

17-6-2020

17/ENG06/010

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Mechanical engineering.

(1) $V = 415V$,

$f = 50\text{Hz}$.

$P = 74.6$.

$\text{PF} = 0.7$.

efficiency = 85%.

3- ϕ

i. $\text{unity} = 1$.

$$C = \frac{\text{KVAR}}{2\pi fV^2}$$

$$\text{KVAR} = \phi \times (\tan \text{actual p.f.} - \tan \text{target p.f.})$$

actual p.f. = $\cos \theta = 0.7$.

$$\theta = \cos^{-1} 0.7$$

$$= 45.57^\circ \quad \therefore \tan 45.57 = 1.0201$$

target p.f. = $\cos \theta = 1$.

$$\theta = \cos^{-1} 1$$

$$\tan 0 = 0$$

$$\text{KVAR} = 74.6 \times (1.0201 - 0)$$

$$= 76.14$$

$$C = \frac{76.1}{2\pi \times 50 \times 415^2}$$

$$2\pi \times 50 \times 415^2$$

$$\begin{aligned}
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 & = 0.0000014 \\
 & = 1.4 \times 10^{-6} \text{ C}
 \end{aligned}$$

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0.9 lagging

$$\text{actual p.f.} = 1.0201$$

$$\text{target p.f.} = \cos \theta = 0.9$$

$$\theta = \cos^{-1}(0.9)$$

$$= 26.16^\circ$$

$$\tan \theta = 0.48$$

$$\begin{aligned}
 \text{KVAR} &= 74.6 \times (1.0201 + 0.48) \\
 &= 111.90 \\
 &= 112
 \end{aligned}$$

$$C = \frac{\text{KVAR}}{2\pi f V^2}$$

$$= \frac{112}{2\pi \times 50 \times 415^2}$$

$$= 2.071 \times 10^{-6}$$

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3. $f = 50\text{Hz}$ $1/4\text{hp}$

$n_s = 2000\text{rpm}$

$V = 220$

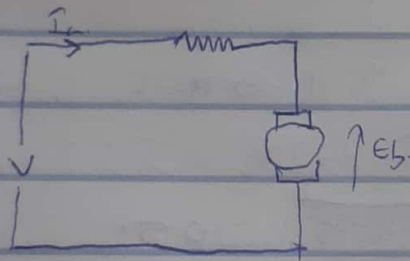
resistance = 15Ω

inductance = 0.25H

on DC supply

Supply voltage = 220

Current drawn = 0.7A



$$V - E_b = I_L \times R$$

$$V - (I_L \times R) = E_b$$

$$E_b = 220 - (0.7 \times 15)$$

$$= 209.5\text{V}$$

Speed on DC

$$n_{dc} = 2000\text{rpm}$$

on A.C. supply

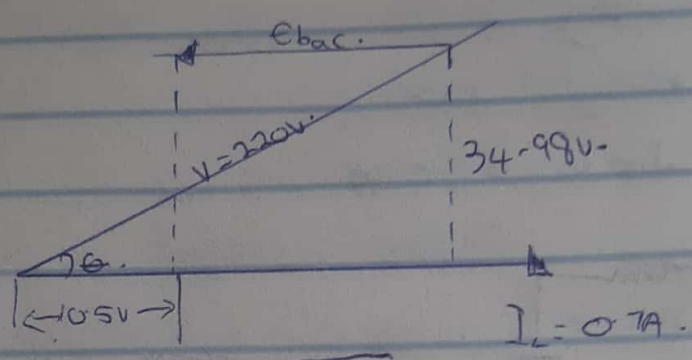
Supply voltage = 220V

Current drawn $I_L = 0.7\text{A}$

$$\text{Reactance drop} = I_L \times R = 0.7 \times 15 = 10.5\text{V}$$

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 Reactance voltage drop = $I_L \times X_L$
 $= 0.7 \times 2\pi fL$

where $X_L = j\omega L = 2\pi fL$
 $= 0.7 \times 2 \times 3.14 \times 50 \times 0.25$
 $= 54.98V$



