

17/ENG06/038

MECHANICAL ENG

300L

ELECTRICAL MACHINES

(1)

$V = 4154$, 3- ϕ , 4 wire, $f = 50\text{Hz}$ $P = 74.6\text{mw}$

$P.f = 0.7$ $\eta_{\text{eff}} = 85\%$

(i) unity = 1

$C = \text{kVAR}$

$2\pi f V^2$

$\text{kVAR} = P \times (\tan \text{ actual p.f} - \tan \text{ target p.f})$

actual p.f = $\cos \theta = 0.7$

$\theta = \cos^{-1}(0.7)$

$= 45.57$

$\tan(45.57) = 1.021$

target p.f $\Rightarrow \cos \theta = 1$

$\theta = \cos^{-1} = 0$

$\tan 0 = 0$

$\text{kVAR} = 74.6 \times (1.021 - 0)$

$= 76.10$

~~$C = \frac{76.10}{2 \times \pi \times 50 \times 415^2} = 1.40 \times 10^{-6} \text{C}$~~

~~$C = \frac{76.10}{2 \times \pi \times 50 \times \left(\frac{415}{\sqrt{3}}\right)^2} = 4.22 \times 10^{-6} \text{C}$~~

$C = \frac{76.10}{2 \times \pi \times 50 \times \left(\frac{415}{\sqrt{3}}\right)^2}$

$C = \frac{76.10}{18035359.83}$

$C = 4.22 \times 10^{-6} \text{C}$

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MREKT ENG

300 L

ii) 0.9 lagging

actual p-f = 1.0201

target p-f = cos θ = -0.9

θ = cos⁻¹(-0.9)

= 154.16

tan θ = -0.48

kVAR = 74.6 × (1.0201 - (-0.48))

= 111.90

≈ 112

~~C = kVAR~~
~~2πfV~~

~~= 112~~

~~2 × π × 50 × 415²~~

= π × 10⁻⁶ C

C = kVAR

2πfV²

= 112

2 × π × 50 × (415/√3)²

= ~~112~~ = 6.21 × 10⁻⁵ C

Type of motor

3-phase induction motor.

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QUESTION 3

MENA ENG

$f = 50\text{ Hz}$, $\frac{1}{4}\text{ hp}$, $N_s = 2000\text{ rpm}$, $V = 220\text{ V}$

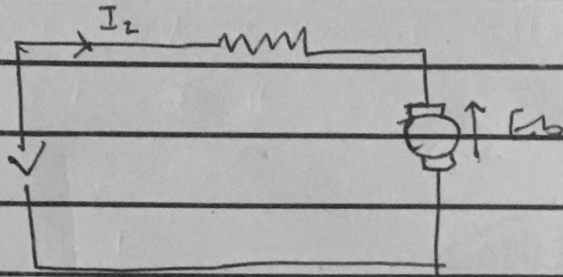
300 L

$15\ \Omega$ and 0.25 H

On DC supply

Supply voltage = 220 V

Current drawn, $I = 0.7\text{ A}$



$$V - E_b = I_2 \times R$$

$$V - [I_L \times R] = E_b$$

$$E_b = 220 - [0.7 \times 15]$$

$$= 209.5\text{ V}$$

speed on DC;

$$N_{dc} = 2000\text{ rpm}$$

On AC Supply

Supply voltage = 220 V

current drawn, $I_L = 0.7\text{ A}$

$$\text{Reactance drop} = I_L \times R = 0.7 \times 15 = 10.5\text{ V}$$

$$\text{Reactance voltage drop} = I_L \times X_L$$

$$= 0.7 \times 2\pi fL$$

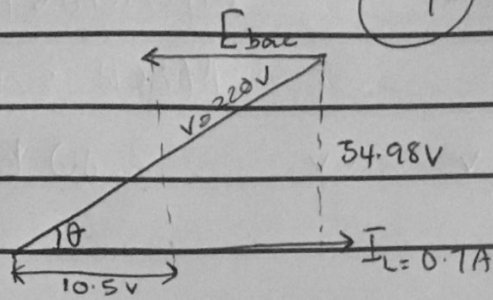
$$\text{where } X_L = \omega L = 2\pi fL$$

$$= 0.7 \times 2\pi \times 50 \times 0.25$$

$$= 54.98\text{ V}$$

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$$E_{bac} = \sqrt{V^2 - [X_L]^2} - I_L R$$

