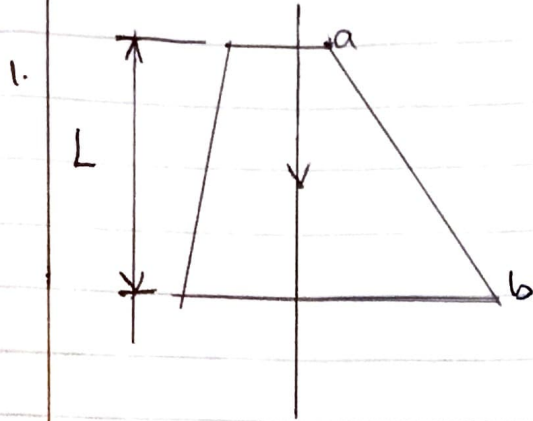


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Computer Engineering

18/ENG021006

ENG 214 Fluid mechanics Assignment 4



length, $L = 2.0\text{m}$

The velocity flow at smaller end $= V_1 = 5\text{m/s}$

Velocity flow at lower end $= V_2 = 2\text{m/s}$

Let the pressure head at the smaller end $= P_1 = 2.5\text{m of liquid}$

Let the loss of head $= H_L = \frac{0.35(V_1 - V_2)^2}{2g}$

$$= \frac{0.35(5-2)^2}{2 \times 9.81} = 0.161\text{m}$$

Let the pressure head at the lower end $= P_2 = ?$

from Bernoulli's equation

$$\frac{P_1}{\rho g} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{\rho g} + \frac{V_2^2}{2g} + z_2 + H_L$$

$$\text{where } P_1 = \frac{P_1}{\rho g} \text{ and } P_2 = \frac{P_2}{\rho g}$$

$$z_1 = 2.0 \text{ and } z_2 = 0$$

$$2.5 + \frac{5^2}{2 \times 9.81} + 2.0 = P_2 + \frac{2^2}{2 \times 9.81} + 0 + 0.161$$

$$2.5 + \frac{25}{19.62} + 2 = P_2 + \frac{4}{19.62} + 0.161$$

$$2.5 + \frac{25}{19.62} + 2 - \left(\frac{4}{19.62} + 0.161 \right) = P_2$$

$$5.774 - 0.365 = P_L$$

$$P_L = 5.409 \text{ m of fluid.}$$

2. Let inlet diameter = $D_1 = 20 \text{ cm}$

Let throat diameter = $D_2 = 10 \text{ cm}$

$$\text{Let inlet area} = A_1 = \frac{\pi D_1^2}{4} = \frac{\pi (20)^2}{4} = 314.16 \text{ cm}^2$$

$$\text{Let throat area} = A_2 = \frac{\pi D_2^2}{4} = \frac{\pi (10)^2}{4} = 78.54 \text{ cm}^2$$

$$\text{Density of water} = \rho = 1000 \text{ kg/m}^3$$

$$\text{Pressure of inlet} = 17.658 \text{ N/cm}^2 = 17.658 \times 10^4 \text{ N/m}^2$$

$$\therefore \frac{P_1}{\rho g} = \frac{17.658 \times 10^4}{1000 \times 9.81} = 18 \text{ m}$$

$$\frac{P_2}{\rho g} = 30 \text{ cm of mercury, } \rho_{\text{Hg}} = 13.6$$

$$\frac{P_2}{\rho g} = -30 \times 10^{-2} \text{ m of mercury} \times 13.6$$
$$= -4.08 \text{ m}$$

$$\text{Let differential head} = \frac{P_1}{\rho g} - \frac{P_2}{\rho g}$$

$$= 18 - (-4.08)$$

$$= 18 + 4.08 = 22.08 \text{ m} \times 100$$

$$H = 2208 \text{ cm.}$$

$$\text{Using, } Q = \frac{C_d \sqrt{2gh} \cdot A_1 A_2}{\sqrt{A_1^2 - A_2^2}}$$

$$= 0.98 \times \frac{\sqrt{2 \times 9.81 \times 2208} \times 314.16 \times 78.54}{\sqrt{(314.16)^2 - (78.54)^2}}$$

