

Matric no: 17/ENGO4/024

Department: Electrical/Electronics Eng.

Level: 300 LoL

Question 1

ABUAD Mango Juice factory is serviced by a 415 V, 3-phase, 4-wire 50Hz. This supply powers the main drive motor having an output of 74.6 kW and running on full load at a power factor of 0.7 lagging with an efficiency of 85%. Identify the drive motor type and sketch the motor supply circuit with a direct online starter. Determine the capacitance per phase of the mesh connected capacitor necessary to raise the power factor to (i) unity & (ii) 0.9 lagging. Sketch the phasor diagram using an appropriate scale showing the computed values of currents.

Answer:

(A)

$V = 415\text{V}$ , 3- $\phi$ , 4-wire,  $f = 50\text{Hz}$ ,  $P = 74.6$   
 $P_f = 0.7$ , % eff = 85%  $\therefore V = 415\text{V}$  to star =  $\frac{415}{\sqrt{3}}$   
 $= 239.6$

(B)

i) unity = 1

$$C = \frac{kVAR}{2\pi f V^2}$$

$$\rightarrow kVAR = P * [\tan \text{ actual P.f} - \tan \text{ target P.f}]$$

$$\text{actual P.f} \Rightarrow \cos \theta = 0.7$$

$$\theta = \cos^{-1} 0.7$$

$$= 45.57$$

$$\tan(45.57) = 1.020$$

$$\text{Target P.f} \Rightarrow \cos \theta = 1$$

$$\theta = \cos^{-1} 1 = 0$$

$$\tan 0 = 0$$



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Continuation of No 1

$$\begin{aligned} \text{kVAR} &= 74.6 \times (1.0201 - 0) \\ &= 76.6995 \\ &\approx 76.18 \end{aligned}$$

$$C = 76.16$$

$$\begin{aligned} \frac{2 \times \pi \times 50 \times 239.6^2}{2 \times \pi \times 50 \times 239.6^2} &= 0.00000422 \\ &\approx 42.2 \times 10^{-6} \text{ F} \end{aligned}$$

B) 0.9 lagging

$$\text{actual P.f} = 1.0201$$

$$\text{Target P.f} = \cos \theta = 0.9$$

$$\theta = \cos^{-1}(0.9)$$

$$= 54.16^\circ$$

$$\tan \theta = 0.48$$

$$\text{kVAR} = 74.6 \times (1.0201 - (-0.48))$$

$$= 111.90$$

$$\approx 112$$

$$C = \frac{\text{kVAR}}{2\pi f V}$$

$$\begin{aligned} &= \frac{112}{2 \times \pi \times 50 \times 239.6^2} \\ &= 0.0000062 \\ &= 62 \times 10^{-6} \text{ F} \end{aligned}$$

$$\Rightarrow 6.0000062$$

$$= 62 \times 10^{-6} \text{ F}$$



Question 1

$V = 415$

Na

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Question 2

~~V~~  $V = 415$  V

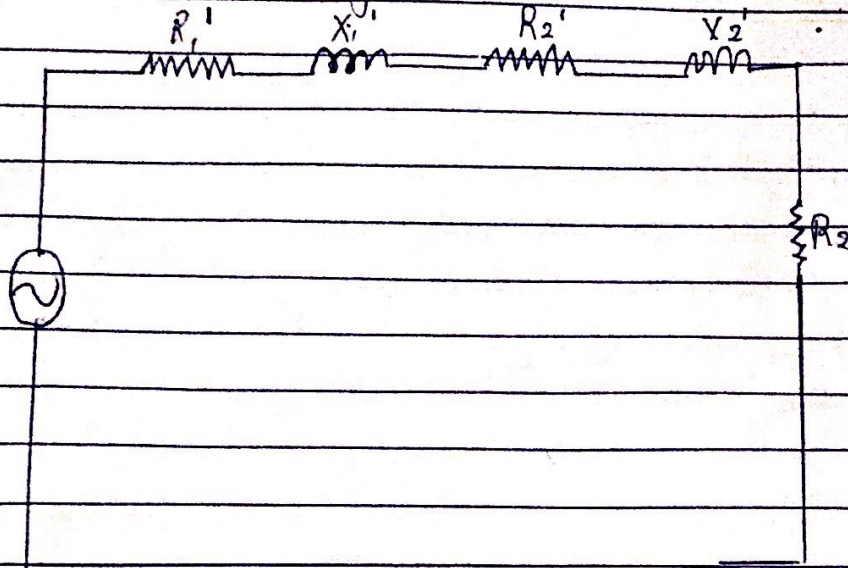
No of poles = 6

$f = 50$  Hz

$k = \frac{5}{6} = 0.83$

$Z_1 = 0.25 + j0.75$  - stator

$Z_2 = 1.173 + j0.52$  - rotor



$$\text{Supply voltage Per phase } V = \frac{415}{\sqrt{3}} = 239.50 \text{ V}$$

referring to rotor

$$R_{02} = (R_2 + k^2 R_1) \\ = (1.173 + \left(\frac{5}{6}\right)^2 \times 0.25)$$

$$R_{02} = 1.341 \Omega$$

$$X_{02} = (X_2 + k^2 X_1) \\ = j(0.52 + \left(\frac{5}{6}\right)^2 \times 0.75) \\ = j1.041$$



