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Course: General mathematics 101

Dept: MEDICINE AND SURGERY

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Integrate the following functions

1) $2x^2 \ln x$

let $u = \ln x$ $dv = 2x^2$

$du = \frac{1}{x} dx$

$\int u dv = uv - \int v du$
 $= \ln x \cdot \frac{2x^3}{3} - \int \frac{2x^3}{3} \cdot \frac{1}{x} dx$

$= \frac{2x^3}{3} \ln x - \int \frac{2x^2}{3} dx = \frac{2x^3}{3} \ln x - \frac{2x^3}{9} + C$

$\therefore \int 2x^2 \ln x dx = \frac{2x^3}{3} \ln x - \frac{2x^3}{9} + C$

or
 $= \frac{2x^3}{3} (\ln x - \frac{1}{3}) + C$

2) $3te^{2t}$

Solution

let $u = 3t$ $dv = e^{2t}$

$du = 3 dt$ $v = \frac{1}{2} e^{2t}$

$\int u dv = uv - \int v du$

$\int 3te^{2t} = 3t \cdot \frac{1}{2} e^{2t} - \int \frac{1}{2} e^{2t} \cdot 3 dt$

$\int 3te^{2t} = \frac{3t}{2} e^{2t} - \int \frac{3}{2} e^{2t} dt$

$= \frac{3t}{2} e^{2t} - \frac{1}{2} \cdot \frac{3}{2} e^{2t} + C$

$\therefore \int 3te^{2t} dt = \left[\frac{3t}{2} e^{2t} - \frac{3e^{2t}}{4} \right] + C$

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3) $x^2 \sin x$

Solution

$$u = x^2 \quad dv = \sin x$$

$$\frac{du}{dx} = 2x \quad v = -\cos x$$

$$dx = 2x dx$$

$$\int u dv = uv - \int v du$$

$$\int x^2 \sin x dx = -x^2 \cos x - \int (-\cos x) \cdot 2x dx$$

$$= -x^2 \cos x + \int 2x \cos x dx$$

$$\therefore -x^2 \cos x + \int 2x \cos x dx$$

$$= \left[\begin{array}{l} u = 2x \\ du = 2 dx \\ dv = \cos x \\ v = \sin x \end{array} \right]$$

$$= -x^2 \cos x + uv - \int v du$$

$$\int x^2 \sin x = -x^2 \cos x + 2x \sin x - \int \sin x \cdot 2 dx$$

$$\therefore \int x^2 \sin x dx = -x^2 \cos x + 2x \sin x - \int 2 \sin x$$

$$\therefore \int x^2 \sin x dx = -x^2 \cos x + 2x \sin x + 2 \cos x + c$$

4) $\cos 5x \cos 6x$

Solution

let $y = 5x, z = 6x$

Recall that

$$\cos A \cos B = \frac{1}{2} [\cos(A+B) + \cos(A-B)]$$

$$= \frac{1}{2} \int \cos 11x + \cos x$$

$$\int \cos 5x \cos 6x dx = \frac{1}{2} \left[\frac{\sin 11x}{11} + \sin x \right] + c$$

$$\therefore \int \cos 5x \cos 6x dx = \frac{\sin 11x}{22} + \frac{\sin x}{2} + c$$

5) $\sin 7x \cos 2x$

Solution

$y = 7x \quad z = 2x$

Recall that; $\sin A \cos B = \frac{1}{2} [\sin(A+B) + \sin(A-B)]$

$$\int \sin 7x \cos 2x dx = \frac{1}{2} (\sin 9x + \sin 5x) = \frac{1}{2} \left[\frac{-\cos 9x}{9} - \frac{\cos 5x}{5} \right] + c$$

$$\therefore \int \sin 7x \cos 2x dx = \frac{-\cos 9x}{18} - \frac{\cos 5x}{10} + c$$