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Matric no: 19/MHS01/244

Course code: Maths b4

Department: MBBS

1. Integrate $\sin^6 x$

$$\int \sin^6(x) dx = \int (\sin^2(x))^3 dx$$

$$\text{Recall that } \sin^2(\theta) = \frac{1}{2}(1 - \cos(2\theta))$$

$$\int (\sin^2(x))^3 dx = \int \frac{1}{2}(1 - \cos(2x))^3 dx$$

$$= \int \left(\frac{1}{2}\right)^3 (1 - \cos(2x))^3 dx$$

$$= \int \frac{1}{8} (1 - \cos(2x))^3 dx$$

$$= \int \frac{1}{8} (1 - 3\cos(2x) + 3\cos^2(2x) - \cos^3(2x)) dx$$

$$= \frac{1}{8} \int dx - \frac{3}{8} \int \cos(2x) dx + \frac{3}{8} \int \cos^2(2x) dx - \frac{1}{8} \int \cos^3(2x) dx$$

$$\frac{x}{8} - \frac{3\sin(2x)}{16} + \frac{3x}{16} + \frac{3\sin(4x)}{64} - \frac{\sin(2x)}{16} + \frac{\sin^3(2x)}{48} + C$$

$$= \frac{x}{8} + \frac{3x}{16} - \frac{3\sin(2x)}{16} + \frac{3\sin(4x)}{64} - \frac{1}{6}\sin(2x) + \frac{1}{48}\sin^3(2x) + C$$

$$= \frac{5x}{16} - \frac{3\sin(2x)}{16} + \frac{3\sin(4x)}{64} - \frac{1}{6}\sin(2x) + \frac{1}{48}\sin^3(2x) + C$$

2. $\int \cos^4 x \sin^3 x dx = \int \sin(x) \cdot \sin^2(x) \cdot \cos^4(x) dx$

$$= \int \sin(x) \cdot (1 - \cos^2(x)) \cdot \cos^4(x) dx$$

Let $u = \cos(x)$

$$du = -\sin(x) dx$$

$$-du = \sin(x) dx$$

$$= \int \sin(x) \cdot (1 - u^2) u^4 dx = \int (1 - u^2) u^4 \sin(x) dx$$

$$= \int (1 - u^2) u^4 \cdot -du$$
$$\int (u^6 - u^4) du = \frac{u^7}{7} - \frac{u^5}{5} + C$$

$$= \frac{\cos^7(x)}{7} - \frac{\cos^5(x)}{5} + C$$

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$$B. \cos(x) \sin 3x = \int \sin(3x) \cos(x) dx$$

Recall,

$$\sin a \cdot \cos b = \frac{1}{2} (\sin(a+b) + \sin(a-b))$$

$$\sin(3x) \cos(x) = \frac{1}{2} (\sin(4x) + \sin(2x))$$

$$= \frac{1}{2} \int \sin(4x) dx + \frac{1}{2} \int \sin(2x) dx$$

$$= \frac{1}{2} \left(\frac{-\cos 4x}{4} \right) + \frac{1}{2} \left(\frac{-\cos 2x}{2} \right) + C$$

$$\cos(x) \sin(3x) = \frac{-\cos(4x)}{8} - \frac{\cos 2x}{4} + C$$