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$$1) \int 2x^2 \ln x \, dx$$

$$u = \ln x \quad dv = 2x^2$$

$$du = \frac{1}{x} dx \quad v = \frac{2x^3}{3}$$

$$\begin{aligned} \int u \, dv &= uv - \int v \, du \\ &= \frac{1}{3} \cdot 2x^3 \ln x - \int \frac{2x^3}{3} \cdot \frac{1}{x} dx \\ &= \frac{2x^3}{3} \ln x - \frac{1}{3} \int 2x^2 \, dx \\ &= \frac{2x^3}{3} \ln x - \frac{2x^3}{9} + C \end{aligned}$$

$$2) \int 3t e^{2t} \, dt$$

$$u = 3t \quad dv = e^{2t}$$

$$du = 3 \quad v = \frac{e^{2t}}{2}$$

$$\begin{aligned} \int u \, dv &= uv - \int v \, du \\ &= 3t \cdot \frac{e^{2t}}{2} - \int \frac{e^{2t}}{2} \cdot 3 \, dt \\ &= \frac{3e^{2t}t}{2} - \frac{3}{2} \int e^{2t} \, dt \\ &= \frac{3e^{2t}t}{2} - \frac{3e^{2t}}{4} + C \end{aligned}$$

$$3) x^2 \sin x$$

$$u = x^2$$

$$du = 2x dx$$

$$= -x^2 \cos x + \int \cos x \cdot 2x dx$$

$$u = 2x$$

$$du = 2 dx$$

$$\Rightarrow 2x \sin x = \int \sin u \cdot 2 dx$$

$$= -x^2 \cos x + 2x \sin x - \int \sin x \cdot 2 dx$$

$$= -x^2 \cos x + 2x \sin x + 2 \cos x$$

$$-dv = \sin x$$

$$v = -\cos x$$

$$dv = \cos x$$

$$v = \sin x$$

$$4) \cos 5x \cos 6x$$

$$\cos A \cos B = \frac{1}{2} [\cos(A+B) + \cos(A-B)]$$

$$A = 5x, B = 6x$$

$$\int \cos 5x \cos 6x dx = \int \frac{1}{2} [\cos 11x + \cos x] dx$$

$$= \frac{1}{2} \left[\frac{\sin 11x}{11} + \sin x \right]$$

$$= \frac{\sin 11x}{22} + \frac{\sin x}{2} + C$$

$$5) \sin 7x \cos 2x$$

$$\sin A \cos B = \frac{1}{2} [\sin(A+B) + \sin(A-B)]$$

$$A = 7x, B = 2x$$

$$\int \sin 7x \cos 2x dx = \frac{1}{2} (\sin 9x + \sin 5x)$$

$$= \frac{1}{2} \frac{\sin 9x}{9} + \frac{\sin 5x}{5}$$

$$= \frac{\sin 9x}{18} + \frac{\sin 5x}{10}$$