$$= 0.98 \times 2081.37 \times 24674.1264$$

$$304.184112$$

$$= 165455.3 \text{ cm}^3/\text{s}$$

$$= \frac{165455.3}{1000} = 165.455 \text{ lit/sec}$$

3. Diameter of pipe = 30 cm

$$A_1 = \frac{\pi d_1^2}{4} = \frac{\pi (30)^2}{4} = 706.86 \text{ cm}^2$$

Diameter of orifice, $d_2 = 15 \text{ cm}$

$$A_2 = \frac{\pi d_2^2}{4} = \frac{\pi (15)^2}{4} = 176.72 \text{ cm}^2$$

Specific gravity of oil, $S_o = 0.9$

Specific gravity of mercury, $S_{hg} = 13.6$

Differential manometer reading, $x = 50 \text{ cm}$ of mercury

Coefficient of discharge, $C_d = 0.64$

Differential head, $h = x \left(\frac{S_{hg}}{S_o} - 1 \right)$

$$h = 50 \left(\frac{13.6}{0.9} - 1 \right)$$

$h = 705.56 \text{ cm}$ of oil

∴ The rate of flow of oil is

$$Q = \frac{C_d \sqrt{2gh} \cdot A_1 A_2}{\sqrt{A_1^2 - A_2^2}}$$

$$Q = \frac{0.64 \times \sqrt{2 \times 9.81 \times 705.56} \times 706.86 \times 176.72}{\sqrt{(706.86)^2 - (176.72)^2}}$$

$$Q = 137443.29 \text{ cm}^3/\text{s}$$

$$Q = 137443.29 \text{ cm}^3/\text{s}$$

$$Q = \frac{137443.29}{1000} = 137.44 \text{ lit/s}$$

4) The difference of mercury load, $x = 17 \text{ cm} = 17 \times 10^{-3} = 0.17 \text{ m}$

The specific gravity of Mercury, $S_g = 13.6$

The specific gravity of sea water, $S_o = 1.026$

The speed, $V = ?$

$$V = \sqrt{2gh}$$

$$h = x \left[\frac{S_g}{S_o} - 1 \right] = 0.17 \left[\frac{13.6}{1.026} - 1 \right] = 2.0834 \text{ m}$$

$$V = \sqrt{2 \times 9.81 \times 2.0834} = 6.393 \text{ m/s.}$$

$$\text{In km/hr } V = \frac{6.393 \times 60^2}{1000} = 23.01 \text{ km/hr.}$$

$$5. Q = 0.05 \text{ m}^3/\text{min} = 50 \text{ cm}^3/\text{min}$$

$$P_0 = 15 \text{ bar} = 15 \times 100000 = 15 \times 10^5 \text{ N/m}^2$$

$$\text{Speed} = 1700 \text{ rev/min}$$

$$T = 15 \text{ Nm, } N_D = 10 \text{ cm}^3/\text{rev}$$

$$\text{i) Volumetric efficiency} = \frac{\text{Actual flow rate}}{\text{Ideal flow rate}}$$

$$\text{Ideal flow rate} = \text{Nominal flow rate} \times \text{speed}$$

$$= 10 \text{ cm}^3/\text{rev} \times 1700 \text{ rev/min}$$

$$= 17000 \text{ cm}^3/\text{min}$$

$$\text{Ideal flow rate} = \frac{17000}{1000000} = 0.017 \text{ m}^3/\text{min}$$

$$\text{Actual flow rate} = 0.05 \text{ m}^3/\text{min}$$

$$\text{Volumetric efficiency} = \frac{0.05}{0.017} = 2.94\% = 294\%$$

$$\text{ii) Fluid power} = P \times Q$$

$$P = 15 \times 10^5 \text{ N/m}^2$$

$$Q = 0.05 \text{ m}^3/\text{min} = \frac{0.05}{60} = 8.33 \times 10^{-4} \text{ m}^3/\text{s}$$

$$\text{Fluid Power} = 15 \times 10^5 \times 8.33 \times 10^{-4}$$

$$= 15 \times 10^5 \times 83.3 \times 10^{-5}$$

$$= 1249.5 \times 10^{5-5}$$

$$\text{Fluid Power} = 1249.5 \text{ watts}$$

$$\text{iii) Shaft power} = \frac{2\pi N T}{60} = \frac{2\pi \times 1700 \times 15}{60}$$

$$\text{Shaft Power} = 2670.35 \text{ watt s}$$

$$\text{Overall efficiency} = \frac{\text{fluid Power}}{\text{shaft Power}}$$

$$\frac{\text{fluid Power}}{\text{shaft Power}} = \frac{1249.5}{2670.35} = 0.468$$

$$\text{shaft Power} = 2670.35$$

$$\text{Overall efficiency} = 0.468 \times 100 = 46.8\%$$