

MATIC NO: 17/ENG06/090

DEPARTMENT: MECHANICAL

QUESTION 1Solution

$$V_{line} = 415V \quad f = 50Hz \quad P = 74.6kW \quad P.f = \cos\theta = 0.7 \text{ lagging}$$

$$E_{eff} = 85\%$$

$$i) V_{phase} = \frac{V_{line}}{\sqrt{3}} = \frac{415}{\sqrt{3}} = 239.6V$$

$$C = \frac{kVar(Q)}{2\pi f V^2}$$

$$Q = P \times [\tan\theta_1 - \tan\theta_2]$$

$$\text{where } \theta_1 = \cos^{-1}[0.7] = 45.57^\circ$$

$$\therefore \text{target P.F} = \cos\theta = 1$$

$$\theta = \cos^{-1}[1]$$

$$\theta_2 = 0^\circ$$

$$\therefore Q = 74.6 \times [\tan(45.57) - \tan(0)]$$

$$= 74.6 \times 1.02$$

$$Q = 76.092kVar$$

TEST

MATIC NO : 17/ENG06/090

DEPARTMENT : MECHANICAL

QUESTION 1Solution

$$\therefore C = \frac{76.092}{2 \times \pi \times 50 \times 239.6^2} = 4.21 \mu F$$

(a) for power factor of 0.9 lagging,

$$\text{actual P.f angle} = \cos^{-1}[0.7] = 45.57^\circ$$

$$\text{target P.f angle} = \cos^{-1}[0.9] = \cancel{25.84^\circ} 154.16^\circ$$

$$\therefore Q = P (\tan \theta_1 - \tan \theta_2)$$

$$= 74.6 \times [\tan(45.57) - \tan(154.16)]$$

$$Q = 74.6 \times (1.02 + 0.48)$$

$$\therefore Q = 111.9 \text{ kVar}$$

$$\therefore C = \frac{111.9}{2 \times \pi \times 50 \times 239.6^2} = 6.204 \mu F$$

$$2 \times \pi \times 50 \times 239.6^2$$

MATRIC NO: 17|ENG06|090  
DEPARTMENT: MECHANICAL

QUESTION 3Solution

$$f = 50\text{Hz} \quad P = \frac{1}{4}\text{hp} = \quad V = 220\text{V} \quad I = 0.7\text{A}$$

$$N_r = 2000\text{rpm}$$

$$R = 15\Omega$$

$$X = 0.25\text{H}$$

$$\therefore \text{Speed of motor} = \frac{120f}{P} = \frac{120 \times 50}{P} = \frac{6000}{P}$$

$$V - E_{b1} = I(R + jX)$$

$$220 - E_{b1} = 0.7(15 + 0.25j)$$

$$E_{b1} =$$

$$V - E_{b1} = IR$$

$$220 - E_{b1} = 0.7(15)$$

$$E_{b1} = 209.5\text{V}$$

for  $E_{b2}$ ,

$$E_{b2} = \sqrt{V^2 - [IX_c]^2} - IR$$



MATRIC NO: 17/ENG06/090

DEPARTMENT: MECHANICAL

QUESTION 3

$$E_{b2} = \sqrt{220^2 - [0.7 \times 0.25]}$$

$$X_L = 2\pi fL = 2 \times \pi \times 50 \times 0.25 = 78.54 \Omega$$

$$\therefore E_{b2} = [220^2 - [0.7 \times 78.54]^2]^{1/2} - [0.7 \times 15]$$

$$E_{b2} = 202.52 \text{ V}$$

but,

$$\frac{N_2}{N_1} = \frac{E_{b2}}{E_{b1}}$$

$$\text{and } N_1 = 2000 \text{ rpm}$$

$$\therefore N_2 = N_1 \times \frac{E_{b2}}{E_{b1}} = 2000 \times \frac{202.52}{209.5} = 1933.37 \text{ rpm}$$

$$(i) \text{ P.f} = \cos \theta = \frac{IR + E_{b2}}{V} = \frac{(0.7 \times 15) + 202.52}{220}$$

$$\text{P.f} = 0.97$$

TEST

MATRIC NO: 17/ENG06/090

DEPARTMENT: MECHANICAL

QUESTION 3

$$T = P \times \omega \quad P = T \times \omega$$

$$\text{or } T = \frac{P}{\omega}$$

$$(ii) \quad \omega = \frac{2\pi N_2}{60} = \frac{2 \times \pi \times 1933.37}{60} = 202.5 \text{ rad/s}$$

$$\text{where } P = \frac{1}{4} \text{ hp} = \frac{1}{4} \times 745.7 = 186.43 \text{ watts}$$

