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**A SUMMARY REPORT**

**ON**

**ELECTRICAL CONDUCTIVITY OF FLUID-SATURATED ROCKS**

**FROM**

**PETROLEUM RESERVOIR ENGINEERING PHYSICAL PROPERTIES**

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**17/ENG07/022**

**FOR**

**PTE 312: RESEVOIR ENGINEERING II**

**TO BE SUBMITTED**

**DEPARTMENT OF PETROLEUM & CHEMICAL ENGINNERING, COLLEGE OF ENGINEERING, AFE BABALOLA UNIVERSITY, ADO-EKITI**

**DATE OF SUBMISSION: 30th MAY, 2020**

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CHAPTER ONE

# **ELECTRICAL CONDUCTIVITY**

Resistivity can also be defined as the ratio of the potential difference, , to the current, , across material which has a cross-sectional area of 1 and is 1 m long.

Electrical conductivity in minerals and solutions takes place by movement of electrons and ions. Most rocks near the earth’s surface have low conductivity. Conduction of electricity is mostly through groundwater contained in pores of the rocks and along surface layers at the contact of rocks and solution. The case of altered rocks in high temperature areas will be discussed separately.

## **RESISTIVITY RELATIONS**

The electrical properties predominantly depend on the geometry of these void spaces and the fluids which resides in the void. In the study of petroleum engineering we are concerned with three fluids they are oil, gas and water. By knowing and estimating the resistivity of the rock matrix, we can further determine its conductivity- why?. This is because the reciprocal of resistivity is conductivity.

Where

In oil-field practice, the resistivity in ohms-meter is commonly represented by symbol R with an appropriate subscript to define the conditions to which R applies.

## **FORMATION FACTOR**

In the late 1920s and early 1930s Archie observed that the bulk resistivity of a rock fully saturated with an aqueous fluid of resistivity is directly proportional to the resistivity of the fluid

Where F is known as the “**formation factor**” or the “**formation resistivity factor**” and describes the effect of the presence of the rock matrix. It can be immediately seen that F = 1.00 for a rock with 100% porosity, i.e., no matrix, just 100% fluid.

The formation resistivity factor, FR, is the ratio of the resistivity of a porous medium that is completely saturated with an ionic brine solution divided by the resistivity of the brine.

Where:

* *Ro* = Resistivity of fully water saturated rock
* *Rw* = Saturating water resistivity

The relationship between electrical properties and the physical properties of the rock are complex but can illustrated by the following proof:

Consider matrix cube of salt water having cross sectional area A, length L, and a resistivity of Rw. Suppose an electrical current is caused to flow the cube, the resistivity of the cube can be determined by;

Now let another cube, cube B with the same dimensions as the former cube, cube A of salt water having 100% saturation of water, but cube B is filled with non-conducting solids and partially saturated with water. Consider, electrical current must then flow through the water pores of cube B having a cross sectional area, Aa of the conduction and the length of the current flow La. Finally, the resistance of Cube B is given as;

Recall

Therefore

But

Where τ is tortuosity

## **RESISTIVITY INDEX**

let consider the cube of a porous rock that contains both hydrocarbons and water, being the only conductor. A decrease in cross sectional area of the conduction is denoted by and the path length of the current flow to be . Then the resistance of such cube is given as;

Then the resistivity of the entire rock formation is;

The ratio of the resistivity of partially saturated rock to the resistivity of the entire rock is known as resistivity index, I

Models have been introduced to develop a relation between formation factor , resistivity index , with porosity and tortuosity . These models include;

1. Wyllie model: its considered that the various pore openings are continuous. The cross sectional area of these pore openings vary with their length but in a manner that the sum of areas of the pores is constant.

