

Nwala Nnamdi Chiriburuoma

17/ENG06/059

Mechanical Engineering

300 Level

Electrical Machines II Test

Question 1

$$V = 415V \quad 4\text{-wire} \quad \text{P.F.} = 0.7$$

$$3\text{-}\phi \quad \% \text{ eff} = 85\%$$

$$f = 50 \text{ Hz}$$

$$P = 74.6$$

$$\text{i.) Unity} = 1 \quad \therefore \text{kVAR} = P \times (\tan \text{ of actual p.f.} - \tan \text{ target p.f.})$$

$$C = \frac{\text{kVAR}}{2\pi f V^2}$$

$$\text{actual P.f.} = \cos \theta = 0.7, \quad \theta = \cos^{-1}(0.7) = 45.57$$

$$\tan(45.57) = 1.0201$$

$$\text{target p.f.} = \cos \theta = 1, \quad \theta = \cos^{-1}(1) = 0$$

$$\tan(0) = 0$$

$$\Rightarrow \text{kVAR} = 74.6 \times (1.0201 - 0) = 74.6(1.0201)$$

$$= 76.0995 \approx 76.10$$

$$C = \frac{76.10}{2\pi \times 50 \times 415^2} = 0.0000014 = 1.4 \times 10^{-6} \text{ F}$$

ii) 0.9 lagging

$$\text{actual p.f.} = 1.0201, \quad \text{target P.f.} = \cos \theta$$

$$\text{target P.f.} = \cos \theta = 0.9$$

$$\therefore \cos^{-1}(0.9) = 26.64$$

$$\tan \theta = 0.48$$

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Question 1 cont.

$$\begin{aligned} \text{kVAR} &= 74.6 \times (1.0201 - (-0.48)) \\ &= 111.90 \end{aligned}$$

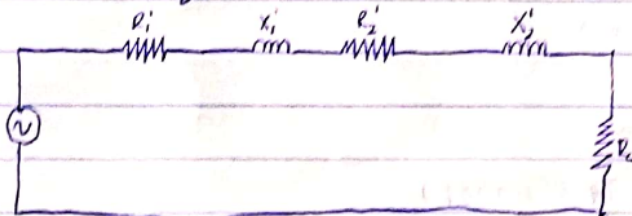
$$\begin{aligned} C &= \frac{\text{kVAR}}{2\pi fV} = \frac{112}{2\pi \times 50 \times 415^2} = 0.00086 \\ &= 8.6 \times 10^{-4} \text{C}_y \end{aligned}$$

Question 2

$$V = 415\text{V}, \text{ No pole} = 6, f = 50\text{Hz}, k = \frac{5}{6} = 0.23$$

$$Z_1 = 0.25 + j0.75 \quad \leftarrow \text{for the stator}$$

$$Z_2 = 1.173 + j0.52 \quad \leftarrow \text{for the rotor}$$



$$\text{Supply of voltage per phase, } V = \frac{415}{\sqrt{3}} = 239.60\text{V}$$

Referring to the rotor

$$R_{02} = (R_2 + k^2 R_1) = (1.173 + (\frac{5}{6})^2 \times 0.25) = 1.347\Omega$$

$$X_{02} = (X_2 + k^2 X_1) = j(0.52 + (\frac{5}{6})^2 \times 0.75) = j1.041$$

$$Z_{02} = R_{02} + jX_{02} = 1.347 + j1.041$$

$$\begin{aligned} Z_{02} &= \sqrt{1.347^2 + 1.041^2} \\ &= 1.7\Omega \end{aligned}$$

To find rotor current

$$\begin{aligned} \therefore I_2 &= \frac{E_2}{Z_{02}} \quad \text{Recall that } E_2 = kV_1 \\ &= \frac{239.6 \times 0.85}{1.7\Omega} \\ &= 1.79.67\text{A} \end{aligned}$$

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Question 2 Cont.

$$\therefore I_2 = \frac{199.67}{1.7} = 117.45 \text{ A}$$

Question 3.

$$f = 50 \text{ Hz}, \quad I = 0.7 \text{ A}, \quad R = 15 \Omega$$

$$N = 1000 \text{ rpm (dc)}, \quad V = 220 \text{ V}, \quad L = 0.25 \text{ H}$$

$$\begin{aligned} E_{dc} &= V - IR \\ &= 220 - (0.7 \times 15) \\ &= 209.5 \text{ V} \end{aligned}$$

$$\begin{aligned} E_{ac} &= \sqrt{V^2 - (I \times L)^2} - IR \\ &= 1 \times L = 0.7 \times 2 \times \pi \times 50 \times 0.25 \\ &= 54.98 \text{ V} \end{aligned}$$

$$IR = 0.7 \times 15 = 10.5 \text{ V}$$

$$\begin{aligned} \therefore E_{ac} &= \sqrt{V^2 - (I \times L)^2} - IR \\ \Rightarrow \sqrt{(220)^2 - (54.98)^2} - 10.5 \\ &= 213.62 - 10.5 \\ &= 202.52 \text{ V} \end{aligned}$$

i) Speed of motor

$$N_{ac} = E_{ac} \quad N_{ac} = \frac{2000 \times 202.52}{209.5}$$

$$\begin{aligned} N_{ac} &= \frac{202.52}{209.5} \quad \therefore N_{ac} = 1933.37 \text{ rpm} \\ 2000 & \quad 209.5 \end{aligned}$$

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Question 3 cont.

ii) Power factor

$$pf = \frac{E + IR}{V} = \frac{202.52 + 10.5}{220} = 0.97$$

iii) Torque developed

$$T = \frac{EI}{2\pi \times 60} = \frac{202.52 \times 0.7}{2\pi \times 1933.37/60}$$

$$= 0.7 \text{ Nm}$$

iv) Universal Motor