$$= \sqrt{(220)^2 - (54.98)^2} - 10.5V$$

$$= 202.52V$$

(i) Speed of the motor

Recall speed constant equation

$$\frac{N_2}{N_1} = \frac{E_{b2}}{E_{b1}}$$

$$\text{So } \frac{E_{bac}}{E_{bdc}} = \frac{N_{ac}}{N_{dc}}$$

$$N_{ac} = N_{dc} \times \frac{E_{bac}}{E_{bdc}}$$

$$= 2000 \times \frac{202.52V}{209.5V}$$

$$N_{ac} = 1933.37 \text{ rpm}$$

ii) Power factor, $\cos \phi = \frac{E_{bac} + I_L R}{V}$

$$= \frac{202.52 + 10.5}{220}$$

$$= 0.9682 \text{ (lagging)}$$

(5)

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3002

iii) Torque developed, $T_w = E_{bac} \times I$

$$T_{ac} = \frac{E_{bac} \times I}{\omega}$$

where ω is speed in rad/s

$$\omega = 2\pi n$$

$$T_{ac} = \frac{E_{bac} \times I}{2\pi \times \frac{N \times \omega}{60}}$$

$$= \frac{202.52 \times 0.7 \times 60}{2\pi \times 1933.37}$$

$$T_{ac} = 0.700 \text{ Nm}$$

iv) Universal motor

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QUESTION 2

$$V_{LL} = 415V$$

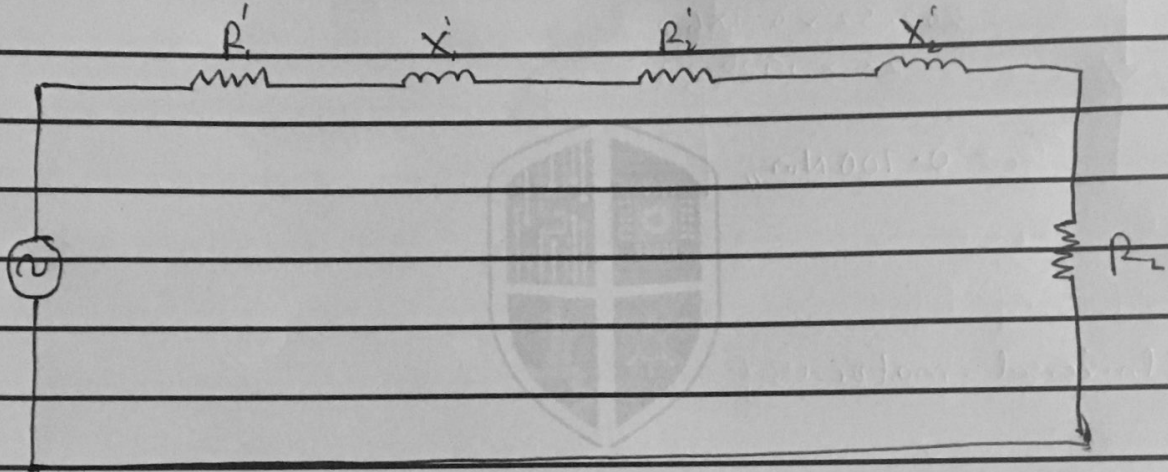
$$\text{No of poles} = 6$$

$$f = 50\text{Hz}$$

$$k = 5/6 = \text{---}$$

$$Z_1 = 0.25 + j0.75 \text{ --- stator}$$

$$Z_2 = 1.173 + j0.52 \text{ --- rotor}$$



$$\text{Supply voltage per phase, } V = \frac{415}{\sqrt{3}} = 239.60V$$

Referring to rotor

$$R_{01} = (R_2 + K^2 R_1) \\ = (1.173 + (5/6)^2 \times 0.25)$$

$$R_{01} = 1.347\Omega$$

$$X_{02} = (X_2 + K^2 X_1) \\ = j(0.52 + (5/6)^2 \times 0.75) \\ = 1.041\Omega$$

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$$Z_{02} = R_{02} + jX_{02}$$
$$= 1.347 + j1.041$$

$$Z_{02} = \sqrt{1.347^2 + 1.041^2}$$
$$= 1.70 \Omega$$

To find rotor current, \bar{I}_2

$$\bar{I}_2 = \frac{E_2}{Z_{02}}$$

Recall; $E_2 = kV_1$

$$= 239.6 \times 0.833$$
$$= 199.58 \text{ V}$$

$$\therefore \bar{I}_2 = \frac{199.58 \text{ V}}{1.70} = 117.4 \text{ A}$$