

1.  $D = 1.5 \text{ km} = 1.5 \times 10^3 \text{ m} = 1500 \text{ m}$

Schedule speed =  $36 \text{ km/h} = \frac{36 \times 1000}{60 \times 60} = 10 \text{ m/s}$

$\beta = 8 \text{ km/h/s} = \frac{8 \times 1000}{60 \times 60} = \frac{80}{36} = \frac{5}{6} \text{ m/s}^2$  or  $0.83 \text{ m/s}^2$

Schedule time of run =  $\frac{1500}{10} = 150 \text{ s}$

Actual time of run =  $150 - 25 = 125 \text{ s}$

$V_a = \frac{1500}{125} = 12 \text{ m/s}$

$V_m = 1.25 \times 12 = 15 \text{ m/s}$

$K = \frac{D}{V_m^2} \left( \frac{V_m}{V_a} - 1 \right) = \frac{1500}{15^2} (1.25 - 1) = \frac{5}{3}$  or  $1.67$

$K = \frac{1}{2} \left( \frac{1}{\alpha} + \frac{1}{\beta} \right)$

substituting the values for K and  $\beta$

$\frac{5}{3} = \frac{1}{2} \left( \frac{1}{\alpha} + \frac{6}{5} \right)$

$\frac{10}{3} = \frac{5 + 6\alpha}{5\alpha}$

$50\alpha = 15 + 18\alpha$

$50\alpha - 18\alpha = 15$

$32\alpha = 15$

$\alpha = \frac{15}{32} = 0.47 \text{ m/s}^2 = 0.47 \times \frac{1000}{60 \times 60} = 1.7 \text{ km/h/s}$

$$2 \quad V_a = 36 \text{ km/h} = \frac{36 \times 1000}{60 \times 60} = 10 \text{ m/s}$$

$$\alpha = 1.8 \text{ km/h/s} = \frac{1.8 \times 1000}{60 \times 60} = 0.5 \text{ m/s}^2$$

$$\beta = 3.6 \text{ km/h/s} = \frac{3.6 \times 1000}{60 \times 60} = 1 \text{ m/s}^2$$

$$D = 2 \text{ km} = 2000 \text{ m}$$

$$t = \frac{D}{V_a} = \frac{2000}{10} = 200 \text{ s}$$

$$K = \frac{1}{2} \left( \frac{1}{\alpha} + \frac{1}{\beta} \right)$$

$$K = \frac{1}{2} \left( \frac{2}{1} + \frac{1}{1} \right) = \frac{3}{2} = 1.5$$

$$V_m = \frac{t - \sqrt{t^2 - 4KD}}{2K} = \frac{200 - \sqrt{(200)^2 - 4 \times 1.5 \times 2000}}{2 \times 1.5}$$

$$V_m = \frac{200 - \sqrt{40000 - 12000}}{3}$$

$$= \frac{200 - \sqrt{28000}}{3} = \frac{200 - 167.33}{3} = \frac{32.67}{3} = 10.89 \text{ m/s}$$

$$V_m = 10.89 \text{ m/s} = 10.89 \times \frac{1000}{60 \times 60} = 39.2 \text{ km/h}$$



$$3. \text{ surface area, } A = 6.0 \text{ m}^2$$

$$90\% = 0.9$$

$$T_1 = 20^\circ\text{C}$$

$$T_2 = 65^\circ\text{C}$$

$$\text{loss per square metre per } 1^\circ\text{C} = 6.3 \text{ W}/^\circ\text{C}/\text{m}^2$$

$$\text{Specific heat, } s = 4200 \text{ J}/\text{kg}/^\circ\text{C}$$

$$1 \text{ kWh} = 3.6 \text{ MJ}$$

$$\text{Assume } A = 6 \times l^2$$

$$\therefore 6 = 6 \times l^2$$

$$l = 1 \text{ m}^2$$

$$\text{Volume} = 1 \text{ m}^3$$

$$\text{Volume of water to be heated daily, } V_d = 6 \times 1 \times 0.9 = 5.4 \text{ m}^3$$

