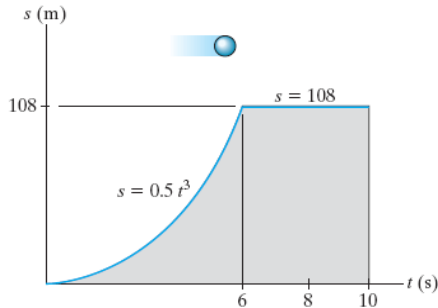


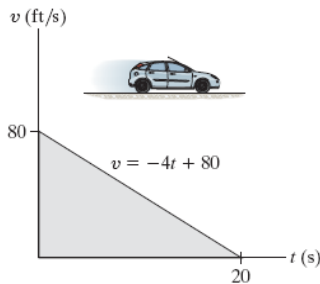
ANSWERS ARE BELOW THE QUESTIONS

F12-9. The particle travels along a straight track such that its position is described by the $s-t$ graph. Construct the $v-t$ graph for the same time interval.



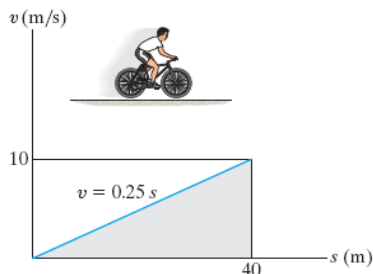
F12-9

F12-10. A van travels along a straight road with a velocity described by the graph. Construct the $s-t$ and $a-t$ graphs during the same period. Take $s = 0$ when $t = 0$.



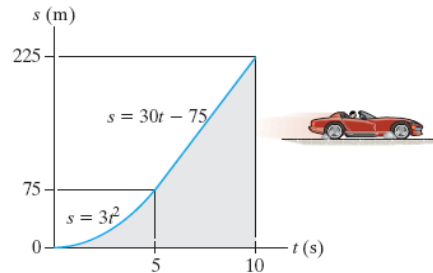
F12-10

F12-11. A bicycle travels along a straight road where its velocity is described by the $v-s$ graph. Construct the $a-s$ graph for the same time interval.



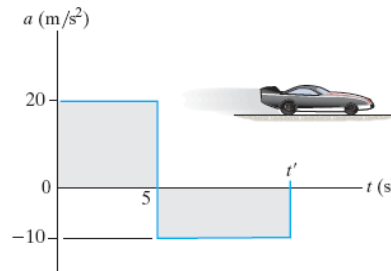
F12-11

F12-12. The sports car travels along a straight road such that its position is described by the graph. Construct the $v-t$ and $a-t$ graphs for the time interval $0 \leq t \leq 10$ s.



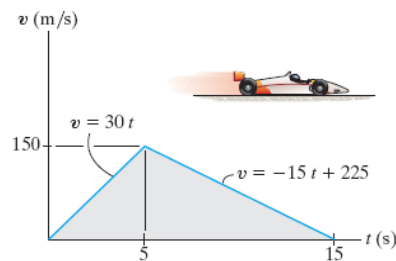
F12-12

F12-13. The dragster starts from rest and has an acceleration described by the graph. Construct the $v-t$ graph for the time interval $0 \leq t \leq t'$, where t' is the time for the car to come to rest.



F12-13

F12-14. The dragster starts from rest and has a velocity described by the graph. Construct the $s-t$ graph during the time interval $0 \leq t \leq 15$ s. Also, determine the total distance traveled during this time interval.

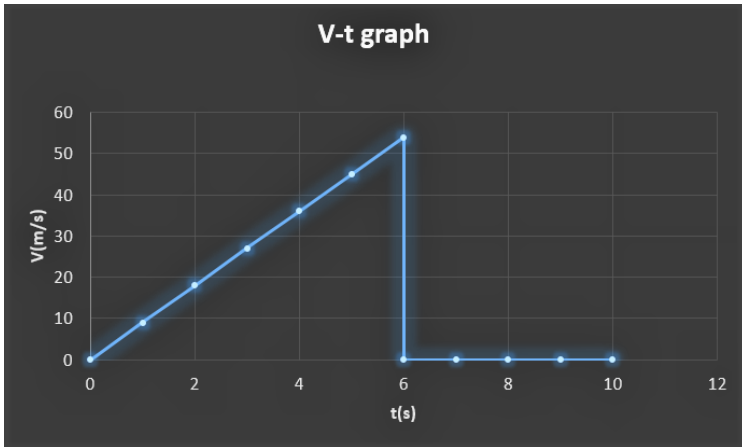


F12-14

NB: Please note, some of the graphs are drawn with free hand because they were quite difficult to draw with software.

