

Algebra - algebra Samuel Chaw
Civil Engineering 18/5/1403/006

①
 $v = 5 \text{ m/s}$ $v_2 = 2 \text{ m/s}$
 $P_1 = 2.5 \text{ m}$ $P_2 = ?$
 $P_1 = P_2 =$

$$\frac{0.35(v_1 - v_2)^2}{2 \times 9.81}$$

$$= \frac{0.35 \times (5 - 2)^2}{2 \times 9.81}$$

$$= 0.161$$

$P_1 = P_2 = 0.161$
 $2.5 - P_1 = 0.161$
 $P_2 = 2.69 \text{ m}$

②

Inlet diameter = 0.2 m
 Area of $A_1 = \frac{\pi}{4} \times 0.2^2$
 $= 0.0314 \text{ m}^2$

Throat diameter $P_2 = 0.1 \text{ m}$
 $A = \frac{\pi d^2}{4} = A \times 0.1^2$
 $= 0.00785 \text{ m}^2$

Pressure at inlet = 17.658
 ~~17.658 kN/m^2~~
 $= 17658000 \text{ N/m}^2$

$\frac{P_1}{\omega} = \frac{17658000}{9.81}$
 $= 1765800 \text{ N/m}^2$

$\frac{P_1}{\omega} = \frac{17658}{9.81} = 1800 \text{ m}$

Vacuum pressure at the throat
 $\frac{P_2}{\omega} = -0.3 \text{ m of mercury}$
 $= -0.3 \times 13.6 = -4.08 \text{ m of water}$

$Q = 0.03$
 Differential head $h = \frac{P_1}{\omega} - \frac{P_2}{\omega}$

\cong
 Spillage = 13.6
 $\frac{P_1}{\omega} = \frac{17.658 \times 10^{-6}}{1000 \times 9.81}$
 $= 1.8 \times 10^{-3}$

Vacuum pressure = $\frac{P_2}{\omega} = 300 \text{ mmHg}$

$P_2 = -300 \text{ mm of mercury}$
 $= -0.3 \times 13.6 = -4.08$

$Q = 0.03$
 Differential head
 $h = \frac{P_1}{\omega} - \frac{P_2}{\omega}$
 $= 1.8 \times 10^{-3} - (-4.08)$
 $= 4.0818$

$Q = \frac{C_d A_1 A_2}{\sqrt{A_1^2 - A_2^2}} \times \sqrt{2gh}$

$$\frac{0.98 \times 0.034 \times 0.00795}{\sqrt{(0.034)^2 - (0.00795)^2}} \times \frac{2 \times 9.81 \times 4.0803}{4.0803}$$

$$= 6.793 \text{ m/s}$$

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$$d_0 = 15 \times 10^{-2} \text{ m}$$

$$d_1 = 30 \times 10^{-2} \text{ m}$$

$$Q = 0.6 \text{ m}^3/\text{s}$$

$$Q = ?$$

$$S_m = 13.6$$

$$S_0 = 0.9$$

$$A_0 = \frac{A \times (15 \times 10^{-2})^2}{4}$$

$$= 0.01767 \text{ m}^2$$

$$A_1 = \frac{A \times (30 \times 10^{-2})^2}{4} = 0.0707 \text{ m}^2$$

$$h = 50 \times 10^{-2} \left[\frac{13.6}{0.9} - 1 \right]$$

$$h = 2.055 \text{ m}$$

$$Q = C_d A_0 A_1 \sqrt{2gh}$$

$$\frac{Q}{\sqrt{A_1^2 - A_0^2}}$$

$$= \frac{0.64 \times 0.0176 \times 0.0707}{\sqrt{0.0707^2 - 0.0176^2}}$$

$$\times \sqrt{2 \times 9.81 \times 2.055}$$

$$0.0707^2 - 0.0176^2$$

$$= 0.139 \text{ m}^2/\text{s}$$

(4)

$$y = 170 \text{ mm} = 170 \times 10^{-3} \text{ m} \text{ hg}$$

$$S_g \text{ of m} \text{ hg} = 13.6 \text{ hg}$$

$$S_g \text{ of } \text{H}_2\text{O} \text{ water} = 1.026$$

$$h = y \times \frac{S_{g1} - 1}{S_0}$$

$$h = 170 \times 10^{-3} \times \frac{13.6 - 1}{1.026}$$

$$= 2.06 \text{ m}$$

$$V = \sqrt{2gh}$$

$$V = 2 \times 9.81 \times 2.06$$

$$= 6.39 \text{ m/s}$$

(5)

Actual Flow rate

$$Q = 8.33 \text{ m}^3/\text{min} = 8.33 \times 10^{-3} \text{ m}^3/\text{s}$$

$$P = 15 \text{ bar} = 15 \times 10^5 \text{ N/m}^2$$

$$v = 1700 \text{ m/min} = 28.33 \text{ m/s}$$

$$T = 150 \text{ K}$$

$$\text{Normal displacement} = \frac{600 \text{ cm}^3/\text{rev}}{1.4 \times 10^{-5} \text{ m}^3/\text{rev}}$$

Adiabatic Efficiency
Actual Flow rate x 100
Work Fr

Work Fr = Displacement

$$= 1 \times 10^{-5}$$

$$= 2.33 \times 10^{-5}$$

Adiabatic Efficiency

$$= 2.33$$

$$2.33$$

Fluid Power

$$= 8.33 \times 10^{-3}$$

$$= 12 \text{ W}$$

Shaft Power

$$W = 2 \times \pi \times r \times v$$

$$= 2 \times \pi \times 0.075 \times 28.33$$

Torque

$$= 1 \text{ Nm}$$

Overall

Flow

Shaft

$$\frac{\text{Volumetric Efficiency}}{\text{Actual Flowrate} \times 100} \\ \text{Ideal Fr}$$

$$\text{Work Fr} = \rho g Q_{\text{actual}} \times \text{Spinn} \\ = 1 \times 10^{-5} \times 28.33 \\ = 2.833 \times 10^{-4} \text{ m}^3/\text{sec}$$

$$\text{Volumetric Efficiency} \\ = \frac{8.33 \times 10^{-5} \times 100}{2.833 \times 10^{-5}} \\ = 29.4\%$$

$$\text{Fluid Power} = Q \times \rho g \\ = 8.33 \times 10^{-5} \times 1.5 \times 10^5 \\ = 124.95 \text{ Watts}$$

$$\text{Shaft Power} = T \times \omega$$

$$\omega = 2 \times \pi \times \text{rpm} \\ = 2 \times \pi \times 28.33 \\ = 17 \text{ rad/sec}$$

$$T \times \omega \\ = 15 \times 17 = 267 \text{ Watts}$$

Overall Efficiency

$$\frac{\text{Fluid Power} \times 100\%}{\text{Shaft Power}} \\ = \frac{124.95}{267} \times 100 \\ = 46.79\%$$