$$E_{bac} = \sqrt{V^2 - (I_L R)^2}$$

$$= \sqrt{220^2 - 10.5^2}$$

$$= 202.52V$$

recall

$$\frac{N_2}{N_1} = \frac{E_{b2}}{E_{b1}}$$

$$\therefore \frac{E_{bac}}{E_{bdc}} = \frac{N_{ac}}{N_{dc}}$$

making N_{ac} subject of formula

$$N_{ac} = N_{dc} \times \frac{E_{bac}}{E_{bdc}}$$

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$$= 2000 \times \frac{202.52 \text{ V}}{209.5 \text{ V}}$$

$$N_{ac} = 1933.37 \text{ rpm}$$

ii Power factor, $\cos \phi = \frac{E_{bac} + I_a R}{V}$

$$= \frac{202.52 + 10.5}{220}$$
$$= 0.97, \text{ lagging}$$

iii Torque developed $\tau_w = E_{bac} \times I_a$

$$\tau_{ac} = \frac{E_{bac} \times I_a}{\omega}$$

where $\omega = \text{speed in rad/sec}$

$$\omega = 2\pi n$$

where $n = \text{speed in rev/sec}$

$$\tau_{ac} = \frac{E_{bac} \times I_a}{\frac{2\pi \times n_{ac}}{60}}$$

$$= \frac{202.52 \times 0.7 \times 60}{2\pi \times 1933.37}$$

$$= 0.7 \text{ Nm}$$

$$= 0.7 \text{ Nm}$$

iv Universal motor.

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2. No of poles = 6.

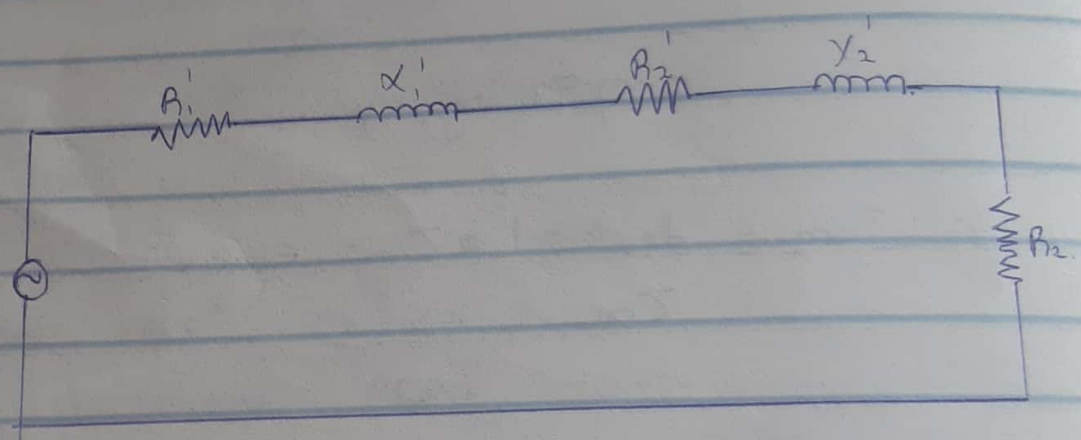
f = 50 Hz.

V = 415 V

~~slip~~ k = ~~0.1~~ $\frac{5}{6} = 0.83$

$Z_1 = 0.25 + j0.75$ for stator.

$Z_2 = 1.713 + j0.52$ for rotor.



Supply voltage per phase = $\frac{415}{\sqrt{3}} = 239.60 \text{ V.}$

wrt the rotor.

$$R_{02} = (R_2 + k^2 R_1) \cdot 0.83^2$$

$$= (1.713 + 0.25) \times 0.83^2$$

$$R_{02} = 1.53 \Omega \cdot 1.347 \Omega$$

$$X_{02} = (X_2 + k^2 X_1)$$

$$= (0.52 + 0.83^2 \times 0.75)$$

$$= 1.041 \Omega$$

$$Z_{02} = R_{02} + X_{02}$$

7.

$$= \frac{1.533 + j1.6}{Z_{02} = \sqrt{1.533^2 + 1.6^2}} = 2.22 \Omega$$

$$= \frac{1.347 + j1.041}{Z_{02} = \sqrt{1.347^2 + 1.041^2}} = 1.7 \Omega$$

To find rotor current

$$I_2 = \frac{E_2}{Z_{02}}$$

$$\begin{aligned} \text{Recall } E_2 &= KV_1 \\ &= 329.6 \times 0.93 \\ &= 199.67V \end{aligned}$$

$$\therefore I_2 = \frac{199.67}{1.7} = 117.5 A$$