

1

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Civil Engineering

Flow rate (Q) = 10 dm³/min
Pressure change (ΔP) = 12 bar
Speed (N) = 1500 rpm
Nominal displacement = 10 cm³/rev
Torque input (T) = 12.5 N-m

i) Ideal flow rate = nominal Displacement × Speed
= 10 cm³/rev × 1500 rpm
= 15000 cm³/min = 15 dm³/min
Volumetric efficiency = Actual flow / ideal flow
= 10 / 15 = 0.6667 or 66.67%

$$ii) Q = \frac{10 \times 10^{-3} \text{ m}^3/\text{sec}}{60} = 16.7 \times 10^{-5} \text{ m}^3/\text{sec}$$

$$\Delta P = 12 \times 10^5 \text{ N/m}^2$$

$$\text{Fluid power} = \Delta P \times Q = 16.7 \times 10^{-5} \text{ m}^3/\text{sec} \times 12 \times 10^5 \text{ N/m}^2 = 200 \text{ watts}$$

$$\text{Shaft power} = \frac{2\pi NT}{60} = \frac{2\pi \times 1500 \times 12.5}{60} = 1963.5 \text{ watts}$$

$$\text{Overall Efficiency} = \frac{F.P.}{S.P.} = \frac{200}{1963.5} = 0.102 \text{ or } 10.2\%$$

Summary: there we can see that shaft power almost 10 times of fluid power can be either increase by the change in pressure or discharge

3

Nominal displacement = 50 cm³/rev
Pressure change (ΔP) = 100 bar
Shaft Power = 15 kilo watts = 15000
Overall Efficiency = ??
Volumetric Efficiency = ??
Flow rate (Q) = 35 dm³/min
Speed (N) = 850 rpm

$$\text{ideal flow rate} = \text{Nominal displacement} \times \text{speed} \\ = 50 \text{ cm}^3/\text{rev} \times 850 \text{ rpm} \\ = 42500 \text{ cm}^3/\text{min} = 42.5 \text{ dm}^3/\text{min}$$

$$\text{Volumetric efficiency} = \frac{\text{Actual flow}}{\text{ideal flow}} \\ = \frac{35}{42.5} = 0.8235 \text{ or } 82.35\%$$

$$ii) Q = \frac{35 \times 10^{-3} \text{ m}^3/\text{sec}}{60} = 58.3 \times 10^{-5} \text{ m}^3/\text{sec}$$

$$\Delta P = 100 \times 10^5 \text{ N/m}^2$$

$$\text{Fluid power} = \Delta P \times Q = \cancel{58.3 \times 10^{-5} \text{ m}^3/\text{sec} \times 100 \times 10^5} \\ = 5830 \text{ watts}$$

$$\text{Shaft power} = 15000 \text{ watts}$$

$$\text{Overall Efficiency} = \frac{\text{Fluid power}}{\text{Shaft Power}} = \frac{5830}{15000} = 0.3886 \text{ or } 38.86\%$$

(4)

$$H = 240\text{m}$$

$$Q = 0.013\text{m}^3/\text{s}$$

$$V = 66\text{m/sec}$$

$$\begin{aligned} a) \text{ Power of Jet } (P_{jet}) &= \frac{1}{2} \rho v^2 \text{ Jet} \\ &= \frac{1}{2} \rho Q v^2 \text{ Jet} \\ &= \frac{1}{2} \times 1000 \times 0.013 \times 66^2 \text{ watt} \\ &= 28314 \\ &= 28.314 \text{ kilowatts} \end{aligned}$$

$$\begin{aligned} b) \text{ Power supplied by } (P_{res}) &= \rho g h \\ \text{reservoir} & \quad v = \rho Q g h \\ &= 1000 \times 0.013 \times 9.81 \times 240 \text{ watt} \\ &= 30607.2 \\ &= 30.6072 \text{ kilowatt} \end{aligned}$$

$$\begin{aligned} c) \text{ Head used to overcome losses} \\ \text{(HF)} &= H - \frac{v_{jet}^2}{2g} \\ &= 240 - \frac{66^2}{2 \times 9.81} \\ &= 17.98\text{m} \end{aligned}$$

$$\begin{aligned} d) \text{ Efficiency of pipeline \& nozzle} &= \frac{P_{jet}}{P_{res}} \times 100 \\ &= \frac{28.314}{30.6072} \times 100 = 92.51\% \end{aligned}$$

