

Jobo Alexander Ithofu  
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MBBS/MHS

$$\int 2x^2 \ln x \, dx$$

$$\int u \, dv = uv - \int v \, du$$

$$u = 2x^2, \, du = 4x \, dx; \, dv = \ln x \, dx, \, v = x \ln x - x$$

$$\int 2x^2 \ln x \, dx = 2x^2 \times (x \ln x - x) - \int x \ln x - x \times 4x \, dx$$

$$\int 2x^2 \ln x \, dx = 2x^3 \ln x - 2x^3 - \int 4x^2 \ln x - 4x^2$$

$$\int 2x^2 \ln x \, dx = 2x^3 \ln x - 2x^3 - \int 4x^2 (\ln x - 1)$$

$$\int 2x^2 \ln x \, dx = 2x^3 \ln x - 2x^3 - \frac{4x^3}{3} \int (\ln x - 1)$$

$$\int 2x^2 \ln x \, dx = 2x^3 \ln x - 2x^3 - \frac{4x^3}{3} ((x \ln x - x) - x) - 2x^3$$

$$\int 2x^2 \ln x \, dx = 2x^3 \ln x - 2x^3 - \frac{4x^3 \ln x}{3} - \frac{8x^3}{3}$$

$$\int 2x^2 \ln x \, dx = 2x^3 \left( \ln x - \frac{2 \ln x}{3} - \frac{4x}{3} - 1 \right) + C$$

$$\int 3t e^{2t} \, dt$$

$$\int u \, dv = uv - \int v \, du$$

$$u = 3t, \, du = 3 \, dt; \, dv = e^{2t} \, dt, \, v = \frac{e^{2t}}{2}$$

$$\int 3t e^{2t} \, dt = 3t \frac{e^{2t}}{2} - \int \frac{e^{2t}}{2} \times 3$$

$$\int 3t e^{2t} \, dt = \frac{3t e^{2t}}{2} - \int \frac{3e^{2t}}{2}$$

$$\int 3t e^{2t} \, dt = 3t e^{2t} - \frac{3}{2} e^{2t}$$

$$\int 3t e^{2t} \, dt = \frac{3t e^{2t}}{2} - \frac{3e^{2t}}{4} + C$$

$$3. \int x^2 \sin x dx$$

$$u = x^2 \quad du = 2x dx \quad v = \sin x \quad dv = \cos x dx \quad w = -\cos x$$

$$\int u dv = uv - \int v du$$

$$\int x^2 \sin x dx = x^2 (-\cos x) - \int (-\cos x) 2x dx$$

$$x^2 \sin x dx = x^2 (-\cos x) + \int 2x \cos x dx$$

$$\int 2x \cos x = 2x \sin x - \int \sin x \times 2 \quad (u = 2x, \quad du = 2 dx, \quad dv = \cos x, \quad v = \sin x)$$

$$\int 2x \cos x = 2x \sin x - 2 \int \sin x$$

$$\int 2x \cos x = 2x \sin x - 2 \cos x$$

$$\int x^2 \sin x dx = -x^2 \cos x + 2x \sin x + 2 \cos x + C$$

$$4. \int \cos 5x \cos 6x dx = \frac{1}{2} \int [\cos(A+B) + \cos(A-B)] \quad (A = 5x, B = 6x)$$

$$= \frac{1}{2} \int [\cos(5x+6x) + \cos(5x-6x)]$$

$$= \frac{1}{2} \int [\cos 11x - \cos x]$$

$$= \frac{1}{2} \left[ \frac{\sin 11x}{11} - \sin x \right]$$

$$= \frac{\sin 11x}{22} - \frac{\sin x}{2} + C$$

$$5. \int \sin 7x \cos 2x dx = \frac{1}{2} \int [\sin(7x+2x) + \sin(7x-2x)] \quad (A = 7x, B = 2x)$$

$$= \frac{1}{2} \int (\sin 9x + \sin 5x) dx$$

$$= \frac{1}{2} \left[ \frac{-\cos 9x}{9} - \frac{\cos 5x}{5} \right]$$

$$= -\frac{\cos 9x}{18} - \frac{\cos 5x}{10} + C$$