

MATHS - FLUID MECHANICS  
 (8) HEAD LOSS  
 EXERCISE / EXERCISES  
 EXERCISE 214 ASSIGNMENT.

1. Let smaller end be (1) and larger end (2).

$L = 2.0m$

$v_1 = 5m/s$

$\rho_1/\rho_2 = 2.5m$  of liquid,

$v_2 = 2m/s$

$P_0/P_2 = ?$

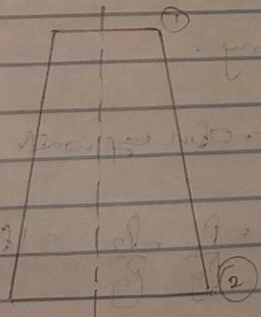
loss of head (h<sub>L</sub>) =  $0.35 \frac{v_1 - v_2}{2g}$

$= \frac{0.35 (5 - 2)}{2 \times 9.81}$

$= 0.16m$

Using Bernoulli's equation.

$\frac{P_1}{\rho g} + \frac{v_1^2}{2g} + z_1 = \frac{P_2}{\rho g} + \frac{v_2^2}{2g} + z_2 + h_L$



Letting the line pass through the region, then  $z_1 = 2, z_2 = 0$

$\therefore \frac{2.5}{2 \times 9.81} + \frac{5^2}{2 \times 9.81} + 2.0 = \frac{P_2}{2 \times 9.81} + \frac{2^2}{2 \times 9.81} + 0 + 0.16$

$2.5 + 1.27 + 2.0 = \frac{P_2}{2 \times 9.81} + 0.204 + 0.16$

$\therefore 5.77 = \frac{P_2}{2 \times 9.81} + 0.364$

$\therefore \frac{P_2}{\rho g} = 5.77 - 0.364 = 5.406m$  of liquid.

$$2. \text{ diameter} = \frac{20 \text{ cm}}{100} = 0.2 \text{ m}$$

$$\text{Area} = \frac{\pi \times (0.2)^2}{4} = 0.0314 \text{ m}^2$$

$$\text{diameter} = \frac{10 \text{ cm}}{100} = 0.1 \text{ m}$$

$$\text{Area} = \frac{\pi \times (0.1)^2}{4} = 7.85 \times 10^{-3} \text{ m}^2$$

$$\rho \text{ for water} = 1000 \text{ kg/m}^3$$

$$P_1 = 17.658 \text{ N/cm}^2 = 17.658 \times 10^4 \text{ N/m}^2$$

$$\therefore \frac{P_1}{\rho g} = \frac{17.658 \times 10^4}{1000 \times 9.81}$$

$= 1.8 \text{ m of water}$

$$\frac{P_2}{\rho g} = \frac{-80 \text{ cm of mercury}}{13.6}$$

$= -0.3 \text{ m of mercury}$

$$= -0.3 \times 13.6 = -4.08 \text{ m of water}$$

$$\therefore \text{Difference of head (A)} = \frac{P_1}{\rho g} - \frac{P_2}{\rho g} = 1.8 + 4.08$$

$$= 22.08 \text{ m of water}$$

$$\text{Using Bernoulli's equation}$$

$$\frac{0.76 \times 0.0314 \times 4.87 \times 10^{-3}}{4 \times 0.0314 \times (7.85 \times 10^{-3})^2} \times \sqrt{2 \times 9.81 \times 22.08}$$

$$= 0.76 \times 8.107 \times 10^{-3} \times 20.81$$

$$= 0.1653 \text{ m}^3/\text{s} = 165.3 \text{ lit/s}$$

$$A_{\text{outlet}} = \frac{\pi}{4} \times (15)^2 = 176.714 \text{ cm}^2 \quad (A_0 \text{ area of outlet})$$

$$A_{\text{pipe}} = \frac{\pi}{4} \times (80)^2 = 5026.548 \text{ cm}^2 \quad (A_p \text{ area of pipe})$$

$$\text{diff. in area of head } (A) = \left[ \frac{13.6 \times 1}{0.9} \right] \times 70 \text{ cm of oil}$$