Therefore

Introducing hydrocarbons to the pores, the water saturation is expressed as a fraction of pore volume. The presence of hydrocarbon further reduced the cross sectional area for current flow to and the effective path length to

Thus

1. Cornell & kartz: In this model, the pores can be uniformed in cross sections but oriented so that they have an effective length which is greater than . The cross sectional area available for flow is uniform across the matrix. The effective cross sectional area is the area normal to the direction of the flow of the pore;

Introducing the hydrocarbon saturation;

Archie in 1942, correlated several formation factors with porosity and permeability. He suggested that the formation factor with the porosity was the better correlation and that formation factor should be expressed as

Where is the fractional porosity and m is the cementation factor. For consolidated sandstones the cementation factor ranged from 1.8-2.0, while for unconsolidated sandstones is 1.3

Other correlation/model of formation resistivity are in the table below

|  |  |
| --- | --- |
| Source | Relation |
| * Wyllie and rose |  |
| * Tixier |  |
| * Winsauer et al |  |

CHAPTER TWO

# **HOW TO MEASURE THE ELECTRICAL RESISTIVITY OF ROCK**

Various devices have been employed to measure the electrical resistivity of rock. The measurement requires a knowledge of the dimension of rock, fluid saturation of rock, the resistivity of the water contained in the rock, and a suitable resistivity cell in which the test is carried out.

A sample cut of the rock is placed in the cell and clamped between electrodes, current is then passed through the sample and the potential drop is observed and the resistance is calculated from ohms law;

And the resistivity is calculated from;

Where A is the cross sectional area of the sample, L is the length of the sample

## **CORRELATIONS OF ELECTRICAL PROPERTIES**

Some of these correlation have been discussed earlier and a short table gives an overview. These correlations include;

* Wyllie was concerned with the influence of particle size and cementation on the formation factor of a variety of materials. Unconsolidated materials were packed in tubes, and were artificially consolidated. It may be noted that cementation results in increased values of formation factor over that observed for un-cemented aggregates. Furthermore, the cemented aggregates exhibit a greater change in formation factor with a change in porosity than unconsolidated aggregates. The correlation include;
* Winsaeur reported a correlation referred to as the Humble relations

## **EFFECT OF CONDUCTIVE SOLIDS**

The formation factor for a clean sand is constant. The formation factor for the clayey sand increases with decreasing water resistivity and approach a constant value at a water resistivity of about 0.1ohm-m. This phenomenon is similar to clay minerals in two electrical circuits connected in parallel

Where is the resistivity of a shaly sand when 100% saturated with water resistivity , is the resistivity due to the clay minerals; is the resistivity due to distributed water and F is the true formation factor of the rock.

Hill and Milburn developed a correlation for the formation factor of shaly sand. It was based on the measurement of large number of samples

Where is the formation factor of the rock when saturated with water having resistivity of 0.01ohm-m. The quantity in the exponent is defined as a shaliness factor and was correlated with cation-exchange capacity. The cation-exchange capacity is related to the clay content of the rock and provides an independent determination of the amount of shale in the rock

CHAPTER THREE

# **RESISTIVITY OF PARTIALLY WATER-SATURATED ROCK**

From studies, a rock containing both hydrocarbon and water has a higher resistivity than another that is fully saturated with water. The resistivity of partially water-saturated rock is a function of the water saturation

Meanwhile the resistivity index is a function of the water saturation and path length, thus the following axiom is produced;

Where C is a function of tortuosity and n is saturation exponent. Few scientist made improvement to the general;

* Achie -
* Willams -

## **USE OF ELECTRICAL PARAMETER IN CHARACTERIZING POROUS MEDIA**

This entails kozeny equation and it is developed as follows;

where is the permeability, is the porosity function, is a shape factor, is the internal surface area per unit pore volume and is the kozeny tortuosity.

CHAPTER FOUR

# CONCLUSION

Confinement or overburden pressure may cause a significant increase in resistivity by blocking of some conduction paths and reduction in the cross sections which are available for flow.  This usually occurs in rocks with low porosity or that are not well cemented. The formation resistivity factor *F*, which is sometimes referred to as the formation factor, can be estimated from an empirical relationship between formation resistivity factor *F* and porosity ϕ. The empirical relationship is

# **REFERENCES**

*FORMATION RESISTIVITY FACTOR* . (2016). Retrieved from SCIENCE DIRECT: https://www.sciencedirect.com/topics/engineering/formation-resistivity-factor