(5)

$$\begin{aligned} Z_1 &= 360\text{cm} = 3.6\text{m} \\ Q_1 &= 220\text{liters} = 0.22\text{m}^3/\text{s} \\ v_1 &= 7\text{m/s} \\ \text{Power of jet} &= \rho Q_1 H \\ \text{where } \rho &= 0.87 \times 1000 = 870\text{kg/m}^3 \\ g &= 9.81\text{m/s}^2 \\ Q &= (220 \times 10^{-3})/\text{s} \\ H &= Z_1 + \frac{v_1^2}{2g} + \frac{Q_1^2}{2g} \\ &= 0 + \frac{0}{2 \times 9.81} + \frac{(0.22)^2}{2 \times 9.81} \\ &= 0.02491 \times 100 \\ &= 2.49\text{J} \\ \text{Power} &= 870 \times 9.81 \times 220 \times 10^{-3} \times 2.49\text{J} \\ &= 47921\text{ watts} \\ \text{Power supplied from reservoir} \\ H &= Z_1 + \frac{v^2}{2g} + \frac{Q^2}{2g} \\ &= 3.6 + \frac{0}{2 \times 9.81} + \frac{Q^2}{2 \times 9.81} \\ &= 3.6 + \frac{Q^2}{2 \times 9.81} \\ \text{Power} &= 870 \times 9.81 \times 220 \times 10^{-3} \times 3.6 \\ &= 5762394\text{ W} \end{aligned}$$

Head used to overcome the loss
= Power loss / $\rho \times v$
= $(5762394 - 47921) / (1000 \times 9.81) \times 10^{-3}$

Efficiency = $\frac{\text{Power of jet}}{\text{Power of reservoir}} \times 100$

(6)

$$\begin{aligned} \text{Power} &= \text{velocity} \times \text{force} \\ \text{velocity} &= 799.6 \\ \text{force} &= \rho v^2 \\ v &= \text{velocity of steam} \\ \rho &= \text{density of water (1000 kg/m}^3\text{)} \\ M &= \rho v \\ v &= \sqrt{\frac{2P}{\rho}} = \sqrt{\frac{2 \times 9.9120}{1979.99\text{m/s}}} \\ P &= \rho v^2 \frac{v}{2} \\ \text{Power} &= 1000 \times \frac{v^3}{2} \times (1979.99\text{m/s} \times 9.81\text{m/s}^2 \times 20\text{m}) \\ &= 1000 \times \frac{v^3}{2} \times 2.5 \times 10^{-2} \times 1979.99 \times 9.81 \times 20 \\ &= 30478.03\text{ W} \\ \text{Power} &= 30478.03\text{ W} \end{aligned}$$

(7)

Downe (A): 0.3m
 $A_1 = \frac{\pi}{4} \times 0.3^2$
 $A_2 = 0.01665 \text{ m}^2$

Throat diameter (D₂): 2m
 $A_2 = \frac{\pi}{4} \times 0.2^2$

$A_3 = 0.03141 \text{ m}^2$, Coefficient of discharge (Cd) = 0.97
Specific weight of gas (γ) = 19.62 N/m³
Density of gas (ρ_g) = $\frac{19.62}{9.81}$

$$\rho_g = 2 \text{ kg/m}^3$$

Razordine method difference (h) = $\frac{5z}{3g} (1 - \frac{z_1}{z_2})$

$$= 0.06 \times \left(\frac{5 \times 10}{3} - 1 \right)$$

$$h = 29.96 \text{ m}$$

∴ Volume flow (Q) = $C_d \sqrt{A_1 - A_2} \sqrt{2gh}$
 $\sqrt{A_1^2 - A_2^2}$

$$= 0.97 \times 0.01665 \times \sqrt{2 \times 9.81 \times 29.96} \times \sqrt{(0.03141)^2 - (0.01665)^2}$$

$$Q = 0.81599 \text{ m}^3/\text{s}$$

(8)

