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 18/ENG02/066
 Computer Eng.
 ENG 214

$$1) \text{ Ideal flow rate} = \text{normal displacement} \times \text{speed}$$

$$= 10 \times 1500$$

$$= 15 \text{ dm}^3/\text{min}$$

$$(i) \text{ Volumetric efficiency} = \frac{\text{Actual flow}}{\text{Idea flow}}$$

$$= \frac{10}{15} \times 100$$

$$= 66.7\%$$

$$(ii) \text{ Fluid power} = \Delta P \cdot Q$$

$$= (1.2 \times 10^5)(1.67 \times 10^{-3})$$

$$= 200.4 \text{ W}$$

$$(iii) \text{ Shaft power} = \frac{2\pi NT}{60}$$

$$= \frac{2 \times \pi \times 1500 \times 12.5}{60}$$

$$= 1963.5 \text{ Nm}$$

$$\Delta P = 1.2 \times 10^5$$

$$Q = \frac{10 \times 10^{-3}}{60}$$

$$= 1.67 \times 10^{-4}$$

$$N = 1500 \text{ rev/min}$$

$$T = 12.5 \text{ Nm}$$

$$(iv) \text{ Overall efficiency} = \frac{\text{Fluid power}}{\text{Shaft Power}}$$

$$= \frac{200.4}{1963.5} \times 100$$

$$= 10.2\%$$

$$2) \text{ Fluid power} = \Delta P Q$$

$$= (100 \times 10^5)(5.83 \times 10^{-4})$$

$$= 5830$$

$$\text{Overall efficiency} = \frac{\text{Fluid power}}{\text{Shaft power}}$$

$$0.87 = \frac{5830}{\text{S.P}}$$

$$\text{S.P} = \frac{5830}{0.87} = 6701.15 \text{ Nm}$$

$$P = 100 \times 10^5 \text{ N/m}^2$$

$$Q = 5.83 \times 10^{-4}$$

$$\text{Overall efficiency} = 87\%$$

$$= 0.87$$

$$\begin{aligned}
 3) \text{ Ideal flow rate} &= \text{normal displacement} \times \text{speed} \\
 &= 50 \times 850 \\
 &= 42.5 \text{ dm}^3/\text{min}
 \end{aligned}$$

$$\begin{aligned}
 \text{(i) Volumetric efficiency} &= \frac{\text{Actual flow}}{\text{Ideal flow}} \\
 &= \frac{35}{42.5} \times 100 \\
 &= 82.4\%
 \end{aligned}$$

$$\begin{aligned}
 \text{(ii) Fluid power} &= \Delta P Q \\
 &= (100 \times 10^5) (8.33 \times 10^{-4}) \\
 &= 8330 \text{ W}
 \end{aligned}$$

$$\begin{aligned}
 \Delta P &= 100 \times 10^5 \\
 Q &= \frac{50 \times 10^{-3}}{60} \\
 &= 8.33 \times 10^{-4}
 \end{aligned}$$

$$\begin{aligned}
 6) \quad V_F^2 &= V_1^2 - 2gh \\
 V_1 &= \sqrt{V_F^2 + 2gh} \\
 &= \sqrt{0 + 2(9.81)(20)} \\
 &= 19.81 \text{ m/s}
 \end{aligned}$$

$$\begin{aligned}
 h &= 20 \text{ m} \\
 d &= 10 \text{ cm} = 0.1 \text{ m} \\
 A &= \frac{\pi}{4} \times 0.1^2 \\
 &= 0.00785 \text{ m}^2 \\
 W &= ?
 \end{aligned}$$

Then;

$$\begin{aligned}
 Q &= VA \\
 &= 19.81 \times 0.00785 \\
 &= 0.156 \text{ m}^3/\text{s}
 \end{aligned}$$

$$\begin{aligned}
 W &= \rho g Q h \\
 &= 1000 \times 9.81 \times 0.156 \times 20 \\
 &= 30607.2 \text{ Kg m}^2/\text{s}^3 \\
 &= 30.6 \times 10^4 \text{ W}
 \end{aligned}$$

$$\begin{aligned}
 7) \quad P_1 + \rho g z_1 &= P_2 + \rho g (z_2 - z_1) + \rho g h_p \\
 P_1 - P_2 &= 19.62 (z_2 - z_1) + 587.423 \quad \text{--- (1)}
 \end{aligned}$$

