

Daka - Sherron Olanrewaju 18/ENG2016
Computer Engineering

2) Length, $L = 2.0m$
 $V_1 = 5m/s$
 $V_2 = 2m/s$
 Let the pressure head at the smaller end = $P_1 = \frac{2.3m \text{ of liquid}}{2}$
 Let the loss of head = $h_f = 0.35(V_1 - V_2)$
 $= 0.35(5 - 2) = 0.105m$
 Let the pressure head = $h_2 = 0.2m$ at the larger end = P_2
 Bernoulli's Equation
 $P_1 + \rho V_1^2 + \rho Z_1 = P_2 + \rho V_2^2 + \rho Z_2 + \rho h_f$
 where $P = \rho / \rho$ and $P_2 = P_1 / \rho$
 $Z_1 = 2.0$ and $Z_2 = 0$
 Substituting values in eqn.
 $2.5 + \frac{5^2}{2 \times 9.81} + 2 = \frac{P_2}{\rho} + \frac{2^2}{2 \times 9.81} + 0 + 0.105$
 $2.5 + 2.5 + 2 = \frac{P_2}{\rho} + 0.161$
 $5.74 = \frac{P_2}{\rho} + 0.161$
 $P_2 = 5.409m \text{ of fluid}$

2) $D_1 = 20cm, D_2 = 10cm$
 $A_1 = \frac{\pi D_1^2}{4} = \frac{\pi (20)^2}{4} = 314.16cm^2$
 Let head area = $A_2 = \frac{\pi D_2^2}{4} = \frac{\pi (10)^2}{4} = 78.54cm^2$
 Pressure at inlet = $17.65N/cm^2 = 17.65 \times 10^4 N/m^2$
 $\therefore h_1 = \frac{17.65 \times 10^4}{1000 \times 9.81} = 18m$
 $P_2 = 30cm \text{ Mercury}, 5.0g/cm^3 = 13.6$
 $P_2 = -30 \times 10^{-2} m \text{ of mercury} \times 13.6 = -4.08m$
 Let Differential Head = $H = P_1 - P_2 = \frac{P_1}{\rho} - \frac{P_2}{\rho}$
 $= 18 - (-4.08)$
 $= 18 + 4.08 = 22.08m \times 100$
 $H = 2208cm$
 Using $Q = C_d \sqrt{\frac{2gH}{A_1^2 + A_2^2}} \cdot A_1 A_2$
 $= 0.98 \sqrt{\frac{2 \times 9.81 \times 2208}{(314.16)^2 + (78.54)^2}} \cdot 314.16 \times 78.54$
 $= 0.98 \times \frac{2081.37 \times 24679.1264}{304184.12}$
 $= 1654.55 \frac{cm^3}{s}$
 $= \frac{1654.55}{1000} = 1.65455 \frac{m^3}{sec}$

3) Diameter of pipe $d_1 = 30cm$
 $A_1 = \frac{\pi d_1^2}{4} = \frac{\pi (30)^2}{4} = 706.86cm^2$
 Diameter of Orifice $d_2 = 15cm$
 $A_2 = \frac{\pi d_2^2}{4} = \frac{\pi (15)^2}{4} = 176.71cm^2$
 Specific gravity of oil $S_o = 0.9$
 Specific gravity of mercury = 13.6
 Differential manometer reading, $x = 50cm$ of mercury
 Coefficient of discharge, $C_d = 0.6$
 Differential head, $h = x \left(\frac{S_m}{S_o} - 1 \right)$
 $h = 50 \left(\frac{13.6}{0.9} - 1 \right)$
 $= 705.56cm \text{ of oil}$
 $\therefore P.H. \text{ of flow of oil} = 705.56cm$
 $Q = C_d \sqrt{\frac{2gH}{A_1^2 + A_2^2}} \cdot A_1 A_2$
 $Q = 0.6 \times \sqrt{\frac{2 \times 9.81 \times 705.56 \times 100}{(706.86)^2 + (176.71)^2}} \cdot 706.86 \times 176.71$
 $Q = 13.744329 \frac{cm^3}{s}$
 $Q = \frac{13744.329}{1000} = 13.744 \frac{m^3}{s}$

4. The difference of Mercury level $x = 170cm = 170 \times 10^{-2} = 1.7m$
 The specific gravity of mercury $S_m = 13.6$
 The specific gravity of sea water, $S_o = 1.026$

$h = x \left(\frac{S_m}{S_o} - 1 \right) = 0.17 \left(\frac{13.6}{1.026} - 1 \right) = 2.013m$
 $\therefore V = \sqrt{2gh}$
 $\therefore \sqrt{2 \times 9.81 \times 2.0134} = 6.393m/s$
 $\therefore V = 6.393 \times 60 = 383.58 \frac{km}{hr}$
 s) $Q = 0.05m^3/min = 50dm^3/min$
 $P_1 = 15bar = 15 \times 10^5 Pa = 1.5 \times 10^6 N/m^2$
 Speed = 1700rpm
 $\omega = 15708 \text{ rad/s}, N = 100 \text{ rev/s}$
 (i) Volumetric Efficiency = $\frac{\text{Actual Flow rate}}{\text{Ideal Flow rate}}$
 Ideal Flow rate = Normal Flow rate $\times \text{Speed}$
 $= 10cm^3/rev \times 1700 \text{ rev/min}$
 $= 17000cm^3/min$
 Ideal Flow rate = $17000 \times 0.001 = 0.017m^3/min$
 Actual Flow rate = $0.05m^3/min$
 $\therefore \text{Volumetric Efficiency} = \frac{0.05}{0.017} = 2.94 = 294\%$
 ii) Fluid Power = $P \times Q$
 $P = 1.5 \times 10^6 N/m^2$
 $Q = 0.05m^3/min = \frac{0.05}{60} = 0.000833$
 Fluid Power = $1.5 \times 10^6 \times 0.000833 = 1250 \text{ Watts}$
 $= 1.25 \text{ kW}$

$= 1249.5 \times 10^{-3} \text{ W}$
 Fluid Power = 1249.5 Watts
 iii) Shaft Power = $2 \pi T \omega = \frac{2 \pi \times 1700 \times 15}{60}$
 Shaft Power = 2670.35 Watts
 iv) Overall Efficiency = $\frac{\text{Fluid Power}}{\text{Shaft Power}}$
 $= \frac{1249.5}{2670.35} = 0.468$
 Overall Efficiency = $0.468 \times 100 = 46.8\%$