

LINEAR TRANSFORMATION

Let P and Q be real vector spaces (their dimensions can be different) and let R be a function with domain P and range in Q (written $R:P \rightarrow Q$)

We say R is a linear transformation if

For all $x, y \in P$, $R(x+y) = R(x) + R(y)$

For all $x \in P, r \in R$, $R(rx) = rR(x)$ (R is homogenous)

RANK OF MATRIX

The dimension of the range of a linear transformation is called the RANK

The rank of a linear transformation are related to each other by the equation

$\text{rank} T + \text{multy } T = \text{dim}(\text{domain})$

$$2. \begin{vmatrix} 1 & 4 & 9 \\ 2 & 7 & 5 \\ 8 & 6 & 3 \end{vmatrix}$$

Det (x)=|x|

$$\text{Det}(x) = 1 \begin{vmatrix} 7 & 5 \\ 6 & 3 \end{vmatrix} - 4 \begin{vmatrix} 2 & 5 \\ 8 & 3 \end{vmatrix} + 9 \begin{vmatrix} 2 & 7 \\ 8 & 6 \end{vmatrix}$$

$$= 1|21-30| - 4|6-40| + 9|12-56|$$

$$= -9 - 4(-34) + 9(-44)$$

$$= -9 - 132 - 39$$

$$= -537$$

Non singular matrix

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$T: x \rightarrow y$

$X = \{e, f, g, h, i, j, k\}$

$Y = \{2, 4, 6, 8, 10\}$

X	y
e	2
f	4
g	6
h	8
i	10
j	codomain
k	
domain	