$$\therefore T = \frac{P}{\omega} = \frac{186.43}{202.5} = 0.92 \text{ Nm}$$

(iv) Universal Motor

MATRIC NO: 17/ENGG06/090

DEPARTMENT: MECHANICAL

QUESTION 2

Solution

$P = 25hp = 25 \times 746 = 18650 \text{ watts}$

$P = 5 \text{ poles}$

$V_{line} = 415 \text{ V}$

$f = 50 \text{ Hz}$

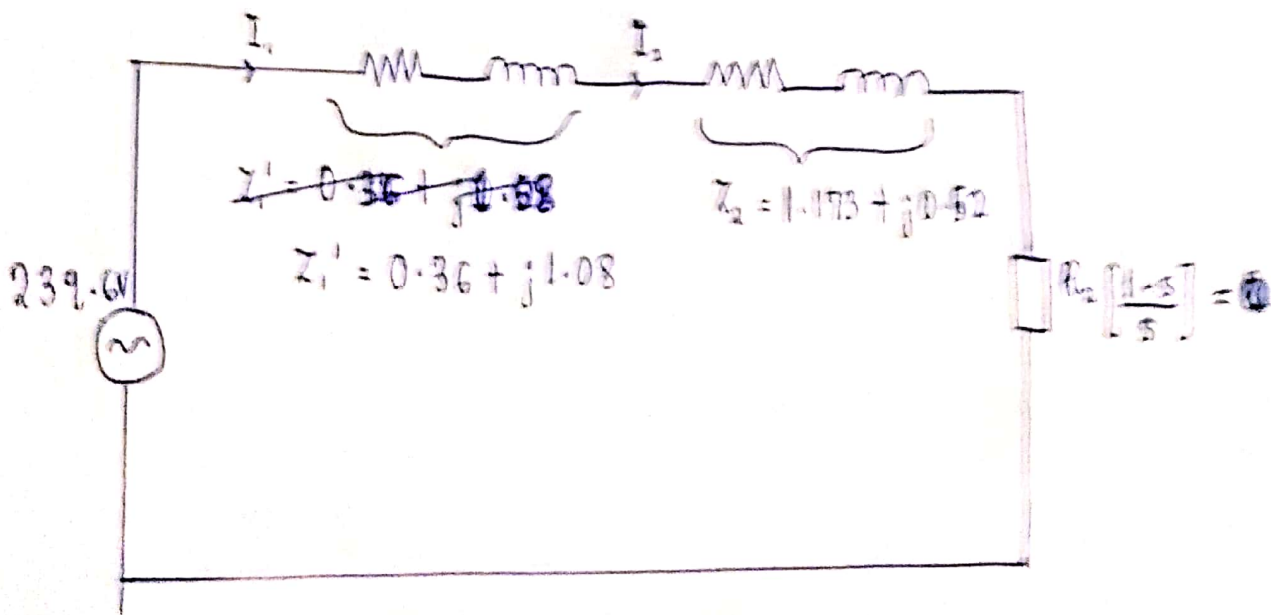
$\frac{V_1}{V_2} = \frac{6}{5}$

$V_{phase} = \frac{415}{\sqrt{3}} = 239.6 \text{ V}$

(i)  $Z_1 = 0.25 + j0.75 \Omega$

$s = 1$

$Z_2 = 1.173 + j0.52 \Omega$



$\frac{V_2}{V_1} = \frac{5}{6} \therefore Z_1' = \frac{Z_1}{k^2} = \frac{0.25 + j0.75}{0.833^2} = 0.36 + j1.08 \Omega$

where  $k = \frac{V_2}{V_1} = \frac{5}{6} = 0.833$



TEST

MATRIC NO: 17/ENG06/090  
DEPARTMENT: MECHANICAL

QUESTION 2Solution

$$(i) \quad Z_T = Z_1 + Z_2 = 0.36 + j1.08 + 1.173 + 0.52j \\ = 1.533 + j1.6$$

$$\therefore I_1 = \frac{V}{Z_T} = \frac{239.6}{1.533 + j1.6} = 108.13 \angle -46.23^\circ \text{ A}$$

~~$$V_{\text{drop}} = I_1 \times Z_1' = (108.13 \angle -46.23^\circ)(0.36 + j1.08) \\ = 123.10 \angle 25.34^\circ \text{ V}$$~~

~~$$\therefore I_2 = \frac{V - V_{\text{drop}}}{Z_2} = \frac{239.6 - (123.10 \angle 25.34^\circ)}{1.173 + j0.52}$$~~

MATRIC NO: 17/ENG06/090  
DEPARTMENT: MECHANICAL

QUESTION 1

Continuation

The drive motor is a star-connected 3 phase induction motor.

