

AULE GENEVIEVE MOURSHIMA

19/MH301/108

MEDICINE AND SURGERY

MATH 104

MBBS ASSIGNMENT

Integrate the following functions

i)  $\sin^6 x$

Using the formula

$$\int \sin^n(x) dx = -\frac{\sin^{n-1}(x) \cos(x)}{n} + \frac{n-1}{n} \int \sin^{n-2}(x) dx$$

$$\int \sin^6 x dx = \frac{-1}{6} \sin^5 x \cos x + \frac{5}{6} \int \sin^4 x dx$$

$$= \frac{-1}{6} \sin^5 x \cos x + \frac{5}{6} \left( \frac{-1}{4} \sin^3 x \cos x + \frac{3}{4} \int \sin^2 x dx \right)$$

$$\text{Using } \sin^2 x = \frac{1 - \cos 2x}{2}$$

$$= \frac{-1}{6} \sin^5 x \cos x + \frac{5}{6} \left( \frac{-1}{4} \sin^3 x \cos x + \frac{3}{4} \int \frac{1 - \cos 2x}{2} dx \right)$$

$$= \frac{-1}{6} \sin^5 x \cos x + \frac{5}{6} \left( \frac{-1}{4} \sin^3 x \cos x + \frac{3}{4} \cdot \frac{1}{2} \int (1 - \cos 2x) dx \right)$$

$$= \frac{-1}{6} \sin^5 x \cos x + \frac{5}{6} \left[ \frac{-1}{4} \sin^3 x \cos x + \frac{3}{8} \left( x - \frac{\sin 2x}{2} \right) \right]$$

$$= \frac{-1}{6} \sin^5 x \cos x + \frac{5}{6} \left[ \frac{-1}{4} \sin^3 x \cos x + \frac{3x}{8} - \frac{3 \sin 2x}{16} \right]$$

$$= \frac{-\sin^5 x \cos x}{6} - \frac{5 \sin^3 x \cos x}{24} + \frac{5x}{16} - \frac{5 \sin 2x}{32} + C$$

$$\therefore \int \sin^6 x dx = -\frac{\sin^5 x \cos x}{6} - \frac{5 \sin^3 x \cos x}{24} + \frac{5x}{16} - \frac{5 \sin 2x}{32} + C$$



