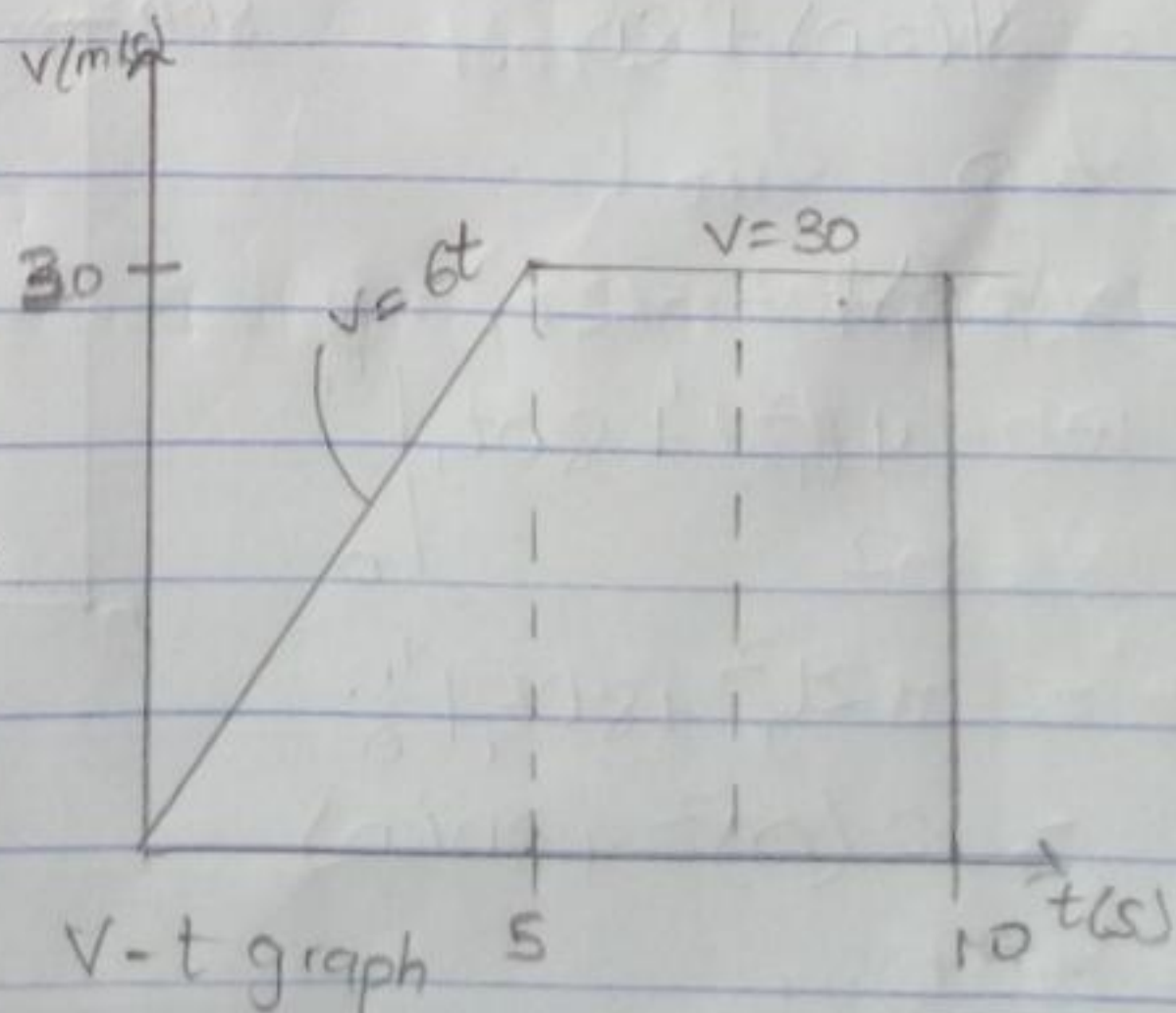


12-12 $0 \leq t \leq 5\text{s}$, $s = 3t^2$

$$v = \frac{ds}{dt} = 6t$$

$$5 < t \leq 10, s = 30t - 75$$

$$v = \frac{ds}{dt} = 30 \text{ m/s}$$



at $t = 7.5\text{s}$, using slope of s-t graph is determined

from the straight line from 5s to 10s

$$v = \frac{\Delta s}{\Delta t} = \frac{225 - 75}{10 - 5} = 30 \text{ m/s}$$

$$\Delta t = 10 - 5$$

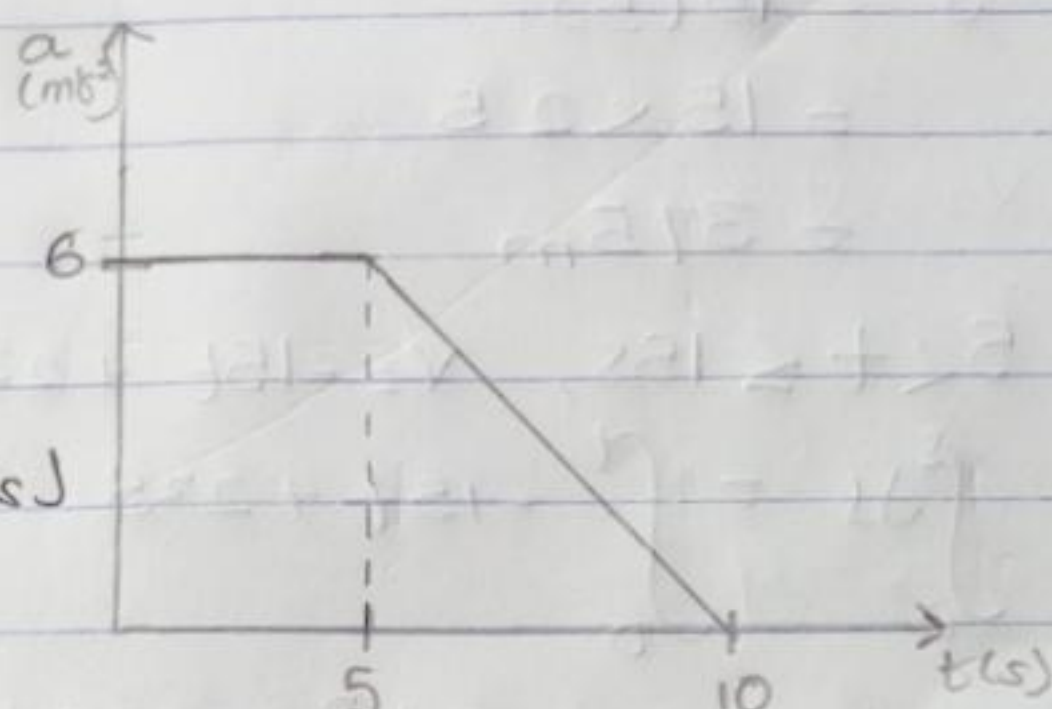