ANSWERS

Question 1



$$V = ds/dt$$

$$V = 1.5t^2$$

$$V = 1.5(6)^2$$

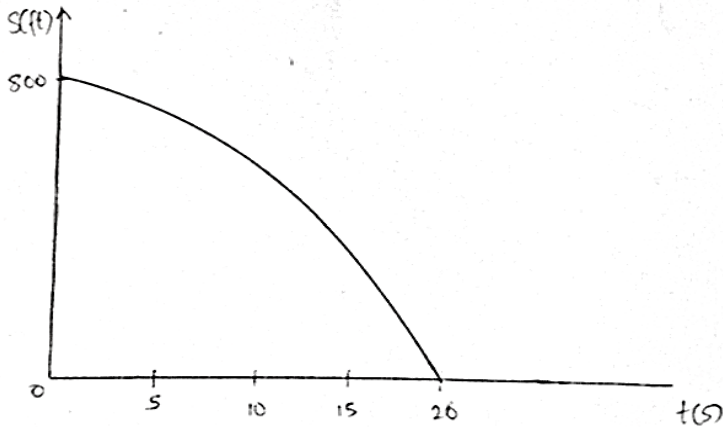
$$V = 1.5 \times 36 = 54 \text{ m/s}$$

Max velocity = 54 m/s @ 6 sec

When $s = 128$, $V = ds/dt$

$$V = 0$$

Question 2



i). $V = -4t + 80$

$$V = ds/dt$$

$$ds = Vdt$$

$$ds = (-4t + 80) dt$$

integrating;

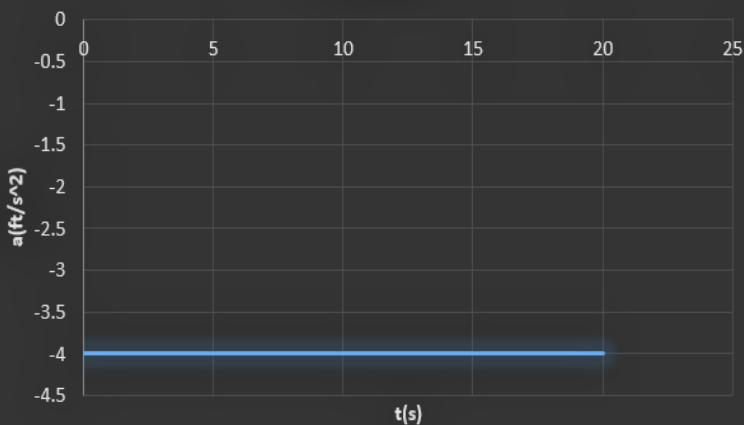
$$\int_0^s ds = \int_0^t (-4t + 80) dt$$

$$|s|_0^s = |-4t^2/2 + 80t|_0^t$$

$$S = -2t^2 + 80t$$

$$@ t = 20 \rightarrow s = -2(20)^2 + 80(20) = 800 \text{ ft.}$$

a-t graph

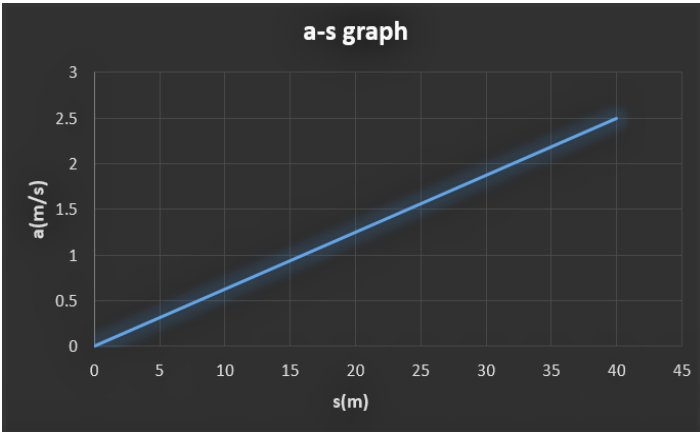


ii). $a = dv/dt$

$$a = \frac{d}{dt} (-4t + 80t)$$

$$\therefore a = -4 \text{ ft/s.}$$

Question 3

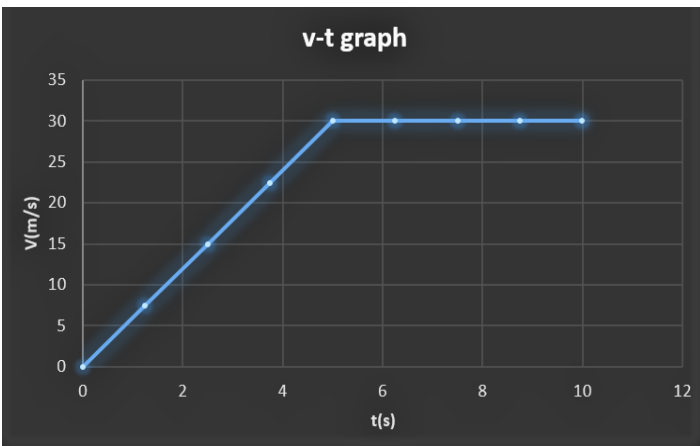


$$a = v \frac{dv}{ds}$$

$$a = \frac{d}{ds} (0.25)(0.25)$$

$$a = 0.0625 \text{ m/s}^2$$

Question 4



From 0 – 5 sec;

