

18/ENG041008

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Course code: ENGI 21+

Course TITLE: Fluid mechanics

Assignment

▷ $Z_1 = 0$

$Z_2 = 2.0\text{m}$

$V_1 = 5\text{m/s}$

$V_2 = 2\text{m/s}$

The pressure, $h_1, \frac{P_1}{\rho} = 2.5\text{m}$.

$\frac{P_2}{\rho} = ??$

$$h_f = 0.35 \frac{(V_1 - V_2)^2}{2g}$$

$$= \frac{0.35 (5-2)^2}{2 \times 9.81} = \frac{0.35 \times 9}{2 \times 9.81}$$

$$= 0.1606\text{m}$$

Applying Bernoulli's Equation

$$\frac{P_1}{\rho} + \frac{V_1^2}{2g} + Z_1 = \frac{P_2}{\rho} + \frac{V_2^2}{2g} + Z_2 + h_f$$

$$\frac{P_2}{\rho} = \frac{P_1}{\rho} + \frac{V_1^2}{2g} + Z_1 - \frac{V_2^2}{2g} - Z_2 - h_f$$

$$= 2.5 + \frac{5^2}{2 \times 9.81} + 0 - \frac{2^2}{2 \times 9.81} - 2.0 - 0.1606$$

$$= 2.5 + 1.274 - 0.204 - 0.1606 - 2.0$$

$$= 1.4094\text{m}$$

$\therefore h_2, \frac{P_2}{\rho} = 1.41\text{m}$

$= 1.41\text{m}$

NO. 2

$$d_1 = 20 \text{ cm} \\ = \frac{20}{100} = 0.2 \text{ m}$$

$$d_2 = 10 \text{ cm} \\ = \frac{10}{100} = 0.1 \text{ m}$$

$$A_1 = \frac{\pi d^2}{4} = \frac{\pi (0.2)^2}{4} \\ = 0.0314 \text{ m}^2$$

$$A_2 = \frac{\pi d^2}{4} = \frac{\pi (0.1)^2}{4} \\ = 0.00785 \text{ m}^2$$

$$P_1 = 17.658 \text{ N/cm}^2 \\ = 17.658 \times 10^4 \\ = 176580 \text{ N/m}^2$$

$$P_2 = 30 \text{ cm of mercury} \\ = 0.3 \text{ m of Hg.} \\ = 0.3 \text{ m Hg} \times 13.6 \\ h_2 = -4.08 \text{ m}$$

$$R_2 h_1 = \frac{P_1}{\rho} = \frac{176580}{1000 \times 9.81} \\ = 18 \text{ m}$$

$$\therefore h = h_1 - h_2 \\ h = 18 - (-4.08) \\ = 18 + 4.08 \\ = 22.08$$

$$\therefore Q = C_d \frac{A_1 A_2 \sqrt{2gh}}{\sqrt{A_1^2 - A_2^2}} \\ = 0.98 \times 0.0314 \times 0.00785 \times \sqrt{2 \times 9.81 \times 22.08} \\ \sqrt{(0.0314)^2 - (0.00785)^2}$$

$$Q = \frac{0.00503}{0.0304} \\ Q = 0.1654 \text{ m}^3/\text{s}$$

$$Q = 0.1654 \text{ m}^3/\text{s}$$

No. 3

3) Orifice diameter, $d_o = 15 \text{ cm}$

$$= 0.15 \text{ m}$$

Pipe diamet. $d_i = 30 \text{ cm}$

$$= 0.3 \text{ m}$$

$$A_o = \frac{\pi d_o^2}{4} = \frac{\pi (0.15)^2}{4}$$

$$= 0.01767 \text{ m}^2$$

$$A_i = \frac{\pi d_i^2}{4} = \frac{\pi (0.30)^2}{4}$$

$$= 0.070686 \text{ m}^2$$

Differential head:

$$y = 50 \text{ cm}$$

$$= 0.5 \text{ m}$$

$$h = \frac{P}{\rho g} = y \left(\frac{\text{Sp. Gr. of mercury}}{\text{Sp. Gr. of oil}} - 1 \right)$$

