

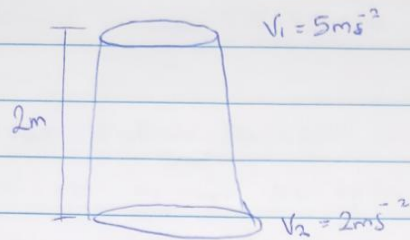
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18/ENG06/023

MECHANICAL ENGINEERING.

FLUID MECHANICS.

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Soln

$$\text{Head loss} = H_L = \frac{0.35(v_1 - v_2)^2}{2g} = \frac{0.35(5-2)^2}{2 \times 9.81} = 0.161 \text{ m}$$

$$H_L = 0.161 \text{ m}$$

Pressure of head at lower end (P_L) = ?

Applying Bernoulli's equation

$$\frac{P_1}{\rho g} + \frac{v_1^2}{2g} + z_1 = \frac{P_2}{\rho g} + \frac{v_2^2}{2g} + z_2 + H$$

$$\text{where } P_S = \frac{P_1}{\rho g} \quad \text{and} \quad P_L = \frac{P_2}{\rho g}$$

$$z_1 = 2.0 \quad \text{and} \quad z_2 = 0$$

Substituting the values of all parameters into the eqn

$$\frac{2.5}{10.62} + \frac{5}{10.62} + 2.0 = \frac{P_L}{10.62} + \frac{2^2}{10.62} + 0 + \cancel{0.26} + 0.161$$

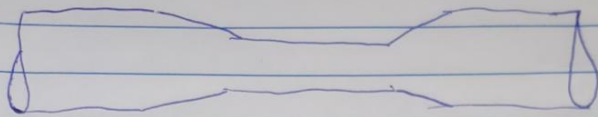
$$\frac{2.5 + 2.5}{10.62} + 2.0 = \frac{P_L}{10.62} + 0.161$$

$$\frac{2.5 + 2.5}{10.62} + 2 - \left(\frac{4}{10.62} + 0.161 \right) = P_L$$

$$5.774 - 0.365 = P_L$$

$$P_L = \underline{\underline{5.409 \text{ m of fluid}}}$$

2



$$\text{Diameter} = 20 \times 10^{-2} \text{ m}$$

$$P_1 = 17.658 \text{ N/cm}^2 = 17.658 \times 10^4 \text{ N/m}^2$$

$$P_2 = 30 \text{ cmHg} = 30 \times 10^{-2} \text{ mHg}$$

$$A_1 = \frac{\pi \times (20 \times 10^{-2})^2}{4} = 0.03 \text{ m}^2$$

$$C_D = 0.98$$

$$A_2 = \frac{\pi \times (10 \times 10^{-2})^2}{4} = 7.85 \times 10^{-3} \text{ m}^2$$

$$\frac{P_2}{\rho} = 0.3 \times 13.6 = 4.08 \text{ mHg}$$

$$\frac{P_2}{\rho} = -4.08$$

$$\frac{P_1}{\rho} = \frac{17.058 \times 10^4}{4.81 \times 10^3} = 18$$

$$h = \frac{P_1}{\rho} - \frac{P_2}{\rho} = 18 - (-4.08) = 22.08$$

$$Q = \frac{C_D A_1 A_2 \sqrt{2gh}}{\sqrt{A_1^2 - A_2^2}}$$

$$Q = \frac{0.98 \times 0.03 \times (7.85 \times 10^{-3}) \times \sqrt{2 \times 9.81 \times 22.08}}{\sqrt{(0.03^2 - (7.85 \times 10^{-3})^2)}}$$

$$Q = 0.166 \text{ m}^3/\text{s}$$

3.

$$D_1 = 30 \times 10^{-2} \text{ m}$$

$$y = 50 \times 10^{-2} \text{ mHg} \quad S_{m1} = 13.6$$

$$C_D = 0.64 \quad S_0 = 0.9$$

$$\sum C_D A = 0.9$$

$$H = y \left[\frac{S_m}{S_0} - 1 \right]$$

$$D = 15 \times 10^{-2} \text{ m}$$

$$A = \frac{\pi D^2}{4} = \frac{\pi \times (15 \times 10^{-2})^2}{4} = 0.0707 \text{ m}^2$$

$$H = 50 \times 10^{-2} \left[\frac{13.6}{0.9} - 1 \right]$$

$$H = 7.055 \text{ m}$$

$$Q = \frac{C_d A_0 A_1 \sqrt{2gh}}{\sqrt{A_1^2 - A_0^2}}$$

$$Q = \frac{0.61 \times 0.0176 \times 0.0707 \sqrt{2 \times 9.81 \times 7.055}}{\sqrt{(0.0707)^2 - (0.0176)^2}}$$

$$Q = \underline{0.137 \text{ m}^3/\text{s}}$$

4. $y = 170 \text{ mmHg} = 170 \times 10^{-3} \text{ mHg}$

S.G of mercury = 13.6 Hg

S.G of Sea water = 1.025

$$v = \sqrt{2gh}$$

$$v = 6.3 \text{ m/s}$$

$$H = y \times \frac{\rho_{h_1} - 1}{\rho_1}$$

$$H = 170 \times 10^{-3} \times \left(\frac{13.6}{1.025} - 1 \right) = 2.08 \text{ m}$$

5. $Q = 0.05 \text{ m}^3/\text{min} = 500 \text{ cm}^3/\text{min}$

$$P = 15 \text{ bar} = 15 \times 100000 = 15 \times 10^5 \text{ N/m}^2$$

Speed = 170 rev/min

$$F = 15 \text{ Nm}, N_0 = 10 \text{ cm}^3/\text{rev}$$

1. Volumetric efficiency = $\frac{\text{Actual flow rate}}{\text{Ideal flow rate}}$

$$\text{Ideal flow rate} = \text{Nominal flow rate} \times \text{Speed}$$

$$= 10 \text{ cm}^3/\text{rev} \times 1700 \text{ rev/min}$$

$$= 17000 \text{ cm}^3/\text{min}$$

$$\text{Ideal flow rate} = \frac{17000}{100000} = 0.17 \text{ m}^3/\text{min}$$

$$\text{Actual flow rate} = 0.05 \text{ m}^3/\text{min}$$

$$\text{volumetric efficiency} = \frac{0.05}{0.17} = 2.94\% = 29.4\%$$

ii. Fluid Power = $P \times Q$

$$P = 15 \times 15 \text{ N/m}^2$$

$$Q = \frac{0.05 \text{ m}^3/\text{min}}{60} = 0.05 = 8.33 \times 10^{-4} \text{ m}^3 \text{ s}^{-2}$$

$$\begin{aligned} \text{Fluid Power} &= 15 \times 10^5 \times 8.33 \times 10^{-4} \\ &= 1249.5 \text{ watts} \end{aligned}$$

iii. Shaft Power = $\frac{2\pi NT}{60} = \frac{2\pi \times 1700 \times 15}{60}$

$$\text{Shaft power} = 2670.35 \text{ watts}$$

$$\text{Overall efficiency} = \frac{\text{Fluid Power}}{\text{Shaft Power}}$$

$$\frac{\text{Fluid power}}{\text{Shaft power}} = \frac{1249.5}{2670.35} = 0.468$$

$$\therefore \text{Overall efficiency} = 0.468 \times 100 = 46.8\%$$