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Aeronautical & Astronautical Eng.

### Answers

- 1] Speed of rotation = 1500 rev/min  
nominal displacement = 10 cm<sup>3</sup>/rev  
Torque input = 12.5 Nm  
rate = 10 dm<sup>3</sup>/min

#### Solution

$$\text{Ideal flow rate} = \text{nominal disp} \times \text{speed}$$
$$\Rightarrow 10 \times 1500 = 15000 \text{ cm}^3/\text{min}$$

$$\text{Volumetric efficiency} = \frac{\text{Actual flow}}{\text{Ideal flow}}$$
$$= \frac{10}{15} = 0.67 \approx 67\%$$

$$Q = (10 \times 10^{-3}) \div 60 \text{ m}^3/\text{s} = 16.7 \times 10^{-6} \text{ m}^3/\text{s}$$
$$\Delta p = 12 \times 10^5 \text{ N/m}^2$$

ii) Fluid power =  $Q \Delta p$

$$= 16.7 \times 10^{-6} \times 12 \times 10^5 = 20.04 \text{ watts}$$

iii) Shaft Power =  $\frac{2\pi NT}{60}$

$$= \frac{2\pi \times 1500 \times 12.5}{60} = 1963.5 \text{ Nm}$$

iv) Overall Efficiency =  $\frac{\text{Fluid Power}}{\text{Shaft Power}}$

$$= \frac{20.04}{1963.5}$$

- 2] delivers 35 dm<sup>3</sup>/min  
pressure change = 100 bar  
efficiency = 88%  
shaft power =  $2\pi NT/60$

$$\text{Fluid power} = Q \Delta P$$
$$Q = (35 \times 10^{-3})/60 = 5.8 \times 10^{-4}$$
$$\Delta P = 100 \times 10^5 \text{ N/m}^2$$

$$\text{Fluid Power} = 5800 \text{ watts}$$
$$\text{Efficiency} = \frac{\text{Fluid power}}{\text{Shaft power}}$$

$$0.88 = \frac{5800}{SP}$$

$$\therefore SP = \frac{5800}{0.88} = 6590 \text{ Nm}$$

- 3) Nominal displacement = 50 cm<sup>3</sup>/rev  
pressure = 100 bar  
shaft power = 15 kW  
Actual flow rate = 35 dm<sup>3</sup>/min  
Speed = 850 rpm

#### Solution

$$\text{Ideal flow rate} = 50 \times 850 =$$

$$\text{Volumetric efficiency} = \frac{35}{42.5} = 0.82$$

$$\text{Fluid power} = (35 \times 10^{-3})/60 \times 100 \times 10^5$$
$$= 5.8 \times 10^{-10} \text{ watts}$$

$$\text{Overall efficiency} = \frac{5.8 \times 10^{-10}}{15 \times 10^{-3}}$$
$$= 3.9 \times 10^{-7}$$

4

$$\rho = 1000 \text{ kg/m}^3$$

$$Z = 240 \text{ m}$$

$$Q = 13 \text{ l/s} = 13 \times 10^{-3} \text{ m}^3/\text{sec}$$

Velocity of jet = 0.6 m/s

Since output of pipe is at datum  $P=0$   $z=0$

$$P = \rho Q + \frac{\rho Q v^2}{2} + \rho g Q z$$

$$P = 1000 + 13 \times 10^{-3} \times (0.6)^2$$

$$= 28314 \text{ watts}$$

ii) Power supplied through reservoir  
substituting  $P=0$  and  $v=0$

In eq 1

$$P = \rho g Q z = 1000 \times 9.81 \times 3 \times 10^{-3}$$

$$= 30607.2 \text{ watts}$$

iii) Head loss  $h = \frac{\text{Power lost in trans}}{\rho g Q}$

$$= \frac{(30607.2 - 28314)}{1000 \times 9.81 \times 1.3 \times 10^{-3}}$$

$$h = 17.982 \text{ m}$$

iv) Efficiency =  $\frac{\text{Power of jet} \times 100}{\text{Power of reservoir}}$