$A_1 = \frac{\pi}{4} \times 0.1^2 = \frac{\pi}{4} \times (0.15)^2 = 0.01816 \text{ m}^2$
 $A_2 = \frac{\pi}{4} \times 0.2^2 = \frac{\pi}{4} \times (0.10)^2 = 4.5365 \times 10^{-3} \text{ m}^2$

$$Q = C_d A_1 \sqrt{2gh} = C_d A_2 \sqrt{2gh}$$

$$= 0.97 \times 0.01816 \times \sqrt{2 \times 9.81 \times 1.933} = 4.5365 \times 10^{-3} \times \sqrt{2 \times 9.81 \times 1.933}$$

$$Q = 0.01924 \text{ m}^3/\text{s}$$

∴ $h = \frac{(A_1^2 - A_2^2)}{3g} = \frac{15170}{3 \times 9.81 \times 4.5365 \times 10^{-3}} = 1.933 \text{ m}$

$$Q = C_d \frac{A_1 A_2}{\sqrt{A_1^2 - A_2^2}} \sqrt{2gh}$$

$$Q = 0.97 \times \frac{0.01816 \times 4.5365 \times 10^{-3} \times \sqrt{2 \times 9.81 \times 1.933}}{\sqrt{(0.01816)^2 - (4.5365 \times 10^{-3})^2}}$$

$$Q = 0.02196 \text{ m}^3/\text{s}$$

(9)

$d_1 = 300 \text{ mm}$
 $d_2 = 300 \text{ mm}$
 $A_1 = \frac{\pi}{4} \times 0.3^2 = 0.0707 \text{ m}^2$
 $A_2 = \frac{\pi}{4} \times 0.3^2 = 0.0707 \text{ m}^2$
 $Q = 60 \text{ l/s} = 60 \times 10^{-3} \text{ m}^3/\text{s}$

$Z_1 = 10 \text{ m}$, $Z_2 = 6 \text{ m}$, $P_1 = ?$, $P_2 = ?$, $P_2 = 4000 \text{ N/m}^2$

$$Q = VA$$

$$V_1 A_1 = Q \Rightarrow V_1 = \frac{Q}{A_1} = \frac{60 \times 10^{-3}}{0.0707} = 0.8485 \text{ m/s}$$

$$V_2 = \frac{Q}{A_2} = 0.8485 \text{ m/s}$$

$$Q = 40 \text{ m}^3/\text{s}$$

$$V_1 = \frac{Q}{A_1} = \frac{40 \times 10^{-3}}{0.0707} = 0.565 \text{ m/s}$$

$$V_2 = \frac{Q}{A_2} = \frac{40 \times 10^{-3}}{0.0707} = 0.565 \text{ m/s}$$

$$Z_1 + \frac{P_1}{\rho} + \frac{V_1^2}{2g} = Z_2 + \frac{P_2}{\rho} + \frac{V_2^2}{2g}$$

$$Z_1 + \frac{P_1}{\rho g} + \frac{V_1^2}{2g} = Z_2 + \frac{P_2}{\rho g} + \frac{V_2^2}{2g}$$

$$10 + \frac{P_1}{9810} + \frac{(0.565)^2}{2 \times 9.81} = 6 + \frac{4000}{9810} + \frac{(0.565)^2}{2 \times 9.81}$$

$$50.79 = P_2 + 6.26 \times 10^3$$

$$P_2 = 50.79 - 626 = 4452.21 \text{ N/m}^2$$

(10)

Calculate the head

$$h = y \left[\frac{\rho_h}{\rho_f} - 1 \right]$$

$$= 0.17 \left[\frac{13.6}{1.026} - 1 \right]$$

$$h = 2.0834$$

 ρ_m = density of mercury ρ_f = density of flowing fluid y → manometric reading

Calculate the velocity of the submarine

$$v = \sqrt{2gh}$$

$$= \sqrt{2 \times 9.81 \times 2.0834}$$

$$= 6.393 \text{ m/sec}$$

(2)

Flow rate (Q) = 35 dm³/minPressure change (ΔP) = 100 bar

Overall Efficiency = 87%

$$\text{Shaft power} = \frac{2\pi NI}{60}$$

Fluid = $\Delta p \times Q$

$$Q = \frac{35 \times 10^{-3}}{60} \text{ m}^3/\text{sec}$$

$$= 58.3 \times 10^{-5} \text{ m}^3/\text{sec}$$

Fluid power

$$\Delta P = 100 \times 10^5 \text{ N/m}^2$$

$$= 58.3 \times 10^{-3} \times 100 \times 10^5$$

$$= 5830 \text{ watts}$$

$$\text{Overall Efficiency} = \frac{\text{Fluid power}}{\text{Shaft power}}$$

$$0.87 = \frac{5830}{\text{Shaft power}}$$

$$\text{Shaft power} = \frac{5830}{0.87} = 6701.14 \text{ watts}$$

Balogun's fluid assignment