

Department: Elect (Elect Engr.  
Matric No: 17/ENGO4/054

① Unity = 1

$$C = \frac{KVAr}{2\pi f V^2}$$

$$KVAr = Px$$

$$\text{actual P.f} = \cos \theta = 0.7$$

$$\theta = \cos^{-1} 0.7$$

$$= 45.57$$

$$\tan(45.57) = 1.020$$

$$\text{target P.f} \Rightarrow \cos \theta = 1$$

$$\theta = \cos^{-1} 1 = 0$$

$$\tan \theta = 0$$

$$KVAr = 74.6 \times (1.020 - 0)$$

$$= 76.6175$$

$$= 76.1$$

$$C = \frac{76.1}{2\pi \times 50 \times 415^2}$$

$$= 1.4 \times 10^{-6} C$$

ii) 0.9 (lagging)

$$\text{actual P.f} = 1.020$$

$$\text{target P.f} = \cos \theta = -0.9$$

$$\theta = \cos^{-1} (-0.9)$$

$$\theta = 154.16$$

$$\tan \theta = \tan(154.16)$$

$$= -0.48$$

$$KVAr = 74.6 \times (1.020 - (-0.48))$$

$$= 111.90$$

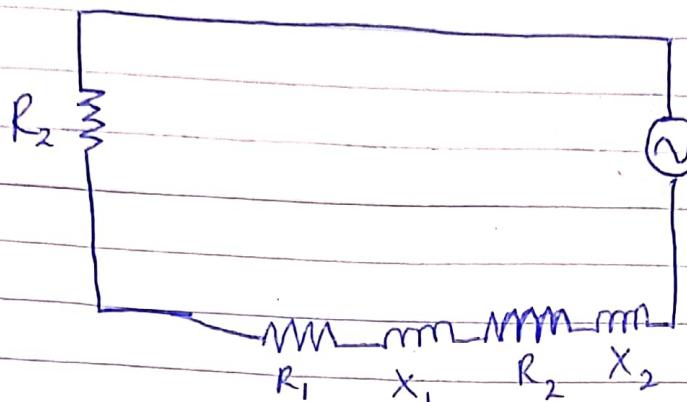
$$\approx 112$$

$$C = \frac{KVAr}{2\pi f V^2} = \frac{112}{2\pi \times 50 \times 415^2}$$

$$= 2.668 \times 10^{-6} C$$

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Matric No: 17/EN604/054

② i)  $Z_1 = 0.25 + j0.75 \dots \text{Star}$   
 $Z_2 = 1.173 + j0.52 \dots \text{rotor}$



Supply Voltage per phase,  $V = \frac{415}{\sqrt{3}} = 239.60V$

Referring to rotor;

$$R_{02} = (R_2 + k^2 R_1)$$
$$= (1.173 + (\frac{5}{6})^2 \times 0.25)$$

$$R_{02} = 1.347 \Omega$$

$$X_{02} = (X_2 + k^2 X_1)$$
$$= j(0.52 + (\frac{5}{6})^2 \times 0.75)$$
$$= 1.041$$

$$Z_{02} = R_{02} + jX_{02}$$
$$= 1.347 + j1.041$$

$$Z_{02} = \sqrt{1.347^2 + 1.041^2}$$
$$= 1.7 \Omega$$

ii) Rotor Current

$$I_2 = \frac{E_2}{Z_{02}}$$

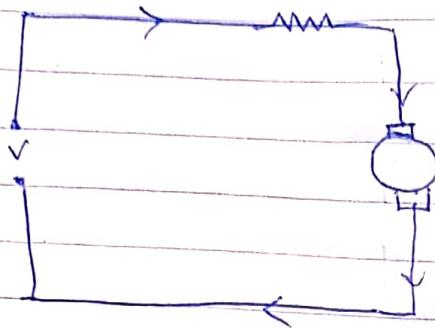
Recall  $\Sigma E_2 = KV$ ,  
 $= 239.6 \times 0.83$   
 $= 199.67 V$

$$\therefore I_2 = \frac{199.67}{1.7} = 117.045 A$$

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(3i)



$$\frac{N_2}{N_1} = \frac{E_{b2}}{E_{b1}}$$

$$\frac{E_{bae}}{E} = \frac{N_{ac}}{N_{dc}}$$

$$\Rightarrow N_{ac} = 2000 \times \frac{202.52V}{209.5V}$$

$$N_{ac} = 1933.37 \text{ rpm}$$

ii) Power factor of the motor

$$\Rightarrow \frac{202.52 \times 10}{220}$$

$$= 0.968 \text{ lagging}$$

iii) Torque developed by the motor

$$= E_{bae} \times I$$

$$\therefore T_{ac} = \frac{E_{bae} \times I}{w}$$

where  $w$  = Speed in rad/s

iv) Universal Motor