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COMPUTER ENGINEERING

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MAT 104

QUIZ ASSIGNMENT

1) $\frac{dy}{dx}$ at $x=2.5$ given $y = (2x^2+3)/\ln 2x$

Let $u = (2x^2+3)$ and $v = \ln 2x$

$\frac{du}{dx} = 4x$ $\frac{dv}{dx} = \frac{1}{2x}$

$\frac{dy}{dx} = \frac{u \frac{dv}{dx} - v \frac{du}{dx}}{v^2}$

$\frac{dy}{dx} = \frac{dy}{dx} = \frac{\ln 2x(4x) - (2x^2+3) \frac{1}{2x}}{(\ln 2x)^2}$

$\frac{dy}{dx} = \frac{4x \ln 2x - \frac{2x^2+3}{2x}}{(\ln 2x)^2}$

At $x=2.5$

$= \frac{4(2.5) \ln(2.5) - \frac{2(2.5)^2+3}{2(2.5)}}{(\ln(2.5))^2} = \frac{16.09 - 6.063}{2.590} = 3.1$

$= \frac{9.163 - 3.1}{2.590} = \frac{6.063}{2.590} = 5.015$
 $= 5.02 \text{ to } 3 \text{ s.f.}$
 $= 2.34$

2) $y = \frac{2x}{x^2-5}$ at the point (2,4).

Let $u = 2x$ and let $v = x^2-5$

$\frac{du}{dx} = 2$ $\frac{dv}{dx} = 2x$

$$\begin{aligned} \frac{d}{dx} &= \frac{V \frac{dV}{dx} - U \frac{dU}{dx}}{V^2} \\ &= \frac{(x^2-5)(2) - 2x(2x)}{(x^2-5)^2} \\ &= \frac{2x^2-10-4x^2}{(x^2-5)^2} \\ &= \frac{-2x^2-10}{(x^2-5)^2} \\ &= \frac{-18}{(x^2-5)^2} \end{aligned}$$

$$x=2$$

$$\begin{aligned} m = \frac{dy}{dx} &= \frac{-2(2)^2-10}{(2^2-5)^2} \\ &= \frac{-8-10}{(4-5)^2} \\ &= \frac{-18}{-1} \\ &= 18 \end{aligned}$$

$$m = -18$$

3) If $z = 2x^3 \ln y$, find $\frac{dz}{dy}$

$$\frac{dz}{dy} = \text{Let } U = 2x^3 \text{ and } V = \ln y$$

$$\frac{dU}{dy} = 6x^2 \frac{dx}{dy} \quad \frac{dV}{dy} = \frac{1}{y}$$

$$\frac{dz}{dy} = U \frac{dV}{dy} + V \frac{dU}{dy}$$

$$\begin{aligned} \frac{dz}{dy} &= 2x^3 \left(\frac{1}{y}\right) + \ln y (6x^2 \frac{dx}{dy}) \\ &= \frac{2x^3}{y} + 6x^2 \ln y \frac{dx}{dy} = 0 \end{aligned}$$

$$(6x^2 \ln y) \frac{dz}{dy} = -\frac{2x^3}{y}$$

$$\frac{dz}{dy} = \frac{-\frac{2x^3}{y}}{6x^2 \ln y} = -\frac{2x^3}{6x^2 y \ln y} = -\frac{2x}{6xy \ln y} = -\frac{1}{3y \ln y}$$

$$\frac{dz}{dy} = \frac{-2x^3}{6x^2 y \ln y} //$$

4) Integrate $\int x(2x^2+1)^{\frac{1}{2}} dx$ from (0 to 2).

$$\int_0^2 x(2x^2+1)^{\frac{1}{2}} dx$$

$$\text{Let } u = 2x^2 + 1$$

$$\frac{du}{dx} = 4x$$

$$du = 4x dx$$

$$dx = \frac{du}{4x}$$

$$\int_0^2 x \cdot u^{\frac{1}{2}} \cdot \frac{du}{4x} = \int_0^2 u^{\frac{1}{2}} \cdot \frac{du}{4}$$

$$\frac{1}{4} \int_0^2 u^{\frac{1}{2}} du$$

$$= \frac{1}{4} \left[\frac{u^{\frac{3}{2}}}{\frac{3}{2}} \right]_0^2$$

$$= \frac{1}{4} \left[\frac{u^{3/2}}{\frac{3}{2}} \right]_0^2 = \frac{u^{3/2}}{6}$$

$$= \frac{1}{6} \left[(2x^2+1)^{3/2} + C \right]_0^2$$
$$= \frac{1}{6} \left[\frac{[2(2)^2+1]^{3/2}}{6} \right] - \left[\frac{[2(0)^2+1]^{3/2}}{6} \right]$$

$$= \left[\frac{[9]^{3/2}}{6} \right] - \left[\frac{[1]^{3/2}}{6} \right]$$

$$= 4.5 - 0.167$$

$$= 4.33 //$$