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18/ENGR06/036

Mechanical engineering
ENGR214 assignment

$$1. \frac{P_1}{\rho} + \frac{v_1^2}{2g} + z_1 = \frac{P_2}{\rho} + \frac{v_2^2}{2g} + z_2 + H_f$$

$$\frac{P_2}{\rho} = \frac{P_1}{\rho} + \frac{v_1^2 - v_2^2}{2g} + (z_1 - z_2) - \frac{0.35(v_1 - v_2)^2}{2g}$$

$$\frac{P_2}{\rho} = 2.5 + \frac{5^2 - 2^2}{2(9.81)} + 2 - \frac{0.35(5-2)^2}{2(9.81)}$$

$$\frac{P_2}{\rho} = 2.5 + 1.07 + 2 - 0.161$$

$$\frac{P_2}{\rho} = 5.409 \text{ m of liquid}$$

$$2. d_1 = 20 \text{ cm} = 0.2 \text{ m}, d_2 = 10 \text{ cm} = 0.1 \text{ m}$$

$$P_1 = 17.658 \text{ MNm}^{-2} = 176580 \text{ Nm}^{-2}, P_2 = 0.30 \text{ cmHg} \\ = 0.3 \text{ mHg}$$

$$A_1 = \frac{\pi(0.2)^2}{4} = 0.031 \text{ m}^2$$

$$A_2 = \frac{\pi(0.1)^2}{4} = 7.85 \times 10^{-3} \text{ m}^2$$

$$h = \frac{P_1}{\rho} - \frac{P_2}{\rho} = \frac{176580}{(1000 \times 9.81)} - (-0.3 \times 13.6)$$

$$h = 18 + 4.08 = 22.08 \text{ m}$$

$$C_d = 0.98$$

$$Q = \frac{C_d A_1 A_2 \sqrt{2gh}}{\sqrt{A_1^2 - A_2^2}} = 0.98 \times 0.031 \times 7.85$$

$$= \frac{0.98 \times 0.031 \times 7.85 \times 10^{-3} \times \sqrt{2 \times 9.81 \times 22.08}}{\sqrt{(0.031^2 - (7.85 \times 10^{-3})^2)}}$$

Continuation of 2

$$Q = 8.85 \times 10^{-5} \times 20.81$$

$$Q = 0.67 \text{ m}^3/\text{s}$$

$$3. A_0 = \pi (0.15)^2 = 0.0177 \text{ m}^2, A_1 = \pi (0.30)^2 = 0.0707 \text{ m}^2$$
$$y = 50 \text{ cmHg} = 0.3 \text{ mHg}, S_0 = 0.9, C_d = 0.64$$

$$h = 7.05 \text{ m}$$

$$Q = \frac{C_d A_0 A_1 \sqrt{2gh}}{\sqrt{A_1^2 - A_0^2}} = \frac{0.64 \times 0.0177 \times 0.0707 \times \sqrt{2 \times 9.81 \times 7.05}}{\sqrt{0.0177^2 - 0.0707^2}}$$
$$= \frac{9.4193 \times 10^{-3}}{0.0685} = 0.1376 \text{ m}^3/\text{s}$$

$$4. y = 170 \text{ mmHg} = 0.17 \text{ mHg}, S_0 \text{Hg} = 13.6, S_{\text{oil}} = 1.026$$
$$\Delta h = y \left[\frac{S_0 \text{Hg}}{S_{\text{oil}}} - 1 \right] = 0.17 \left[\frac{13.6}{1.026} - 1 \right]$$

$$\Delta h = 2.08 \text{ m}$$

$$v = \sqrt{2g\Delta h} = \sqrt{2 \times 9.81 \times 2.08}$$
$$v = 6.388 \text{ m/s}$$

$$5. Q = 0.05 \text{ dm}^3/\text{min} = 8.33 \times 10^{-3} \text{ m}^3/\text{sec}$$

$$\text{speed of rotation} = 1700 \text{ rev/min} = 28.3 \text{ rev/sec}$$

$$\text{Nominal displacement} = 10 \text{ cm}^3/\text{rev} = 10^{-5} \text{ m}^3/\text{rev}$$

$$\text{Torque input} = 15 \text{ Nm}$$

$$\text{Pressure change} = 15 \text{ bar} = 15 \times 10^5 \text{ Nm}^2$$

$$\text{Ideal flow rate} = \text{nominal displacement} \times \text{speed of rotation}$$

$$= 10^{-5} \times 28.3 = 2.83 \times 10^{-4} \text{ m}^3/\text{sec}$$

$$\text{Volumetric efficiency} = \frac{\text{Actual flow rate}}{\text{Total flow rate}} \times 100$$

$$= \frac{8.33 \times 10^{-5}}{2.83 \times 10^{-4}} \times 100 = 29.45 \%$$

Continuation of 5.

b. fluid power, $P = Q \Delta r$

$$= 8.33 \times 10^{-5} \times 15 \times 10^5 = 124.95 \text{ watts}$$

c. Shaft power = $T \times \omega$

$$\omega = 2\pi \times \text{Speed of rotation} = 2\pi \times 28.3$$

$$= 177.81 \text{ rad/sec}$$

$$\therefore \text{Shaft power} = 15 \times 177.81 = 2667.2 \text{ watts}$$

d. Overall efficiency = $\frac{\text{fluid power}}{\text{Shaft power}} \times 100$

$$= \frac{124.95}{2667.2} \times 100$$

$$= 4.68\%$$