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MATRIC NO: 19/MSU/41

DEPARTMENT: MBBS

MAT 104

ASSIGNMENT

1. $\sin^2 x$

$$\sin^2 x = 1 - \cos^2 x$$

$$\int (1 - \cos^2 x)^3 dx$$

$$\int (1 - \cos^2 x)^2 (1 - \cos^2 x) dx$$

$$\int (1 - 2\cos^2 x + \cos^4 x)(1 - \cos^2 x) dx$$

$$\int (1 - 3\cos^2 x + 3\cos^4 x - \cos^6 x) dx$$

$$\text{Using } \cos^2 x = \frac{1}{2}(1 + \cos 2x)$$

$$\int \left(1 - 3\left(\frac{1}{2}(1 + \cos 2x)\right) + 3\left(\frac{1}{4}(1 + \cos 2x)^2\right) - \left(\frac{1}{8}(1 + \cos 2x)^3\right) \right) dx$$

$$\int \left(1 - \frac{3}{2}(1 + \cos 2x) + \frac{3}{4}(1 + \cos 2x)^2 - \frac{1}{8}(1 + \cos 2x)^3 \right) dx$$

$$\int \left(1 - \frac{3}{2} - \frac{3}{2}\cos 2x + \frac{3}{4}(1 + 2\cos 2x + \cos^2 2x) - \frac{1}{8}(1 + 3\cos 2x + 3\cos^2 2x + \cos^3 2x) \right) dx$$

$$\int \left(1 - \frac{3}{2} - \frac{3}{2}\cos 2x + \frac{3}{4} + \frac{3}{2}\cos 2x + \frac{3}{4}\cos^2 2x - \frac{1}{8} - \frac{3}{8}\cos 2x - \frac{3}{8}\cos^2 2x - \frac{1}{8}\cos^3 2x \right) dx$$

$$\int \left(-\frac{1}{2} - \frac{3}{8}\cos 2x + \frac{3}{4} + \frac{3}{2}\cos 2x + \frac{3}{4}\cos^2 2x - \frac{1}{8} - \frac{3}{8}\cos 2x - \frac{3}{8}\cos^2 2x - \frac{1}{8}\cos^3 2x \right) dx$$

$$\int \left(\frac{1}{8} + \frac{3}{4}\cos^2 2x - \frac{3}{8}\cos 2x - \frac{3}{8}\cos^2 2x - \frac{1}{8}\cos^3 2x \right) dx$$

$$\int \left(\frac{1}{8} + \frac{3}{4}(1 + \cos 2x) - \frac{3}{8}\cos 2x - \frac{3}{8}(1 + \cos 2x) - \frac{1}{8}(\cos^2 2x + \cos 2x) \right) dx$$

$$\int \left(\frac{1}{8} + \frac{3}{8} + \frac{3}{8}\cos 2x - \frac{3}{8}\cos 2x - \frac{3}{16} - \frac{3}{16}\cos 2x - \frac{1}{8}(\cos^2 2x + \cos 2x) \right) dx$$

$$\int \left(\frac{5}{16} + \frac{3}{8}\cos 2x - \frac{3}{8}\cos 2x - \frac{3}{16}\cos 2x - \frac{1}{8}(\cos^2 2x + \cos 2x) \right) dx$$

$$\int \left(\frac{5}{16} + \frac{3}{8}\cos 2x - \frac{3}{8}\cos 2x - \frac{3}{16}\cos 2x - \frac{1}{8}(1 - \sin^2 2x)(\cos 2x) \right) dx$$

$$\int \left(\frac{5}{16} + \frac{3}{8}\cos 2x - \frac{3}{8}\cos 2x - \frac{3}{16}\cos 2x - \frac{1}{8}(1 - \sin^2 2x)(\cos 2x) \right) dx$$

$$\int \left(\frac{5}{16} + \frac{3}{8}\cos 2x - \frac{3}{8}\cos 2x - \frac{3}{16}\cos 2x \right)$$



16
16
 $\frac{dy}{2}$
 $\frac{1}{2} \int 1 - \sin^2 2x$
 $\frac{1}{2} \int (1 - \sin^2 2x)$
 $\frac{1}{2} \int (1 - \sin^2 2x)$
 $\frac{1}{2} \int (1 - \sin^2 2x)$

$$= 5x + 3 \sin 4x - 3 \sin 2x - 3 \sin 4x$$

$$16 \quad 32 \quad 16 \quad 64$$

Finding $\int (-\sin 2x)(\cos 2x)$

let $y = \sin 2x$

$$\frac{dy}{dx} = 2 \cos 2x$$

$$\frac{1}{2} dy = \cos 2x dx$$

$$\int \frac{1}{2} (-y^2) dy$$

$$= \frac{1}{2} (y - y^3)$$

$$= \frac{y - y^3}{2}$$

$$= \frac{\sin 2x - \sin^3 2x}{2}$$

Partial Fractions

$$= \frac{5x}{16} + \frac{3 \sin 4x}{32} - \frac{3 \sin 2x}{16} - \frac{3 \sin 4x}{64} - \frac{1}{5} \left(\frac{\sin 4x}{2} - \frac{\sin^3 2x}{6} \right) + C$$

$$= \frac{5x}{16} + \frac{3 \sin 4x}{32} - \frac{3 \sin 2x}{16} - \frac{3 \sin 4x}{64} - \frac{\sin 2x}{10} + \frac{\sin^3 2x}{30} + C$$

$$\int \sin^2 x = 60x + 18 \sin 4x - 48 \sin 2x + 45 \sin^3 2x + C \quad 192$$

$$\int \sin^2 x = 60x + 18 \sin 4x - 48 \sin 2x + 45 \sin^3 2x + C \quad 192$$

2. $\int \cos 3x \sin^2 x dx$

let $u = \cos 3x$

$$\frac{du}{dx} = -3 \sin 3x \quad dx = \frac{-du}{3}$$

$$\int \frac{1}{3} u^2 \sin^2 x \cdot \frac{-du}{3}$$

$$= -\frac{1}{9} \int u^2 \sin^2 x du$$

$$\sin^2 x = 1 - \cos^2 x$$

$$= \int u^2 (1 - u^2) du$$

$$= \int u^2 - u^4 du$$

$$= \frac{1}{3} u^3 - \frac{1}{5} u^5 + C$$

$$= \frac{1}{3} \cos^3 3x - \frac{1}{5} \cos^5 3x + C$$



$$= \frac{u^7}{7} - \frac{u^5}{5} + C$$

$$\int \cos^4 x \sin^2 x \, dx = \frac{\cos^4 x}{7} - \frac{\cos^5 x}{5} + C$$

3. $\int \cos x \sin^3 x \, dx$

let $u = \cos x$

$$\frac{du}{dx} = -\sin x$$

$$dx = \frac{-du}{\sin x}$$

$$\int \frac{u \cdot \sin^3 x \cdot (-du)}{\sin x}$$

$$= -\int u \sin^2 x \, du$$

$$= -\int u(1-u^2) \, du$$

$$= -\int (u - u^3) \, du$$

$$= \int (u^3 - u) \, du$$

$$= \frac{u^4}{4} - \frac{u^2}{2} + C$$

$$\int \cos x \sin^3 x \, dx = \frac{\cos^4 x}{4} - \frac{\cos^2 x}{2} + C$$