

$$\int \cos x \sin^3 x \, dx$$

substitute $u = \sin x$

$$= \int u^3 \, dx$$

$$= \frac{u^4}{4}$$

substitute back

$$= \frac{\sin^4 x}{4}$$

$$= \frac{\sin^4(x)}{4} + C$$

$$2. \int \cos^4 x \sin^3 x \, dx$$

Let $u = \cos x$

$$= \int -u^4 + u^6 \, du$$

$$= -\int u^4 \, du + \int u^6 \, du$$

$$= -\frac{u^5}{5} + \frac{u^7}{7}$$

$$= -\frac{\cos^5 x}{5} + \frac{\cos^7 x}{7} \quad \text{substitute back}$$

$$= -\frac{\cos^5 x}{5} + \frac{\cos^7 x}{7} + C$$

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Assignment

$$\int \sin^6 x \, dx$$

$$= \frac{-1}{6} \times \sin^5(x) \cos(x) + 5 \int \sin^4(x) \, dx$$

$$= \frac{-1}{6} \sin^5(x) \cos(x) + 5 \times \frac{(-1) \sin^4(x) \cos(x)}{4} + 3 \int \sin^2(x) \, dx$$

$$= \frac{-1}{6} \times \sin^5(x) \cos(x) + 5 \left(\frac{-1 \sin^4(x) \cos(x)}{4} + 3 \int \frac{1 - \cos(2x)}{2} \, dx \right)$$

$$= \frac{-1}{6} \sin^5(x) \cos(x) + 5 \left(\frac{1 \sin^4(x) \cos(x)}{4} + 3 \int \frac{1 - \cos(2x)}{2} \, dx \right)$$

$$= \frac{-1 \sin^5(x) \cos(x)}{6} + 5 \left(\frac{-1 \sin^4(x) \cos(x)}{4} + 3 \times \frac{1}{2} \int (1 - \cos(2x)) \, dx \right)$$

$$= \frac{-1 \sin^5(x) \cos(x)}{6} + 5 \times \left(\frac{-1 \sin^4(x) \cos(x)}{4} + 3 \left(\frac{1}{2} x - \int \cos(2x) \, dx \right) \right)$$

$$= \frac{-1 \sin^5(x) \cos(x)}{6} + 5 \left(\frac{-1 \sin^4(x) \cos(x)}{4} + 3 \left(\frac{x - \sin(2x)}{2} \right) \right)$$

$$= \frac{\sin^5(x) \cos(x)}{6} - \frac{5 \sin^4(x) \cos(x)}{24} - \frac{5}{16} x \sin(2x) + \frac{5 \sin(2x)}{32}$$