

17HENG061043

Question 1

(i) ϕ given $V = 415\text{ V}$, 3-pole, 4-wires, $F = 50\text{ Hz}$, $P = 74.6$, $P.F = 0.7$
Efficiency = 95%

Unity = 1

$$C = \frac{\text{KVAR}}{2\pi FV}$$

$\rightarrow \text{KVAR} = P \times (\tan \text{ actual PF} - \tan \text{ target PF})$

where actual PF = $\cos \theta = 0.7$
 $\theta = \cos^{-1} 0.7 = 45.57$
hence $\tan(45.57) = 1.0201$

target PF = $\cos \theta = 1$
 $\theta = \cos^{-1} 1 = 0$
 $\tan 0 = 0$

$$\text{KVAR} = 74.6 \times (1.0201 - 0)$$

$$= 76.09946$$

$$\approx 76.10$$

$$C = \frac{76.10}{2\pi \times 50 \times 415^2} = 0.000014$$

$$\approx 1.4 \times 10^{-6}$$

ii) Lagging

actual pf = 1.0201
target pf = $\cos \theta = -0.9$
 $\theta = \cos^{-1} (-0.9)$
 $= 157.16$
 $\tan \theta = -0.48$

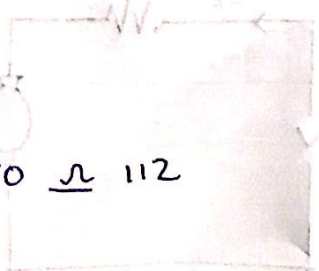
$$\text{KVAR} = 74.6 \times (1.0201 - (-0.48)) = 111.90 \approx 112$$

$$C = \frac{\text{KVAR}}{2\pi FV}$$

$$= \frac{112}{2\pi \times 50 \times 415^2} = 2.07 \times 10^{-6}$$

$$\approx 2.07 \times 10^{-6}$$

(1)



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Question 2

$V_{line} = 415V$

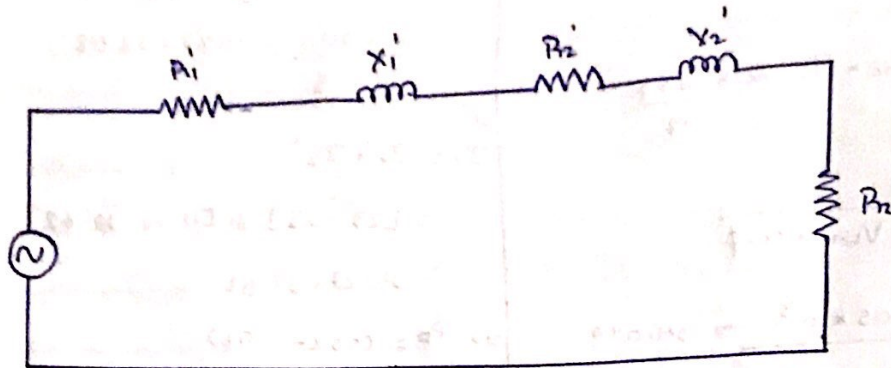
$f = 50Hz$

$Z_1 = 0.25 + j0.75$ (Stator)

No. of poles = 6

$k = \frac{5}{6} = 0.83$

$Z_2 = 1.173 + j0.82$ (Rotor)



Supply Voltage per phase

$V_{line} = \sqrt{3} V_{phase} \therefore V_{phase} = \frac{V_{line}}{\sqrt{3}} = \frac{415}{\sqrt{3}} = 239.60V$

Referring to rotor

$R_{02} = (R_2 + k^2 R_1)$
 $= (1.173 + (\frac{5}{6})^2 \times 0.25)$

$R_{02} = 1.347 \Omega$

$X_{02} = (X_2 + k^2 X_1)$
 $= j(0.82 + (\frac{5}{6})^2 \times 0.75)$
 $= j1.041$

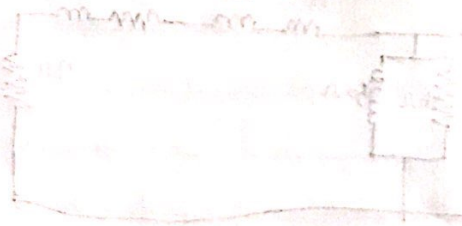
$Z_{02} = \sqrt{R_{02}^2 + X_{02}^2}$
 $= \sqrt{1.347^2 + 1.041^2}$
 $= 1.702 \Omega$