$$V = 3t^2$$

$$V = \frac{ds}{dt}$$

$$\therefore V = \frac{d}{dt} (3t^2)$$

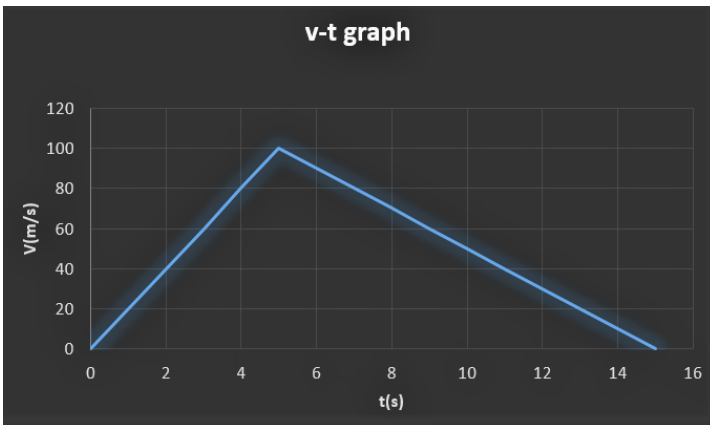
$$V = 6t \text{ m/s @ } t = 5 \rightarrow V = 6(5) = 30 \text{ m/s}$$

From 5 – 10 sec

$$V = \frac{d}{dt} (30t - 75)$$

$$\therefore V = 30 \text{ m/s}$$

Question 5



$$a = dv/dt$$

$$dv = a dt$$

$$\text{when } t = 5, a = 20$$

$$V = a(5)$$

$$\int_0^v dv = \int_0^{t=5} 20 dt$$

$$|v|_0^v = |20t|_0^5$$

$$V = 20(5)$$

$$V = 100 \text{ m/s}$$

$$\text{When } t = t', a = -10$$

$$\int_{100}^v dv = \int_5^t -10 dt$$

$$|v|_{100}^v = |-10|_5^t$$

$$V - 100 = -10t' = 10(5)$$

$$V - 100 = -10t' = 50$$

$$V = 150 - 10t'$$

$V = 0$ when the car is at rest

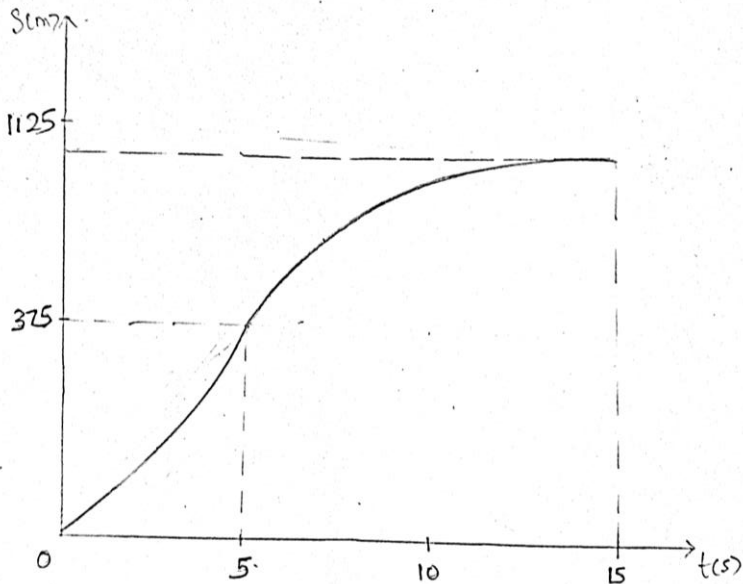
$$0 = 150 - 10t'$$

$$10t' = 150$$

$$t' = \frac{150}{10}$$

$$t' = 15 \text{ sec}$$

Question 6



$$V = ds/dt$$

$$ds = v dt$$

From 0 – 5sec

$$\int_0^s ds = \int_0^5 30t dt$$

$$s = \left| \frac{30t^2}{2} \right|_0^5 = 15t^2 \Big|_0^5$$

$$s = 15(5)^2 = 375\text{m}$$

From 5 – 15 sec

$$ds = (-15t + 225) dt$$

$$\int_{375}^s ds = \int_5^{15} (15t + 225) dt$$

$$s \Big|_{375}^s = \left| \frac{15t^2}{2} + 225t \right|_5^{15}$$

$$s - 375 = \left[\frac{15(15^2)}{2} + 225(15) \right] - \left[\frac{15(5^2)}{2} + 225(5) \right]$$

$$s = 5062.5 - 937.5 - 375$$

$$s = 1125 \text{ m}$$