5)  $S_g = 0.89$

$$\rho = 890$$

$$z = 300$$

$$Q = 0.22 \text{ m}^3/\text{sec}$$

Velocity = 7 m/s

$$P = \rho Q + \frac{\rho Q v^2}{2} + \rho g Q z$$

i) Power of jet =  $\frac{\rho Q v^2}{2} = \frac{890 \times 0.22 \times 7^2}{2}$

$$= 4797.1 \text{ watt}$$

ii) Power supplied from reservoir

$$P = \rho g Q z$$

$$= 890 \times 9.81 \times 0.22 \times 300$$

$$= 576239.4 \text{ watts}$$

iii) Head loss  $h = \frac{\text{Power loss in transmission}}{\rho g Q}$

$$= \frac{576239.4 - 4797.1}{0.22 \times 390 \times 9.81}$$

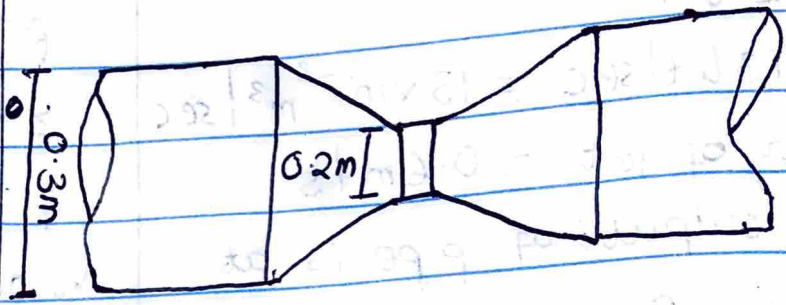
$$= 29.75 \text{ m}$$

$$= \frac{576239.4 - 4797.1}{0.22 \times 390 \times 9.81}$$

$$= 29.75 \text{ m}$$



7)



Diameter of inlet = 0.3 m

$$\text{Area of inlet} = \frac{\pi \times 0.3^2}{4} = 0.071 \text{ m}^2$$

Diameter of throat = 0.2 m

$$\text{Area of throat} = \frac{\pi \times 0.2^2}{4} = 0.031 \text{ m}^2$$

Pressure difference on U-tube (y) = 0.06 m

Specific weight of gas = 19.62 N/m<sup>3</sup>

$$= 0.01962 \text{ kN/m}^3$$

Specific gravity of gas =  $\frac{0.01962}{9.81} = 2 \times 10^{-3}$

$$\text{Differential reading (h)} = y \left[ \frac{sgW}{sgG} - 1 \right]$$

$$= 0.06 \left[ \frac{1}{2 \times 10^{-3}} - 1 \right]$$

$$= 29.94$$

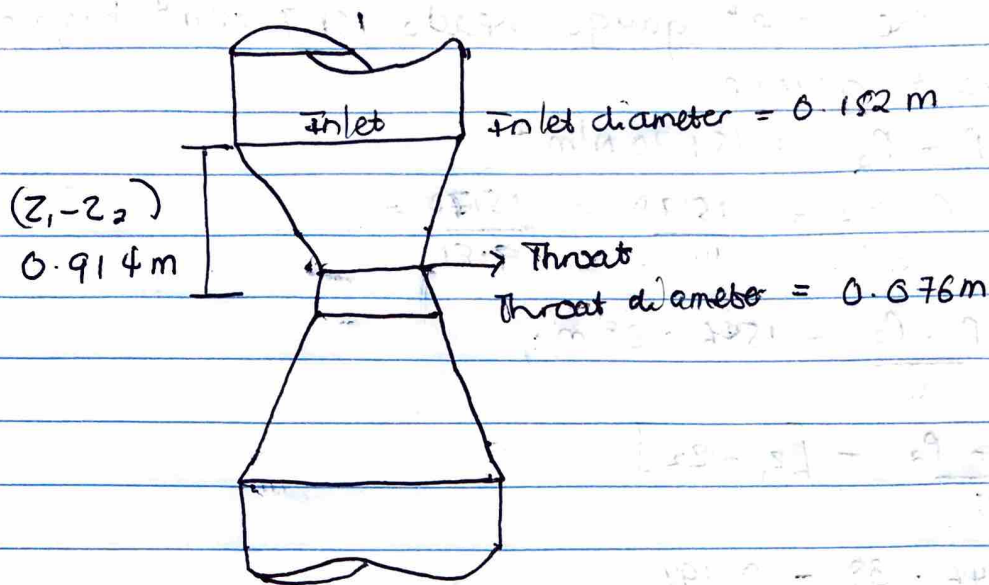
$$Q = C_d \times \frac{A_1 A_2}{\sqrt{A_1^2 - A_2^2}} \times \sqrt{2gh}$$

$$= 0.98 \times 0.071 \times 0.031 \times \sqrt{2 \times 9.81 \times 29.94}$$

$$\sqrt{0.071^2 - 0.031^2}$$

$$= 0.803 \text{ m}^3/\text{s}$$

# NUMBERS



Diameter of inlet = 0.152 m

$$\text{Area of inlet} = \frac{\pi \times 0.152^2}{4} = 0.018 \text{ m}^2$$

Diameter of throat = 0.076 m

$$\text{Area of throat} = \frac{\pi \times 0.076^2}{4} = 4.54 \times 10^{-3} \text{ m}^2$$

$$\begin{aligned} \text{The differential reading (h)} &= \left[ \frac{P_1}{\rho} + z_1 \right] - \left[ \frac{P_2}{\rho} + z_2 \right] \\ &= \left[ \frac{P_1}{\rho} - \frac{P_2}{\rho} \right] - [z_1 - z_2] \end{aligned}$$

a) When the pressure gauge reading is the same.