To find rotor current

$I_2 = \frac{E_2}{Z_{02}}$ Recall that $E_2 = kV_1$
 $= 239.6 \times 0.83$
 $= 199.67V$

$\therefore I_2 = \frac{199.67}{1.702} = 117.315A$

(2)



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Question (3)

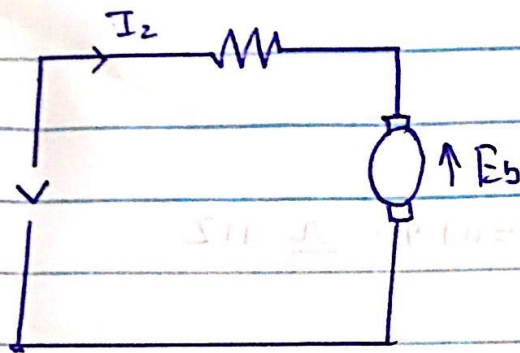
(3) Given 50Hz, Y/4hp motor runs $N_s = 2000 \text{ rpm}$ $I = 0.7$ $V = 220$

$$R = 15 \Omega \quad L = 0.25 \text{ H}$$

on Dc supply

$$\text{supply voltage} = 220 \text{ V}$$

$$\text{current drawn} = I = 0.7 \text{ A}$$



$$V - E_b = I_L \times R$$

$$V - [I_L \times R] = E_b$$

$$E_b = 220 - [0.7 \times 15]$$

$$= 209.5 \text{ V}$$

Speed on Dc

$$N_s = 2000 \text{ rpm}$$

(3)

Continuation of 3

On dc supply

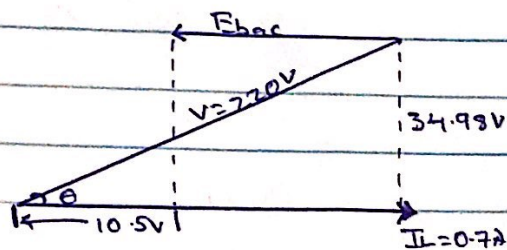
supply Voltage = 220V

Current drawn $I_L = 0.7A$ Resistance drop = $I_L \times R = 0.7 \times 15 = 10.5V$ Reactance Voltage drop = $I_L \times X_L = 0.7 \times 27\pi$ where $X_L = j\omega L = 2\pi fL$

~~$= 0.7 \times 2\pi \times 50 \times 0.25$~~

$$\therefore = 0.7 \times [2 \times \pi \times 50 \times 0.25]$$

$$= 54.98V$$



$$\begin{aligned} E_{bac} &= \sqrt{V^2 - (IX_L)^2} - IR \\ &= \sqrt{(220)^2 - (54.98)^2} - 15 \times 0.7 \\ &= 202.52V \end{aligned}$$

Recall speed equation

$$\frac{N_2}{N_1} = \frac{E_{b2}}{E_{b1}}$$

$$\text{so } \frac{E_{bac}}{E_{bdc}} = \frac{N_{ac}}{N_{dc}}$$

Making N_{ac} the subject of formulae

$$N_{ac} = \frac{N_{dc} \times E_{bac}}{E_{bdc}} = \frac{2000 \times 202.52V}{209.9V}$$

$$= 1933.37 \text{ rpm}$$

$$\text{Power factor} = \cos \phi = \frac{E_{bac} + IR}{V} = \frac{202.52 + 10}{220}$$

$$= 0.969 \text{ Lagging}$$

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3) Continuation

$$\text{Torque developed} = T_w = E_{bac} \times I$$

$$T_{ac} = \frac{E_{bac} \times I}{\omega}$$

where $\omega = 2\pi n$, where n is speed in rev

$$T_{ac} = \frac{E_{bac} \times I}{2\pi \times \frac{N_{ac}}{60}}$$

$$= \frac{202.52 \times 0.7 \times 60}{2\pi \times 1933.37}$$

$$20.700 \text{ Nm}$$

(5)