$$= 1017.556 \text{ cm of oil}$$

$$Q = C_d \times A_0 A_p \times \sqrt{2gh}$$

$$\sqrt{A_p^2 - A_0^2}$$

$$= 0.64 \times 17.714 \times 5026.548 \times \sqrt{2 \times 9.81 \times 101.756}$$

$$\sqrt{5026.548^2 - 176.714^2}$$

$$= 0.64 \times 17.714 \times 5026.548 \times 147.656$$

$$= 13742.76 \text{ cm}^3/\text{sec}$$

$$= 13.74276 \text{ lit}/\text{sec}$$

$\Delta$  Difference of mercury level  $\rho_c = 13600 \text{ kg/m}^3 = 0.17 \text{ m}^3$   
 $\rho$  Sp. gr. of mercury  $\rho_g = 13.6$   
 $\rho_w$  Sp. gr. of water  $\rho_w = 1.026$

$$\therefore h = \frac{\rho_c}{\rho_w} \left[ \frac{\rho_g}{\rho_w} - 1 \right] = 0.17 \left[ \frac{13.6}{1.026} - 1 \right] = 2.0834 \text{ m}$$

$$\text{Lang } v = \sqrt{2gh}$$

$$v = \sqrt{2 \times 9.81 \times 2.0834}$$

$$= 6.378 \text{ m/s}$$

convert to  $\text{km/hr}$

$$6.378 \times 60 \times 60$$

$$= 22 \text{ km/hr}$$

∴ Volumetric flow rate

changing from  $\text{dm}^3/\text{min}$  to  $\text{m}^3/\text{min}$

$$10 \text{ dm} = 1 \text{ m}$$

$$\therefore 10^3 \text{ dm}^3 = 1 \text{ m}^3$$

$$1000 \text{ dm}^3 = 1 \text{ m}^3$$

$$5 \text{ dm}^3 = ?$$

$$? = \frac{5}{1000} = 0.005$$

∴ Volumetric flow rate =  $0.005 \text{ m}^3/\text{min}$

$$\text{Actual flow rate} = \frac{0.005}{60} = 8.33 \times 10^{-5} \text{ m}^3/\text{sec}$$

Speed = 1700 rpm

changing to rps

$$\frac{1700}{60} = 28.33 \text{ rev/sec}$$

$$\Delta P = 18 \text{ bar} \approx 18 \times 10^5 \text{ N/m}^2$$

Normal displacement =  $10 \text{ cm}^3/\text{rev}$

Note that  $10^3 \text{ cm}^3 = 1 \text{ m}^3$

$$10 \text{ cm}^3 = x$$

$$x = \frac{10}{1000} = 1 \times 10^{-2} \text{ m}^3/\text{rev}$$

∴ Ideal flow rate = Normal displacement  $\times$  Speed

$$= 8.33 \times 1 \times 10^{-2}$$

$$= 8.33 \times 10^{-2}$$

Q415

Volume Efficiency =  $\frac{\text{Actual flow rate}}{\text{Ideal flow rate}} \times 100\%$   
 $= \frac{6.83 \times 10^{-5}}{2.83 \times 10^{-4}} \times 100\%$   
 $= 24.1\%$

Flow power =  $Q \cdot \Delta P$   
 $= 6.83 \times 10^{-5} \times 1.8 \times 10^6$   
 $= 124.74 \text{ Nm/sec}$

Shaft power =  $T \cdot \omega$   
 $T = 1.8 \text{ Nm}$   
 $\omega = 2 \times \frac{2\pi}{7} \times 28.33 = 198.07 \text{ rad/sec}$   
 $\text{Shaft power} = 1.8 \times 198.07 = 356.53 \text{ Watts}$

Overall efficiency =  $\frac{\text{Flow power}}{\text{Shaft power}} \times 100\%$   
 $= \frac{124.74}{356.53} \times 100\%$   
 $= 34.99\%$

Handwritten notes at the bottom of the page, including some faint calculations and possibly a reference to a textbook or manual.