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DEPARTMENT: MBSS

MAT 104

ASSIGNMENT

1. $\sin^3 x$

$$\sin^3 x = 1 - \cos^2 x$$

$$\int (1 - \cos^2 x)^3 dx$$

$$\int (1 - \cos^2 x)^2 (1 - \cos^2 x) dx$$

$$\int (1 - 2\cos^2 x + \cos^4 x)(1 - \cos^2 x) dx$$

$$\int (1 - 3\cos^2 x + 3\cos^4 x - \cos^6 x) dx$$

$$\text{Using } \cos^2 x = \frac{1}{2}(1 + \cos 2x)$$

$$\int \left(1 - 3\left(\frac{1}{2}(1 + \cos 2x)\right) + 3\left(\frac{1}{4}(1 + \cos 2x)^2\right) - \frac{1}{8}(1 + \cos 2x)^3 \right) dx$$

$$\int \left(1 - \frac{3}{2}(1 + \cos 2x) + \frac{3}{4}(1 + \cos 2x)^2 - \frac{1}{8}(1 + \cos 2x)^3 \right) dx$$

$$\int \left(1 - \frac{3}{2} - \frac{3}{2}\cos 2x + \frac{3}{4}(1 + 2\cos 2x + \cos^2 2x) - \frac{1}{8}(1 + 3\cos 2x + 3\cos^2 2x + \cos^3 2x) \right) dx$$

$$\int \left(1 - \frac{3}{2} - \frac{3}{2}\cos 2x + \frac{3}{4} + \frac{3}{2}\cos 2x + \frac{3}{4}\cos^2 2x - \frac{1}{8} - \frac{3}{8}\cos 2x - \frac{3}{8}\cos^2 2x - \frac{1}{8}\cos^3 2x \right) dx$$

$$\int \left(1 - \frac{3}{2} + \frac{3}{4} - \frac{3}{2}\cos 2x + \frac{3}{2}\cos 2x + \frac{3}{4}\cos^2 2x - \frac{1}{8} - \frac{3}{8}\cos 2x - \frac{3}{8}\cos^2 2x - \frac{1}{8}\cos^3 2x \right) dx$$

$$\int \left(1 + \frac{3}{4}\cos^2 2x - \frac{3}{8}\cos 2x - \frac{3}{8}\cos^2 2x - \frac{1}{8}\cos^3 2x \right) dx$$

$$\int \left(1 + \frac{3}{4}(1 + \cos 4x) - \frac{3}{8}\cos 2x - \frac{3}{8}(1 + \cos 4x) - \frac{1}{8}(\cos^3 2x + \cos 2x) \right) dx$$

$$\int \left(1 + \frac{3}{4} + \frac{3}{4}\cos 4x - \frac{3}{8}\cos 2x - \frac{3}{8} - \frac{3}{8}\cos 2x - \frac{1}{8}(\cos^3 2x + \cos 2x) \right) dx$$

$$\int \left(\frac{5}{4} + \frac{3}{4}\cos 4x - \frac{3}{8}\cos 2x - \frac{3}{8}\cos 2x - \frac{1}{8}(\cos^3 2x + \cos 2x) \right) dx$$

$$\int \left(\frac{5}{4} + \frac{3}{4}\cos 4x - \frac{3}{8}\cos 2x - \frac{3}{8}\cos 2x - \frac{1}{8}(1 - \sin^2 2x)(\cos 2x) \right) dx$$

$$\int \left(\frac{5}{4} + \frac{3}{4}\cos 4x - \frac{3}{8}\cos 2x - \frac{3}{8}\cos 2x - \frac{1}{8}(1 - \sin^2 2x)(\cos 2x) \right) dx$$

$$\int \left(\frac{5}{4} + \frac{3}{4}\cos 4x - \frac{3}{8}\cos 2x - \frac{3}{8}\cos 2x \right)$$

$$= 5x + 2 \sin^2 x - 2 \sin^2 x - 3 \sin^2 x$$

$$16 \quad 32 \quad 16 \quad 64$$

Finishing $\int (1 - \sin^2 x) \cos^2 x dx$

let $y = \sin x$

$\frac{dy}{dx} = \cos x$

$\frac{1}{2} dy \cos^2 x dx$

$\int \frac{1}{2} (1 - y^2) dy$

$$= \frac{1}{2} (\log y^2)$$

$$= \frac{y}{2} - \frac{y^3}{6}$$

$$= \frac{2 \sin x - \sin^3 x}{6}$$

Add everything

$$= \frac{5x}{16} + \frac{2 \sin^2 x}{32} - \frac{2 \sin^2 x}{32} - \frac{3 \sin^2 x}{64} - \frac{11}{5} \left(\frac{\sin^2 x}{2} - \frac{\sin^3 x}{6} \right) + C$$

$$= \frac{5x}{16} + \frac{2 \sin^2 x}{32} - \frac{2 \sin^2 x}{32} - \frac{3 \sin^2 x}{64} - \frac{\sin^2 x}{10} + \frac{\sin^3 x}{6} + C$$

$$\int \sin^4 x = 60x + 18 \sin^2 x - 36 \sin^4 x - 9 \sin^6 x - 12 \sin^8 x + 4 \sin^{10} x + C$$

$$\int \sin^5 x = 60x + 9 \sin^2 x - 48 \sin^4 x + 4 \sin^6 x + C \quad 156x \quad 60x$$

2. Kosin^2 dx

let $u = \cos x$

$$\frac{du}{dx} = -\sin x \quad dx = -\frac{du}{\sin x}$$

$$\int u^2 \sin^2 x - \frac{du}{\sin x}$$

$$- \int u^2 \sin^2 x du$$

$$\sin^2 x = 1 - \cos^2 x$$

$$- \int u^2 (1 - u^2) du$$

$$- \int u^2 - u^4 du$$

$$= \int u^4 - u^2 du$$