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MAT 104 ASSIGNMENT

$$\begin{aligned} 1. \int \sin^6 x \, dx &= \int \sin^2 x \cdot \sin^4 x \\ &= \int \left(\frac{1 - \cos 2x}{2} \right) \cdot \left(\frac{1 - \cos 2x}{2} \right)^2 \\ &= \int \frac{1 - \cos 2x}{2} \cdot \frac{1 - \cos 2x}{2} \cdot \frac{1 - \cos 2x}{2} \\ &= \frac{1}{8} \int (1 - \cos 2x) (1 - 2\cos 2x + \cos^2 2x) \\ &= \frac{1}{8} \int 1 - 3\cos 2x + 3\cos^2 2x - \cos^3 2x \\ &= \frac{1}{8} \int 1 - 3\cos 2x + 3 \left[\frac{1 + \cos 4x}{2} \right] - \cos 2x [1 - \sin^2 2x] \\ &= \frac{1}{8} \int 1 - 3\cos 2x + \frac{3}{2} + \frac{3\cos 4x}{2} - \cos 2x + \cos 2x \sin^2 2x \\ &= \frac{1}{8} \int \frac{5}{2} - 4\cos 2x + \frac{3\cos 4x}{2} + \cos 2x \sin^2 2x \\ &= \frac{1}{8} \left[\frac{5}{2}x - \frac{4\sin 2x}{2} + \frac{3\cos 4x}{8} + \frac{\sin^3 2x}{6} \right] + C \\ &= \frac{1}{8} \left[\frac{5}{2}x - 2\sin 2x + \frac{3\cos 4x}{8} + \frac{\sin^3 2x}{6} \right] + C \end{aligned}$$

$$2. \int \cos^4 x \sin^3 x$$

$$u = \cos x$$

$$\frac{du}{dx} = -\sin x$$

$$dx = -\frac{du}{\sin x}$$

$$\begin{aligned} \int \cos^4 x \sin^3 x &= \int u^4 \cdot \sin x \cdot \sin^2 x \cdot -\frac{du}{\sin x} \\ &= -\int u^4 \cdot (1 - \cos^2 x) \\ &= -\int u^4 (1 - u^2) \end{aligned}$$

$$\begin{aligned}
&= - \int u^4 - u^6 \\
&= - \left[\frac{u^5}{5} - \frac{u^7}{7} \right] + C \\
&= \frac{u^7}{7} + \frac{u^5}{5} + C
\end{aligned}$$

∴

$$\int \cos^4 x \sin^3 x \, dx = \frac{\cos^7 x}{7} - \frac{\cos^5 x}{5} + C$$

$$3) \int \cos x \sin^3 x \, dx$$

$$u = \sin x$$

$$\frac{du}{dx} = \cos x$$

$$dx = \frac{du}{\cos x}$$

$$\begin{aligned}
\int \cos x \sin^3 x \, dx &= \int \cos x \cdot u^3 \frac{du}{\cos x} \\
&= \int u^3 du
\end{aligned}$$

$$\int \cos x \sin^3 x \, dx = \left[\frac{u^4}{4} \right] + C$$

$$= \frac{\sin^4 x}{4} + C$$