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① $\int \sin^6 x$

$$= \int \sin^2 x \cdot \sin^4 x \, dx$$

$$= \int (\cos^2 x) \cdot (\sin^2 x)^2 \, dx$$

$$= \int \left(\frac{1 - \cos 2x}{2} \right) \cdot \left(\frac{1 - \cos 2x}{2} \right)^2 \, dx$$

$$= \int \left(\frac{1 - \cos 2x}{2} \right) \left(\frac{1 - 2\cos 2x + \cos^2 2x}{4} \right) \, dx$$

$$= \frac{1}{8} \int (1 - 2\cos 2x + \cos^2 2x - \cos 2x + 2\cos^2 2x - \cos^3 2x) \, dx$$

$$= \frac{1}{8} \int \left(1 - 3\cos 2x + 3 \left[\frac{1 + \cos 4x}{2} \right] - \cos 2x - [1 - \sin^2 2x] \right) \, dx$$

$$= \frac{1}{8} \int \left(\frac{5}{2} - 4\cos 2x + \frac{3\cos 4x}{2} + \cos 2x - \sin^2 2x \right) \, dx$$

$$= \frac{1}{8} \left[\frac{5x}{2} + \frac{2\sin 2x}{2} + \frac{3\sin 4x}{8} + \frac{\sin^3 2x}{6} \right] + C$$

2) $\int \cos^4 x \sin^3 x \, dx$

$\sin^3 x = \text{odd}$

$$u = \cos x$$

$$\frac{du}{dx} = -\sin x$$

$$dx = -\frac{du}{\sin x}$$

$$\text{and } \sin^2 x + \cos^2 x = 1$$

$$\sin^2 x = 1 - \cos^2 x$$

$$= \int u^4 \sin x \cdot \sin^2 x \cdot \frac{-du}{\sin x}$$

$$= \int u^4 \cdot (1 - \cos^2 x) \cdot -du$$

$$= -\int u^4 (1 - u^2) \cdot du$$

$$= -\int (u^4 - u^6) du$$

$$= \int (u^6 - u^4) du$$

$$= \left[\frac{u^7}{7} - \frac{u^5}{5} \right] + C$$

$$= \frac{(\cos x)^7}{7} - \frac{(\cos x)^5}{5}$$

3 $\int \cos x \sin^3 x$

Solution

$$u = \cos x$$

$$\frac{du}{dx} = -\sin x$$

$$du = -\sin x dx$$

$$-du = \sin x dx \quad dx = \frac{-du}{\sin x}$$

$$= \int u \cdot \sin^3 x \cdot \frac{-du}{\sin x}$$

$$= -\int u \cdot \sin^2 x \cdot du$$

$$= -\int u \cdot (1 - \cos^2 x) \cdot du$$

$$= -\int u(1 - u^2) \cdot du$$

$$= -\int (u - u^3) du$$

$$= \int (u^3 - u) du$$

$$= \left[\frac{u^4}{4} - \frac{u^2}{2} \right] + C = \frac{(\cos x)^4}{4} - \frac{(\cos x)^2}{2}$$