

Derivation of the derivative of $\ln(x^2 + 1)$

$$\frac{d}{dx} \ln(x^2 + 1) = \frac{1}{x^2 + 1} \cdot \frac{d}{dx} (x^2 + 1)$$

$$= \frac{2x}{x^2 + 1}$$

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$$1) \frac{d}{dx} \left[\frac{x^2}{x^2 - 5} \right]$$

$$= \frac{2x \cdot \frac{d}{dx} (x^2 - 5) - x^2 \cdot \frac{d}{dx} (x^2 - 5)}{(x^2 - 5)^2}$$

$$= \frac{2x(2x) - x^2(2x)}{(x^2 - 5)^2}$$

$$= \frac{2x(2x - x^2)}{(x^2 - 5)^2}$$

$$= \frac{2x(2 - x)}{(x^2 - 5)^2}$$

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3) $2 = 2x^3 \ln x$
 $x = 2x^2$
 $\frac{d}{dx} 2 = 0$
 $\frac{d}{dx} 2x^3 \ln x = 2 \cdot 3x^2 \ln x + 2x^3 \cdot \frac{1}{x}$
 $= 6x^2 \ln x + 2x^2$

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u = ln(x)

3) $u = \frac{-2(2)^2 - 10}{(2)^2 - 5} = -18$

Gradient = -18

3) $z = 2x^3 \ln y$
 $u = 2x^3$ $u = \ln y$

$\frac{dz}{dy} = 6x^2 \frac{du}{dy}$ $\frac{dz}{dy} = \frac{1}{y}$

$\frac{dz}{dy} = 2x^3 \cdot \frac{1}{y} + \ln y \cdot 6x^2 \frac{dx}{dy}$

$\frac{dz}{dy} = \frac{2x^3}{y} + 6x^2 \ln y \frac{dx}{dy}$

$\int_0^2 x(2x^2+1)^{1/2} dx$

let $u = 2x^2+1$

$\frac{du}{dx} = 4x$

$du = 4x dx$

$dx = \frac{du}{4x}$

$\int_0^2 u^{1/2} \cdot \frac{du}{4} = \frac{du^{3/2}}{4 \cdot 3/2}$

$\frac{1}{4} \int_0^2 u^{1/2} du$

$\frac{1}{4} \left[\frac{u^{3/2}}{3/2} \right]_0^2$

$= \frac{1}{6} (2(2)^2 + 1)^{3/2} - 2(0)^2 + 1)^{3/2}$

$= \frac{1}{6} [2^3 - 1]$

$= \frac{1}{6} [2^3]$

$= 4.533 = 4.53$