$$\text{i.e. } \left[ \frac{P_1}{\rho} = \frac{P_2}{\rho} \right]$$

$$h = [z_1 - z_2] = 0.194 \text{ m}$$

$$\therefore \dot{Q} = C_d \times \frac{A_1 A_2}{\sqrt{A_1^2 - A_2^2}} \times \sqrt{2gh}$$

$$= 0.97 \times 0.018 \times 4.54 \times 10^{-3} \times \sqrt{2 \times 9.81 \times 0.194}$$

$$= 8.88 \times 10^{-3} \text{ m}^3/\text{s}$$



b) when the inlet gauge reads  $15170 \text{ N/m}^2$  higher than the throat gauge

$$\therefore P_1 - P_2 = 15170 \text{ N/m}^2$$

$$\Rightarrow \frac{P_1 - P_2}{\rho} = \frac{15170}{9.81} = \frac{15170}{9.81} =$$

$$\Rightarrow \frac{P_1 - P_2}{\rho} = 1546.38 \text{ m}$$

$$h = \frac{P_1 - P_2}{\rho} - [z_1 - z_2]$$

$$h = 1546.38 - 0.194$$

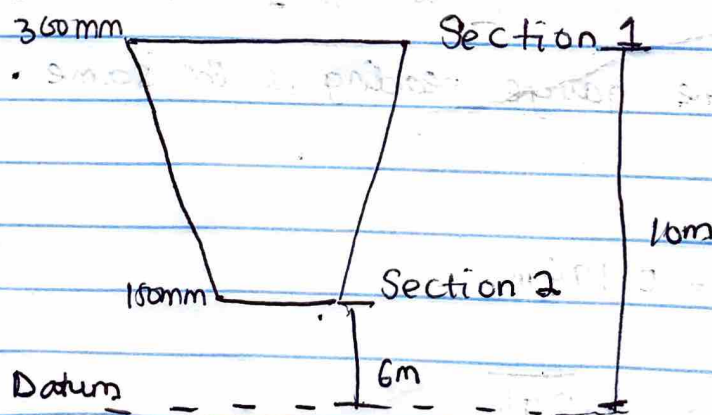
$$= 1546.2 \text{ m}$$

$$\therefore Q = C_d \times \frac{A_1 A_2}{\sqrt{A_1^2 - A_2^2}} \times \sqrt{2gh}$$

$$Q = 0.97 \times \frac{0.018 \times 4.54 \times 10^{-3}}{\sqrt{0.018^2 - (4.54 \times 10^{-3})^2}} \times \sqrt{2 \times 9.81 \times 1546.2}$$

$$= 0.793 \text{ m}^3/\text{s}$$

9)



Section 1

Diameter ( $d_1$ ) = 300mm

Pressure ( $P_1$ ) =  $40 \text{ kN/m}^2$

$z_1 = 10 \text{ m}$

Section 2

Diameter ( $d_2$ ) = 150mm

Pressure ( $P_2$ ) = ?

$z_2 = 6 \text{ m}$

$$\text{Volumetric rate } (\phi) = 4 \text{ lit/sec} \\ = 0.04 \text{ m}^3/\text{s}$$

$$\text{Recall } \phi = A_1 V_1 = A_2 V_2$$

$$\text{But } A_1 = \frac{\pi d_1^2}{4} = \frac{\pi \times 0.3^2}{4} =$$

$$A_1 = 0.236 \text{ m}^2$$

$$\therefore 0.04 = 0.236 \times V_1$$

$$V_1 = 0.169 \text{ m/s}$$

$$\text{But } A_2 = \frac{\pi d_2^2}{4} = \frac{\pi \times 0.15^2}{4}$$

$$= 0.118 \text{ m}^2$$

$$V_2 = \frac{0.04}{0.118} = 0.339 \text{ m/s}$$

From Bernoulli's equation

$$\frac{P_1}{\rho} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{\rho} + \frac{V_2^2}{2g} + z_2$$

$$\frac{400}{9.81} + \frac{0.169^2}{2 \times 9.81} + 10 = \frac{P_2}{9.81} + \frac{0.339^2}{2 \times 9.81} + 6$$

$$40.77 + 1.456 \times 10^{-3} + 10 + \frac{P_2}{9.81} + 5.857 \times 10^{-3} + 6$$

$$50.771 = \frac{P_2}{9.81} + 6.006$$

$$44.765 = \frac{P_2}{9.81} + 6.006$$

$$38.759 = \frac{P_2}{9.81}$$

$$P_2 = 38.759 \times 9.81 = 380.045 \text{ kN/m}^2$$

10) Reading of differential manometer (y) = 0.17m

Specific gravity of mercury = 13.6

Specific gravity of sea water = 1.025

$$\text{to find head } (h) = 0.17 \left[ \frac{13.6}{1.025} - 1 \right] = 2.09$$

$$\therefore \text{Velocity of Submarine} = \sqrt{2gh} =$$

$$\Rightarrow \sqrt{2 \times 9.81 \times 2.09} = 6.403 \text{ m/s}$$