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Mechanical Engineering

① Length  $L = 2.0\text{m}$

The velocity flow at smaller end =  $V_1 = 5\text{m/s}$

The velocity flow at larger end =  $V_2 = 2\text{m/s}$

pressure head at the smaller end =  $P_1 = 2.5\text{m}$  of liquid.

$$\begin{aligned} \text{loss of head} = h_L &= \frac{0.35 (V_1 - V_2)^2}{2g} \\ &= \frac{0.35 (5-2)^2}{2 \times 9.81} = 0.161\text{m} \end{aligned}$$

pressure head at lower head =  $P_L = ?$

$$\frac{P_1}{\rho g} + \frac{V_1^2}{2g} + Z_1 = \frac{P_2}{\rho g} + \frac{V_2^2}{2g} + Z_2 + h$$

where  $P_1 = \frac{P_1}{\rho g}$  and  $P_2 = \frac{P_2}{\rho g}$

$Z_1 = 2.0$  and  $Z_2 = 0$ .

putting values into the equation.

$$2.5 + \frac{5^2}{2 \times 9.81} + 2.0 = P_L + \frac{2^2}{2 \times 9.81} + 0 + 0.161$$

$$2.5 + \frac{25}{19.62} + 2 = P_L + \frac{4}{19.62} + 0.161$$

$$2.5 + \frac{25}{19.62} + 2 - \left( \frac{4}{19.62} + 0.161 \right) = P_L$$

$$5.774 - 0.365 = P_L$$

$$R = 5.409 \text{ m of fluid.}$$

2) let inlet diameter =  $D_1 = 20 \text{ cm}$

" throat " =  $D_2 = 10 \text{ cm}$

" inlet area =  $A_1 = \pi D_1^2 = \pi (20)^2 = 314.16 \text{ cm}^2$

throat area =  $A_2 = \frac{\pi D_2^2}{4} = \frac{\pi (10)^2}{4} = 78.54 \text{ cm}^2$

Density of water,  $\rho = 1000 \text{ kg/m}^3$

pressure at inlet =  $17.658 \times 10^4 \text{ N/m}^2$

$$\frac{P_1}{\rho g} = \frac{17.658 \times 10^4}{1000 \times 9.81} = 18 \text{ m}$$

$$\frac{P_2}{\rho g} = -30 \text{ cm of mercury, } 5.94 \text{ g/cc} = 13.6$$

$$\frac{P_2}{\rho g} = \frac{-30 \times 10^{-2} \text{ m of mercury} \times 13.6}{1} = -4.08 \text{ m}$$

Differential Head =  $H = \frac{P_1}{\rho g} - \frac{P_2}{\rho g}$   
 $= 18 - (-4.08)$

differential head =  $H = \frac{P_1}{\rho g} - \frac{P_2}{\rho g} = 18 + 4.08 = 22.08 \text{ m} \times 100$   
 $= 2208 \text{ cm}$

Using  $Q = C_d \frac{\sqrt{2gh} \cdot A_1 A_2}{\sqrt{A_1^2 - A_2^2}}$

$$= 0.98 \times \frac{\sqrt{2 \times 9.81 \times 2208} \times 314.16 \times 78.54}{\sqrt{(314.16)^2 - (78.54)^2}}$$

$$= 165.455 \text{ ltr/sec}$$

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$$d_1 = 30 \text{ cm}$$

$$A_1 = \frac{\pi d_1^2}{4} = \frac{\pi (30)^2}{4} = 176.72 \text{ cm}^2$$

$$d_2 = 15 \text{ cm}$$

$$A_2 = \frac{\pi d_2^2}{4} = \frac{\pi (15)^2}{4} = 176.72 \text{ cm}^2$$

Specific gravity of oil = 0.9

" of mercury = 13.6

Diff manometer reading,  $x = 50 \text{ cm}$  of mercury

Coefficient of discharge,  $C_d = 0.64$

Differential head,  $h = x \left( \frac{S_g}{S_o} - 1 \right)$

$$h = 50 \left( \frac{13.6}{0.9} - 1 \right)$$

$$h = 705.56 \text{ cm of oil}$$

$\therefore$  The rate of flow of oil is

$$Q = \frac{C_d \sqrt{2gh} \cdot A_1 \cdot A_2}{\sqrt{A_1^2 - A_2^2}}$$

$$Q = 0.64 \times \sqrt{2 \times 9.81 \times 705.56} \times 706.86 \times 176.72$$