a-t graph

$$0 \leq t < 5s, v = 6t \text{ (m/s)}$$

$$a = \frac{\Delta v}{\Delta t} = 6 \text{ m/s}^2$$

$$5 < t \leq 10s, v = 20 \text{ (m/s)}$$

$$a = \frac{\Delta v}{\Delta t} = 0$$



a-t graph

12-13 $\Delta v = a \Delta t$

$$0 \leq t \leq 5s$$

$$a = 20 \text{ m/s}^2$$

$$\int_0^v \Delta v = \int_0^t 20 \Delta t$$

$$v = 20t$$

when $t = 5s$,

$$v = 20(5) = 100 \text{ m/s}$$

$$5 < t \leq t'$$

$$a = -10 \text{ m/s}^2$$

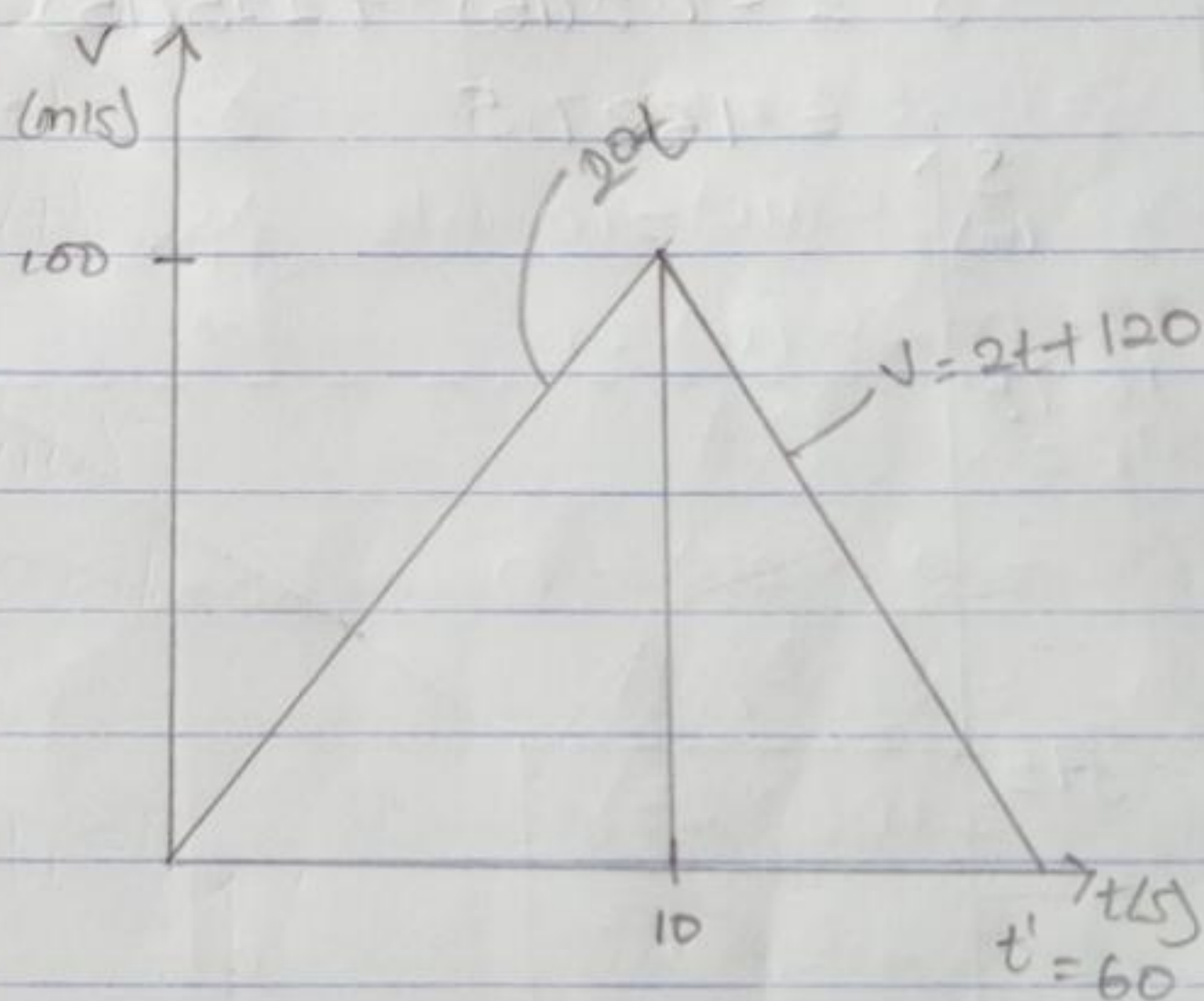
$$\int_{100}^v \Delta v = \int_{100}^t -10 \Delta t$$

$$v = (-10t + 120) \text{ m/s}$$

when $t = t'$

$$v = 0$$

$$t' = 60s$$



v-t graph

12-14 $S = \int v dt$

$$0 \leq t \leq 5s, v = 30t$$

$$\int_0^s ds = \int_0^t 30 dt$$

$$s = 15t^2$$

when $t=5$

$$\begin{aligned} s &= 15(5)^2 \\ &= 15 \times 25 \\ &= 375 \text{ m} \end{aligned}$$