Since  $1 \text{ m}^3$  of water weighs  $1000 \text{ kg}$

$$\therefore \text{mass of water to be heated daily, } m = V_d \times 1000 = 5.4 \times 1000 = 5400 \text{ kg}$$

$$\text{Heat required to raise temp, } H = m \times s \times \Delta T$$

$$= 5400 \times 4200 \times 45$$

$$= 1020 \text{ MJ}$$

$$\text{converting to kWh} = \frac{1020}{3.6} = 283.3 \text{ kWh}$$

$$\text{Daily loss from the surface of the tank} = 6.3 \times 6 \times (65 - 20) \times \frac{24}{1000}$$

$$= 40.8 \text{ kWh}$$

$$\text{Energy supplied daily} = 283.3 + 40.8 = 324.1 \text{ kWh}$$

$$\text{Loading in kW} = \frac{324.1}{24} = 13.5 \text{ kW}$$

$$\text{Efficiency of tank} = \frac{283.3}{324.1} \times 100 = 87.4\%$$

4 Secondary voltage,  $V = 20V$

Input Power,  $P = 600KW$  or  $600 \times 10^3W$

Power Factor,  $pf = 0.6$

$$\text{Secondary current, } I = \frac{P}{V \times pf} = \frac{600 \times 1000}{20 \times 0.6} = 5 \times 10^4 A$$

$$\text{Voltage across resistance, } V_r = V \times pf = 20 \times 0.6 = 12V$$

$$\text{Voltage across reactance, } V_x = V \times \sqrt{1 - pf^2} = 20 \times \sqrt{1 - 0.6^2} = 16V$$

$$V_r = I \times R; R = \frac{V_r}{I} = \frac{12}{5 \times 10^4} = 2.4 \times 10^{-4} \Omega$$

$$V_x = I \times X; X = \frac{V_x}{I} = \frac{16}{5 \times 10^4} = 3.2 \times 10^{-4} \Omega$$

when hearth is half-full

$$R_2 = 2 \times R = 2 \times 2.4 \times 10^{-4} = 4.8 \times 10^{-4} \Omega$$

$$X_2 = X = 3.2 \times 10^{-4} \Omega$$

$$pf_2 = \frac{R_2}{\sqrt{R_2^2 + X_2^2}} = \frac{4.8 \times 10^{-4}}{\sqrt{(4.8 \times 10^{-4})^2 + (3.2 \times 10^{-4})^2}} = 0.83$$

$$V_{r_2} = V \times pf_2 = 20 \times 0.83 = 16.6V$$

From  $V_r = I \times R$

$$I_2 = \frac{V_{r_2}}{R_2} = \frac{16.6}{4.8 \times 10^{-4}} = 34583.3A \text{ or } 3.5 \times 10^4 A$$

$$\text{Power absorbed, } P_2 = \frac{V \times I_2 \times pf}{1000} = \frac{20 \times 3.5 \times 10^4 \times 0.83}{1000}$$

$$\text{Power absorbed, } P_2 = 581KW$$

$$\text{Power factor, } pf = 0.83$$



B. Intensity,  $I = 300 \text{ cd}$   
 height,  $h = 20 \text{ m}$   
 diameter of luminous area,  $d = 20 \text{ m}$

WITHOUT REFLECTOR

$$\textcircled{a} E_c = \frac{I}{h^2} = \frac{300}{20 \times 20} = \frac{3}{4} = 0.75 \text{ lumens/m}^2$$

$$\textcircled{b} \theta = \tan^{-1} \left[ \frac{d/2}{h} \right] = \tan^{-1} \left[ \frac{20/2}{20} \right] = \tan^{-1}(0.5) = 26.6^\circ$$

distance between edge and source lamp

$$l^2 = h^2 + \left( \frac{d}{2} \right)^2$$

$$l = \sqrt{20^2 + \left( \frac{20}{2} \right)^2} = 22.36 \text{ m}$$

$$E_d = \frac{I}{l^2} \times \cos \theta = \frac{300}{22.36^2} \times \cos(26.6) = 0.537 \text{ lumens/m}^2$$

WITH REFLECTOR

Luminous output of the lamp,  $= 4\pi I = 4\pi \times 300 = 3769.9 \text{ lumens}$

Flux directed by the reflector  $= 0.5 \times 4\pi I = 1884.96 \text{ lumens}$

Area of disc  $= \frac{\pi d^2}{4} = \frac{\pi \times 20^2}{4} = 314.2 \text{ m}^2$

Illumination at every point  $E_p = \frac{0.5 \times 4\pi I}{A}$

$$= \frac{1884.96}{314.2} = 5.99 \text{ lumens/m}^2$$