$$\sqrt{(706.86)^2 - (176.72)^2}$$

$$Q = \frac{137443.29}{1000} = 137.44 \text{ lit/hr.}$$

4) difference of mercury = 170 mm = 170 mm =  $170 \times 10^{-3} = 0.17 \text{ m}$

Specific gravity of mercury,  $S_g = 13.6$

Specific gravity of sea water,  $S_o = 1.026$

Speed,  $V = ?$

$$V = \sqrt{2gh}$$

$$h = x \left[ \frac{S_g}{S_o} - 1 \right] = 0.17 \left[ \frac{13.6}{1.026} - 1 \right] = 2.0834 \text{ m}$$

$$V = \sqrt{2 \times 9.81 \times 2.0834} = 6.393 \text{ m/s}$$

In km/hr

$$V = \frac{6.393 \times 60^2}{1000} = 23.01 \text{ km/hr.}$$

$$\begin{aligned}
 a &= (20 - 0.05s^2) (-0.13) \\
 &= -2s + 5 \times 10^{-3} s^3 \\
 &= -2(15) + 5 \times 10^{-3} (15)^3 \\
 &= -13.13 \text{ m/s}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{b) } Q &= 0.05 \text{ m}^3/\text{min} = 50 \text{ dm}^3/\text{min} \\
 P &= 15 \text{ bar} = 15 \times 10000 = 15 \times 10^5 \text{ N/m}^2 \\
 \text{Speed} &= 1700 \text{ rev/min} \\
 T &= 15 \text{ Nm}, \quad ND = 10 \text{ cm}^3/\text{rev}
 \end{aligned}$$

$$\text{v) volumetric efficiency} = \frac{\text{Actual flow rate}}{\text{Ideal flow rate}}$$

$$\begin{aligned}
 \text{Ideal flow rate} &= \text{Nominal flow rate} \times \text{Speed} \\
 &= 10 \text{ cm}^3/\text{rev} \times 1700 \text{ rev/min} \\
 &= 17000 \text{ cm}^3/\text{min}
 \end{aligned}$$

$$\text{Ideal flow rate} = \frac{17000}{1000000} = 0.017 \text{ m}^3/\text{min}$$

$$\text{Actual flow rate} = 0.05 \text{ m}^3/\text{min}$$

$$\therefore \text{volumetric efficiency} = \frac{0.05}{0.017} = 2.94\% = 294\%$$

$$\text{ii) fluid power} = P \times Q$$

$$P = 15 \times 10^5 \text{ N/m}^2$$

$$Q = 0.05 \text{ m}^3/\text{min} = \frac{0.05}{60} = 8.33 \times 10^{-4}$$

$$\text{fluid power} = 15 \times 10^5 \times 8.33 \times 10^{-4}$$

$$\text{fluid power} = 1249.5 \text{ watts}$$

$$\text{iii) shaft power}$$

$$= \frac{2\pi NT}{60} = \frac{2\pi \times 1700 \times 15}{60}$$

$$= 2670.35 \text{ watts}$$

$$\text{iv) overall efficiency} = \frac{\text{fluid power}}{\text{shaft power}}$$

$$= \frac{1249.5}{2670.35} = 0.468$$

$$2670.35$$

$$\text{Overall Efficiency} = 0.468 \times 100 = 46.8\%$$