$$= 0.5 \left(\frac{13.6}{0.9} - 1 \right)$$

$$= 0.5 (12.4) = 0.5 (14.11)$$

$$= 6.3 = 7.06 \text{ m}$$

$$\therefore h = 7.06 \text{ m}$$

$$\therefore Q = \frac{C_d \times A_i \times A_o \cdot \sqrt{2gh}}{\sqrt{A_i^2 - A_o^2}}$$

$$= \frac{0.64 \times 0.01767 \times 0.07068 \cdot \sqrt{2 \times 9.81 \times 7.06}}{\sqrt{(0.070686)^2 - (0.01767)^2}}$$

$$= \frac{0.009407}{0.06844}$$

$$\textcircled{1} Q = 0.1374 \text{ m}^3/\text{s}$$

$$Q = 0.137 \text{ m}^3/\text{s}$$

$$Q = 0.137 \text{ m}^3/\text{s}$$

No. 4

Difference of Hg (y)

$$y = 170 \text{ mm} \\ = \frac{170}{1000}$$

$$y = 0.17 \text{ m.}$$

S.G. of mercury = 13.6

S.G. of sea water = 1.026

$$\therefore h = y \left(\frac{\text{S.G. of Hg}}{\text{S.G. of sea water}} - 1 \right)$$

$$= y \left(\frac{13.6}{1.026} - 1 \right)$$

$$= 0.17 (12.255)$$

$$= 2.08 \text{ m.}$$

$$\text{velocity} = \sqrt{2gh}$$

$$= \sqrt{2gh}$$

$$= \sqrt{2 \times 9.81 \times 2.08}$$

$$V = 6.39 \text{ m/s.}$$

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$$\begin{aligned}\text{Actual flow rate} &= 0.65 \text{ m}^3/\text{min} \\ &= \frac{0.65}{60} \text{ m}^3/\text{sec} \\ &= 8.33 \times 10^{-4} \text{ m}^3/\text{sec}\end{aligned}$$

$$\begin{aligned}\text{Change in pressure, } \delta p &= 15 \text{ bar} \\ &= 15 \times 10^5 \text{ N/m}^2\end{aligned}$$

$$\begin{aligned}\text{Speed of rotation, } N &= 1700 \text{ rev/min} \\ &= \frac{1700}{60} \\ &= 28.33 \text{ rev/sec}\end{aligned}$$

$$\begin{aligned}\text{Nominal displacement} &= 10 \text{ cm}^3/\text{rev} \\ &= \frac{10}{10^6} \text{ m}^3/\text{rev} \\ &= 1 \times 10^{-5} \text{ m}^3/\text{rev}.\end{aligned}$$

$$\text{Torque input, } T = 15 \text{ Nm}$$

1) Volumetric efficiency

$$= \frac{\text{Actual flowrate} \times 100\%}{\text{Ideal flowrate}}$$

$$\text{Actual flowrate} = 8.33 \times 10^{-4} \text{ m}^3/\text{sec}$$

$$\begin{aligned}\text{Ideal flowrate} &= \text{Speed of rotation} \times \text{Nominal disp} \\ &= 28.33 \times 1 \times 10^{-5} \\ &= 2.833 \times 10^{-4}\end{aligned}$$

$$\begin{aligned}\therefore \text{Volumetric Efficiency} &= \frac{8.33 \times 10^{-4} \times 100\%}{2.833 \times 10^{-4}} \\ &= 2.9403 \times 100\% \\ &= 294.03\%\end{aligned}$$

ii) fluid power, $P_f = Q \times \delta p$

$$\begin{aligned}&= 8.33 \times 10^{-4} \times 15 \times 10^5 \\ &= 1249.5 \text{ Watts}\end{aligned}$$

iii) Shaft Power = $T \cdot \omega$

$$\text{Given } T = 15 \text{ Nm}$$

$$\omega = 2\pi N \text{ rad/s}$$

$$= 2 \times \frac{22}{7} \times 28.33$$

$$= 178.07 \text{ rad/s}$$

$$\therefore \text{Shaft Power} = 15 \times 178.07 \\ = 2671.11 \text{ Watt}$$

iv) Overall efficiency = $\frac{\text{Hurd Power}}{\text{Shaft Power}} \times 100\%$

$$= \frac{1249.5}{2671.11} \times 100\%$$

$$= 0.468 \times 100\%$$

$$= 46.8\%$$

\therefore The overall efficiency is ~~46.8%~~ 46.8%