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1) $M = Pi - 6j - 3k$, $N = 4i + 3j - k$, $O = i - 3j + 2k$.

a) M and N are perpendicular to each other.

$$\begin{aligned}\therefore M \cdot N &= (Pi - 6j - 3k) \cdot (4i + 3j - k) \\ &= 4P - 18j + 3 \\ &= 4P - 15\end{aligned}$$

Since they are perpendicular,

$$4P - 15 = 0$$

$$P = 15/4 //$$

b) M, N and O are co-planar.

$M \cdot (N \times O)$

$$N \times O = \begin{vmatrix} i & j & k \\ 4 & 3 & -1 \\ 1 & -3 & 2 \end{vmatrix}$$

$$\begin{aligned}&= i(6-3) - j(8+1) + k(12-3) \\ &= 3i - 9j - 15k\end{aligned}$$

$$\begin{aligned}\therefore M \cdot (N \times O) &= (Pi - 6j - 3k) \cdot (3i - 9j - 15k) \\ &= 3Pi + 54j + 45k\end{aligned}$$

$$\therefore 3P + 54 + 45 = 0$$

$$3P + 99 = 0$$

$$P = -33 //$$

2) $\vec{v} = (3i + 2j + 5k) + (i - j + 6k) + (5j + 2j - 3k)$
 $= 10i + 3j + 8k$

$$a_x = 10, a_y = 3 \text{ and } a_z = 8$$

$$|\vec{v}| = \sqrt{10^2 + 3^2 + 8^2}$$

$$= \sqrt{100 + 9 + 64}$$

$$= \sqrt{173} = 13.15$$

direction of cosine are:

$$\cos \alpha = \frac{a_x}{|\vec{v}|} = \frac{10}{13.15} = 0.761$$

$$\cos \gamma = \frac{a_z}{|\vec{v}|} = \frac{8}{13.15} = 0.608$$

$$\cos \beta = \frac{a_y}{|\vec{v}|} = \frac{3}{13.15} = 0.228$$

ii) unit vector $\therefore \frac{v}{|v|} = \frac{10i + 3j + 8k}{13.15}$

3) $F = 3ui + u^2j + (u+2)k$
 $v = 2ui - 3uj + (u-2)k$

$$F \times v = \begin{vmatrix} i & j & k \\ 3u & u^2 & (u+2) \\ 2u & -3u & (u-2) \end{vmatrix}$$

$$F \times v = i [u^3 - 2u^2 + 3u^2 + 6u] - j [u^2 - 10u] + k [-2u^3 - 9u^2]$$

$$= i [u^3 + u^2 + 6u] - j [u^2 - 10u] + k [-2u^3 - 9u^2]$$

$$\int (F \times v) = \int i [u^3 + u^2 + 6u] - \int j [u^2 - 10u] + \int k [-2u^3 - 9u^2]$$

$$= i \int u^3 + u^2 + 6u - j \int u^2 - 10u + k \int -2u^3 - 9u^2$$

$$= i \left[\frac{u^4}{4} + \frac{u^3}{3} + 6u \right] - j \left[\frac{u^3}{3} - 5u \right] + k \left[\frac{-2u^4}{4} - \frac{9u^3}{3} \right] + c$$

$$= i \left[\frac{u^4}{4} + \frac{u^3}{3} + 3u^2 \right] - j \left[\frac{u^3}{3} - 5u^2 \right] + k \left[\frac{-u^4}{2} - 3u^3 \right] + c$$

$$\int (F \times v) = i \left[\frac{1^4}{4} + \frac{1^3}{3} + 3(1)^2 \right] - j \left[\frac{1^3}{3} - 5(1)^2 \right] + k \left[\frac{-(1)^4}{2} - 3(1)^3 \right] + c = [0 + c]$$

∴ taking the l.c.m.

$$\therefore \int (F \times v) = i \left[\frac{43}{12} \right] - j \left[\frac{-14}{3} \right] + k \left[\frac{-7}{2} \right]$$

$$\therefore \int (F \times v) = \frac{43}{12} i - \frac{14}{3} j - \frac{7}{2} k //$$