

$$D = 2.0 \text{ m}$$

$$v_1 = 5 \text{ m/s}$$

$$L = 2.5 \text{ m}$$

$$v_2 = 2 \text{ m/s}$$

$$h = 0.25 (v_1 - v_2)^2$$

$$= \frac{0.25 (5-2)^2}{2 \times 9.81}$$

$$= 0.1618 \text{ m}$$

Franklin's equation

$$\frac{p_1}{\rho} + \frac{v_1^2}{2g} + z_1 = \frac{p_2}{\rho} + \frac{v_2^2}{2g} + z_2 + h$$

where $z_1 = 2 \text{ m}$ and $z_2 = 0 \text{ m}$

$$2.5 + \frac{5^2}{2 \times 9.81} + 2 = \frac{p_2}{\rho} + \frac{2^2}{2 \times 9.81} + 0 + 0.161$$

$$4.5 + \frac{25}{19.62} = \frac{p_2}{\rho} + \frac{4}{19.62} + 0.161$$

$$\frac{p_2}{\rho} = \frac{25 - 4 + 45 - 0.161}{19.62}$$

$$\frac{p_2}{\rho} = \frac{21 + 43.79}{19.62}$$

$$= 1.07 + 4.339$$

$$\frac{p_2}{\rho} = 5.409 \text{ m of liquid}$$

$$2) d_1 = 20 \text{ cm} = 0.2 \text{ m}$$

$$A_1 = \frac{\pi \times 0.2^2}{4} = 0.0314 \text{ m}^2$$

$$d_2 = 10 \text{ cm} = 0.1 \text{ m}$$

$$A_2 = \frac{\pi \times 0.1^2}{4} = 0.0079 \text{ m}^2$$

$$p_1 = 17.658 \text{ N/cm}^2 = 17.658 \times 10^4 \text{ N/m}^2$$

Ans: 1) 0.1618 m

density of water = 1000 kg/m^3

$$\rho_1 = 17.658 \times 10^4$$

$$\rho_2 = \frac{1000 \times 9.81}{1.8} = 5450 \text{ N/m}^2$$

$$p_2 = -30 \text{ cm mercury}$$

$$p_2 = -0.3 \text{ m mercury}$$

$$= -0.3 \times 13.6 = -4.08 \text{ m of water}$$

$$h = \frac{p_1}{\rho} - \frac{p_2}{\rho}$$

$$= 1.07 - (-4.08)$$

$$= 5.15 \text{ m}$$

$$= 22.88 \text{ m of water}$$

$$Q_1 = Q_2 = A_1 v_1 = A_2 v_2$$

$$0.0314 \times 5 = 0.0079 \times v_2$$

$$v_2 = \frac{0.0314 \times 5}{0.0079} = 19.87 \text{ m/s}$$

$$Q = A v = 0.0314 \times 19.87 = 0.624 \text{ m}^3/\text{s}$$

$$= 16.05 \text{ m}^3/\text{s}$$

$$3) d_0 = 15 \text{ cm} = 0.15 \text{ m}$$

$$A_0 = \frac{\pi \times 0.15^2}{4} = 0.0177 \text{ m}^2$$

$$d_1 = 30 \text{ cm} = 0.3 \text{ m}$$

$$A_1 = \frac{\pi \times 0.3^2}{4} = 0.0707 \text{ m}^2$$

5) 40.1 -
Mansour

h =

*) x =

5.9 m

5.9 m

h =

v =

v =

5) Volume

Spe

Sp - 1

Normal

$S_{y_{oil}} = 0.9$
 diameter of rod $d = 50 \text{ mm}$
 viscosity $\mu = 50 \text{ cP}$

$$h = x \left(\frac{50 \text{ mm}}{59 \text{ oil}} - 1 \right) = 0.05 \left(\frac{136}{0.9} - 1 \right)$$

$$= 0.5 \times 1411 = 7.055 \text{ m oil}$$

$$Q_u = C_d \frac{A_0 A_1}{\sqrt{A_1^2 - A_0^2}} \times \sqrt{2gh}$$

$C_d = 0.64$

$$Q_u = 0.64 \times \frac{0.0177 \times 0.0702 \sqrt{2 \times 9.81 \times 7.055}}{\sqrt{0.0702^2 - 0.0177^2}}$$

$$= \frac{0.0872256 \times 11.765}{0.66845} = 0.138 \text{ m}^3/\text{s}$$

$x = 170 \text{ mm} = 0.17 \text{ m}$
 $S_{y_{mercury}} = 13.6$
 $S_{y_{oil}} = 0.9$

$$h = x \left(\frac{S_{y_{mercury}}}{S_{y_{oil}}} - 1 \right) = 0.17 \left(\frac{13.6}{0.9} - 1 \right)$$

$$= 2.0874 \text{ m}$$

$$v = \sqrt{2gh}$$

$$v = \sqrt{2 \times 9.81 \times 2.0874} = 6.393 \text{ m/s}$$

$$= 6.393 \text{ m/s} \times \frac{3600}{1000} = 23 \text{ km/hr}$$

3) Volumetric flow rate $= 0.15 \text{ m}^3/\text{min} \times \frac{1}{60}$
 $S_{y_{oil}} = 0.9$
 $Q = 8.33 \times 10^{-4} \text{ m}^3/\text{s}$
 Speed $= 1700 \text{ rpm} \times \frac{1}{60} = 28.33 \text{ rps}$
 $\mu = 15 \text{ bar} = 15 \times 10^5 \text{ N/m}^2$
 Nominal displacement $= 10 \text{ cm}^3/\text{rev} \times 10^{-6}$
 $= 1 \times 10^{-5} \text{ m}^3/\text{rev}$

Ideal flow rate = Nominal displacement \times speed
 $= 1 \times 10^{-5} \times 28.33$
 $= 2.833 \times 10^{-4}$

Volume efficiency $= \frac{\text{Actual flow rate}}{\text{Ideal flow rate}}$
 $= \frac{8.33 \times 10^{-4}}{2.833 \times 10^{-4}}$
 $= 2.94\%$

1) Fluid power $= Q \times p$
 $= 0.138 \times 15 \times 10^5$
 $= 1250 \text{ Nm/s}$

2) Shaft power $= T \times \omega$
 $T = 15 \text{ Nm}$
 $\omega = 2\pi \times 28.33$
 $= 178.02 \text{ rad/sec}$
 $PW = 178.02 \times 15$
 $= 2670.35 \text{ W}$

Overall efficiency $= \frac{\text{Fluid power}}{\text{Shaft power}}$
 $= \frac{1250 \times 100}{2670}$
 $= 46.8\%$