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Continuation of No-2

$$Z_{02} = R_{02} + jX_{02}$$
$$= 1.347 + j1.041$$

$$I_{02} = \sqrt{1.347^2 + 1.041^2}$$
$$= 1.7 \text{ A}$$

To find rotor current-

$$I_2 = \frac{E_2}{Z_{02}}$$

Recall that  $E_2 = kV_1$

$$= 239.6 \times 0.85$$
$$= 199.67 \text{ V}$$

$$\therefore I_2 = \frac{199.67}{1.7} = 117.45 \text{ A}$$

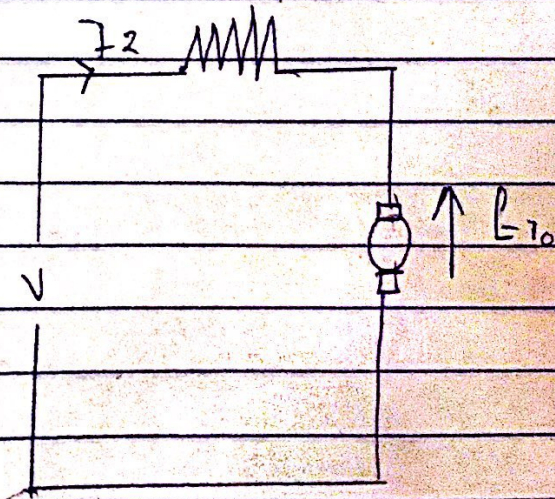
Question 3

$f = 50 \text{ Hz}$ ,  $1/4 \text{ hp}$ ,  $N_2 = 2000 \text{ rpm}$ ,  $15 \mu$  and  $0.25 \text{ A}$

On DC supply

Supply voltage  $= 220 \text{ V}$

Current drawn,  $I = 0.7 \text{ A}$





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Continuation of N/o. 3

On DC supply

$$\text{Supply voltage} = 220 \text{ V}$$

$$\text{Current draws } I = 0.7 \text{ A}$$

$$V - E_b = I_2 * R$$

$$V - [I_2 * R] = E_b$$

$$E_b = 220 - [0.7 * 15]$$

$$= 209.5 \text{ V}$$

Speed on DC

$$N_{dc} = 2000 \text{ rpm}$$

On AC supply

$$\text{Supply voltage} = 220 \text{ V}$$

$$\text{Current draws } I = 0.7 \text{ A}$$

$$\text{Resistance drop} = I_2 * R = 0.7 * 15 = 10.5 \text{ V}$$

$$\text{Reactance voltage drop} = I_2 * X_L$$
$$= 0.7 * 2\pi f L$$

$$\text{where } X_L = j\omega L = 2\pi f L$$

$$= 0.7 * 2\pi * 50 * 0.2$$

$$= 34.98 \text{ V}$$

$E_{ba}$  (from diagram)

$$E_{ba} = \sqrt{V^2 - [X_L]^2} - IR$$

$$= \sqrt{220^2 - 34.98^2} - 10.5 \text{ V}$$

$$= 202.52 \text{ V}$$

Recall speed

$$\frac{N_2}{N_1} = \frac{E_{b2}}{E_{b1}}$$



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$$\therefore \frac{E_{bac}}{E_{bdc}} = \frac{N_{ac}}{N_{dc}}$$

$$\begin{aligned} \therefore N_{ac} &= N_{dc} \times \frac{E_{bac}}{E_{bdc}} \\ &= 2000 \times \frac{202.52 \text{ V}}{209.5 \text{ V}} \end{aligned}$$

$$N_{ac} = 1933.37 \text{ rpm}$$

$$\begin{aligned} \text{ii) Power factor, } \cos \phi &= \frac{E_{bac} + IR}{V} \\ &= \frac{202.52 + 10.5}{220} \\ &\Rightarrow 0.968 \text{ lagging} \end{aligned}$$

$$\begin{aligned} \text{iii) Torque developed } T_w &= \frac{E_{bac} \times I}{\omega} \\ T_{ac} &= \frac{E_{bac} \times I}{\omega} \end{aligned}$$

$\omega$  is speed in rad/s

$$\omega = 2\pi n, \text{ where } n \text{ is speed}$$

$$T_{ac} = \frac{E_{bac} \times I}{2\pi \times \frac{N_{ac}}{60}}$$

$$= \frac{207.52 \times 0.7 \times 60}{2\pi \times 1933.37}$$

$$\approx 0.700 \text{ Nm}$$

iv) Universal Motors