Venturimeter:

$$\frac{P_1}{\rho g} + \frac{U_1^2}{2g} + z_1 = \frac{P_2}{\rho g} + \frac{U_2^2}{2g} + z_2$$

$$P_1 - P_2 = 19.62 (z_2 - z_1) + 0.803 U_2^2 \quad \text{--- (2)}$$

$$\begin{aligned}
 \rho g &= 19.62 \text{ N/m}^2 \\
 C_d &= 0.96 \\
 d_1 &= 0.3 \text{ m} \\
 d_2 &= 0.2 \text{ m} \\
 U_1 &=
 \end{aligned}$$

8) Using Bernoulli's equation

$$\frac{P_1}{\rho g} + \frac{V_1^2}{2g} + Z_1 = \frac{P_2}{\rho g} + \frac{V_2^2}{2g} + Z_2$$

a) $P_1 = P_2$

$$\therefore \frac{V_1^2}{2g} + Z_1 = \frac{V_2^2}{2g} + Z_2$$

$$Q = V_1 A_1 = V_2 A_2$$

$$V_2 = \frac{V_1 A_1}{A_2} = 0.4$$

$$V_1 = \sqrt{\frac{0.914 \times 2 \times 9.81}{15}} = 1.0934 \text{ m/s}$$

$$Q = C_d A_1 V_1 = 0.96 \times 0.01815 \times 1.0934 = 0.019 \text{ m}^3/\text{s}$$

b) $P_1 - P_2 = 15170$

$$\frac{P_1 - P_2}{\rho g} = \frac{V_2^2 - V_1^2}{2g} - 0.914$$

$$\frac{15170}{\rho g} = \frac{Q^2 (220.43^2 - 55.11^2)}{2g} - 0.914$$

$$Q = 0.035 \text{ m}^3/\text{s}$$

9) $A_1 V_1 = A_2 V_2 = 40 \text{ l/sec} = 40 \times 10^{-3} \text{ m}^3/\text{sec}$

$$V_1 = \frac{40 \times 10^{-3}}{0.0707} = 0.566 \text{ m/s}$$

$$V_2 = \frac{40 \times 10^{-3}}{0.0177} = 2.260 \text{ m/s}$$

Applying Bernoulli's method

$$\frac{400 \times 10^3}{9800} + \frac{(0.566)^2}{2 \times 9.8} + 10 = \frac{P_2}{\rho} + \frac{(2.264)^2}{2 \times 9.8} + 6$$

$$\frac{P_2}{\rho} = 44.57 \text{ N/m}^2$$

$$d_1 = 0.152 \text{ m}$$

$$d_2 = 0.076 \text{ m}$$

$$\rho = 800 \text{ kg/m}^3$$

$$C_d = 0.97$$

$$A_1 = 0.01815 \text{ m}^2$$

$$A_2 = 0.00454 \text{ m}^2$$

$$d_1 = 0.3 \text{ m}$$

$$A_1 = \frac{\pi}{4} \times 0.3^2 = 0.0707 \text{ m}^2$$

$$Z_1 = 10 \text{ m}$$

$$P_1 = 400 \times 10^3 \text{ N/m}^2$$

$$V_1 = ?$$

$$d_2 = 0.15 \text{ m}$$

$$A_2 = \frac{\pi}{4} \times (0.15)^2 = 0.0177 \text{ m}^2$$

$$V_2 = ?$$

$$P_2 = ?$$

$$Z_2 = 6 \text{ m}$$

$$\begin{aligned} 10) \quad h &= y \left[\frac{s_{hl}}{s_l} - 1 \right] \\ &= 0.17 \left[\frac{13.6}{1.026} - 1 \right] \\ &= 2.08 \end{aligned}$$

$$\begin{aligned} v &= \sqrt{2gh} \\ &= \sqrt{2 \times 9.81 \times 2.08} \\ &= 6.388239194 \\ &\approx 6.39 \text{ m/s} \end{aligned}$$

$$\begin{aligned} y &= 170 \text{ mm} = 0.17 \text{ m} \\ Hg, s_{hl} &= 13.6 \\ \text{Seawater, } s_l &= 1.026 \end{aligned}$$