

Question 1:

ABUAD mango Juice Factory is serviced by a 415V, 3-phase, 4-wire 50Hz. This supply powers the main drive motor having an output of 74.6 kW and running on full load at a power factor of 0.7 lagging with an efficiency of 85%.

Identify the drive motor type and sketch the motor-supply circuit with a direct-online starter.

Determine the capacitance per phase of a mesh-connected capacitor necessary to raise the power factor to

(i) Unity

(ii) 0.9 lagging.

Answers

NOTE: $V = 415V$, $f = 50Hz$, $P.F. = 0.7$,
3- ϕ , 4-wire, $P = 74.6$, $\% \text{ ef} = 85\%$

① unity $\Rightarrow T$

$$C = \frac{kVAR}{2\pi f V^2}$$

$$\therefore kVAR = P \times (\tan \text{ actual P.F.} - \tan \text{ target P.F.})$$

$$\therefore \text{actual P.F.} \Rightarrow \cos \theta = 0.7$$

$$\theta = \cos^{-1} 0.7$$

$$\therefore = 45.57$$

$$\tan (45.57) = 1.0201$$

$$\text{target P.F.} \Rightarrow \cos \theta = 1$$

$$\theta = \cos^{-1} 1 = 0$$

$$\tan 0 = 0$$

$$\therefore kVAR = 74.6 \times (1.0201 - 0)$$

$$= 76.0975$$

$$\therefore \approx 76.10$$

$$C = \frac{76.10}{2 \times \pi \times 50 \times 415^2}$$

$$= 0.000004$$

$$\therefore \approx 1.4 \times 10^{-6} \text{ C} //$$

ii 0.9 Lagging

when actual p.f = 1.0201

$$\text{target p.f} = \cos \theta = -0.9$$

$$\theta = \cos^{-1}(-0.9)$$

$$= 154.16$$

$$\therefore \tan \theta = -0.48.$$

$$\text{KVAR} = 74.6 \times (1.0201 - (-0.48))$$

$$= 111.90$$

$$\approx 112$$

$$C = \frac{\text{KVAR}}{2 \pi F V}$$

$$= \frac{112}{2 \times \pi \times 50 \times 415^2}$$

$$= 0.00086$$

$$\approx 8.6 \times 10^{-4} \text{ C} //$$

$$= 0.00086$$

$$\approx 8.6 \times 10^{-4} \text{ C} //$$

QUESTION 3

A 50Hz, 1/4hp motor runs at 2000rpm and takes 0.7A when connected to a 220V DC source if the resistance and inductance of the machine are given as 15Ω and 0.25H respectively. Determine the following when the motor is connected to a 220V, 50Hz AC supply and is loaded to take 0.7A of current.

- i Speed of the motor
- ii The power factor of the motor
- iii Torque developed by the motor
- iv What type of motor could be used for this application

Answers

NOTE:

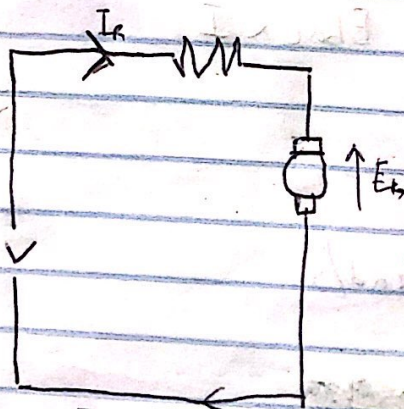
$$F = 50 \text{ Hz}, \frac{1}{4} \text{ hp}, N_r = 2000 \text{ rpm},$$

$$V = 220 \text{ V}, R = 15 \Omega, L = 0.25 \text{ H}$$

On a DC supply

$$\text{Voltage} = 220 \text{ V}$$

$$\text{Current } I = 0.7 \text{ A}$$



$$\therefore V - E_b = I_L \times R$$

$$V - [I_L \times R] = E_b$$

$$\therefore E_b = 220 - [0.7 \times 15]$$

$$= 209.5 \text{ V}$$

$$\text{Speed on DC, } = 2000 \text{ rpm}$$

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On AC Supply

$$\text{Supply voltage (V)} = 220 \text{ V}$$

$$\text{Current drawn, } I_L = 0.7 \text{ A}$$

$$\text{Reactance drop} = I_L \times R = 0.7 \times 15$$

$$\therefore = 10.5 \text{ V} //$$

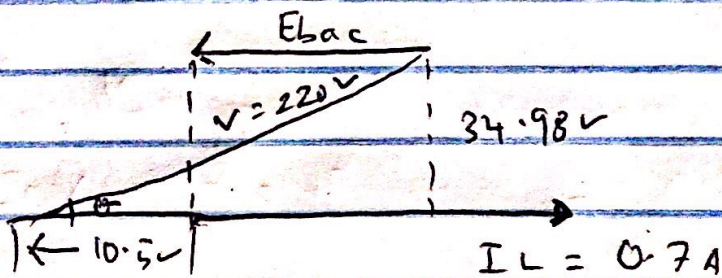
$$\text{Reactance voltage drop} = I_L \times X_L$$

$$= 0.7 \times 2\pi FL$$

$$\text{Where } X_L = j\omega L = 2\pi FL$$

$$= 0.7 \times 2\pi \times 30 \times 0.25$$

$$= 54.98 \text{ V} //$$



$$E_{bac} = \sqrt{V^2 - (X_L)^2} - IR$$

$$\therefore = \sqrt{(220)^2 - (54.98)^2} - 10.5 \text{ V}$$

$$= 202.32 \text{ V} //$$

i. Speed constant equation :

$$\frac{N_2}{N_1} = \frac{E_{b2}}{E_{b1}}$$

$$\therefore \frac{E_{bac}}{E_{bdc}} = \frac{N_{ac}}{N_{dc}}$$

$$\begin{aligned} \therefore N_{ac} &= N_{dc} \times \frac{E_{bac}}{E_{bdc}} \\ &= 2000 \times \frac{202.52V}{209.5V} \end{aligned}$$

$$\therefore N_{ac} = 1933.37 \text{ rpm} //$$

ii. Power factor ($\cos \theta$) = $\frac{E_{bac} + IR}{V}$

$$\therefore = \frac{202.52 + 10.5}{220}$$

$$\therefore = 0.968 \text{ Lagging} //$$

Torque developed (T_w) = $E_{bac} \times I$

$$\therefore T_{ac} = \frac{E_{bac} \times I}{\omega}$$

where (ω) is speed in rad/s

$$\therefore \omega = 2\pi n$$

$$\therefore T_{ac} = \frac{E_{bac} \times I}{2\pi \times \frac{N_{ac}}{60}}$$

$$\therefore = \frac{202.52 \times 0.7 \times 60}{2\pi \times 1933.37}$$

$$\therefore = 0.7004 \text{ N} //$$