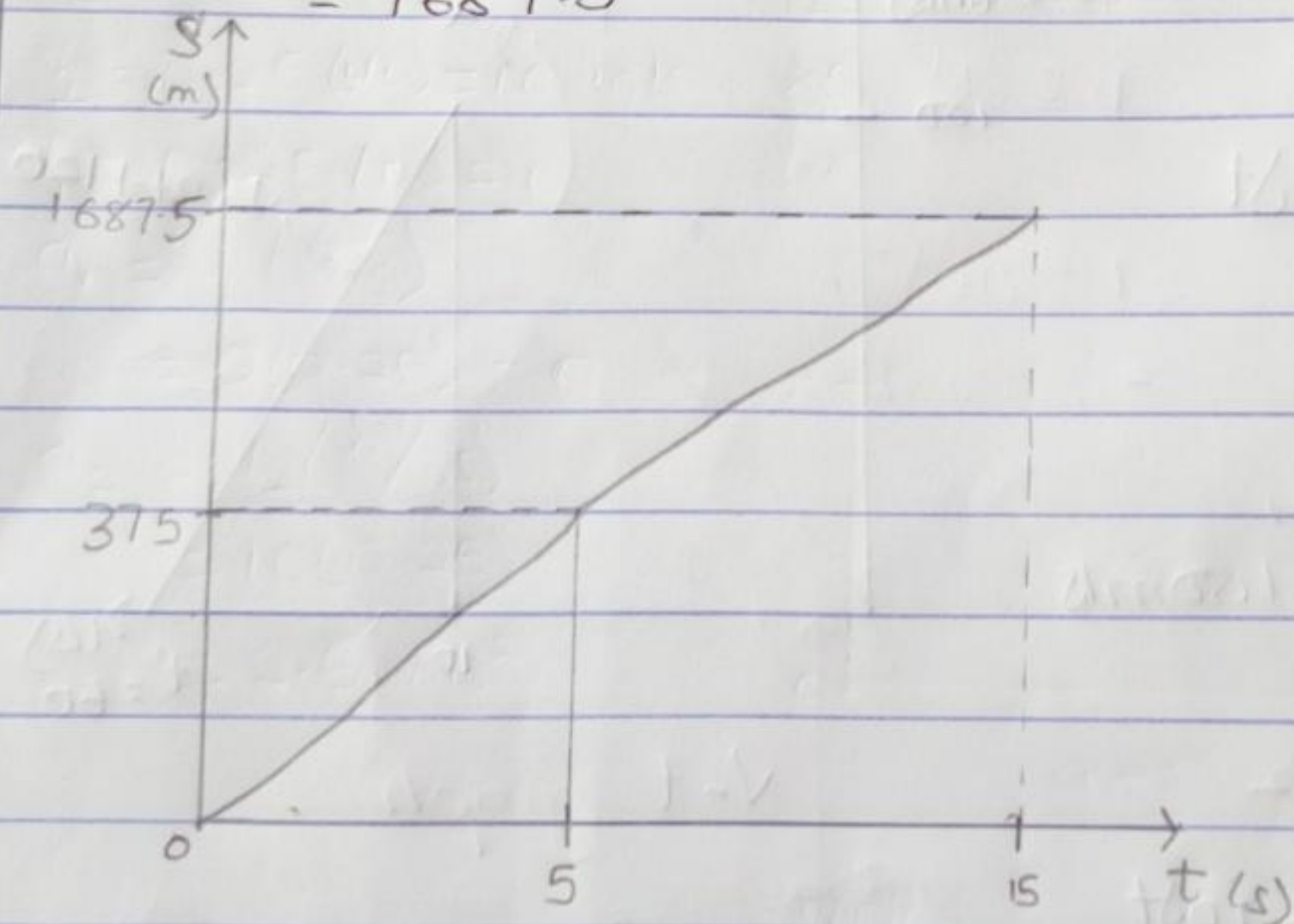
$$5 < t \leq 15, \quad v = -15t + 225$$

$$\int ds = \int -15t + 225$$

$$s = -7.5t^2 + 225t$$

when $t=15$

$$\begin{aligned} s &= -7.5(15)^2 + 225(15) \\ &= 1687.5 \end{aligned}$$



S-t graph

Total distance traveled during time interval is ~~168~~ 1687.5 m