

$$\frac{dy}{dx} = \frac{10}{1.6094} - \frac{3.1}{2.5902}$$

$$\frac{dy}{dx} = 6.2133 - 1.1967$$

$$\frac{dy}{dx} = 5.01657$$

$$\frac{dy}{dx} \approx 5.02 \text{ to 3 s.f.}$$

2) $y = 2x/(x^2 - 5)$ at point $(2, -4)$

$$y = \frac{2x}{x^2 - 5}$$

u v

$$\frac{dy}{dx} = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$$

$$\frac{du}{dx} = 2$$

$$\frac{dv}{dx} = 2x$$

$$\frac{x^2 - 5(2) - 7x(2)}{(x^2 - 5)^2}$$

$$\frac{dy}{dx} = \frac{2x^2 - 10 - 4x^2}{x^4 - 10x^2 + 25}$$

$$m = \frac{dy}{dx} \quad y - y_1 = m(x - x_1)$$

$$m = \frac{2x^2 - 10 - 4x^2}{x^4 - 10x^2 + 25}$$

$$\text{at } x = 2$$

$$m = \frac{2(2)^2 - 10 - 4(2)^2}{(2)^4 - 10(2)^2 + 25}$$

$$m = \frac{8 - 10 - 16}{16 - 40 + 25} = \frac{-18}{1}$$

$$m_1 = -18$$

$$\text{at } x = -4$$

~~$$m = \frac{2x^2 - 10 - 4x^2}{x^4 - 10x^2 + 25}$$~~

$$\int_0^2 \frac{x^2}{2} \times \frac{(2x^2+1)^{3/2}}{3/2}$$

when $x=2$

$$\frac{4}{2} \times \frac{(9)^{3/2}}{3/2}$$

$$2 \times \frac{27}{3/2}$$

$$2 \times 18 \\ = 36$$

at $x=0 = 0$

upper bound - lower bound

$$= 36 - 0$$

$$\therefore \int_0^2 x(2x^2+1) dx$$

$$= 36.$$

$$\frac{-2(-4)^2 - 10}{(-4)^4 - 10(-4)^2 + 25}$$

$$m = \frac{-32 - 10}{256 - 160 + 25} = \frac{-42}{121}$$

$$m = \frac{2(-4)^2 - 10 - 4(-4)^2}{(-4)^4 - 10(-4)^2 + 25}$$

$$m = \frac{32 - 10 - 64}{256 - 160 + 25} = \frac{-42}{121}$$

$$m = -0.35$$

$$m = -18 \text{ and } m = -0.35 //$$

$$3) z = 2x^3 \ln y,$$

$$\frac{dz}{dy} = 3.$$

$$u = 2x^2 + 1$$

$$2x^2 = u - 1$$

$$x^2 = \frac{u-1}{2}$$

$$x = \frac{\sqrt{u-1}}{2}$$

$$\int x \cdot \sqrt{u} \cdot \frac{du}{2x}$$

$$\int_0^2 \sqrt{\frac{u-1}{2}} \cdot \sqrt{u} \cdot \frac{du}{2x}$$

$$\int_0^2 \sqrt{\frac{2x^2+1-1}{2}} \cdot \sqrt{2x^2+1} \cdot \frac{du}{4x}$$

$$\int_0^2 \sqrt{\frac{2x^2}{2}} \cdot \sqrt{2x^2+1} \cdot \frac{du}{2x}$$

$$\int_0^2 x = (2x^2+1)^{1/2}$$