

16/ENG04/031 - 400 level - Elect/Elect Engineering

Question number 1;

ABUAD mango juice factory is serviced by a 415V, 3- ϕ , 4 wire, 50Hz. This supply powers the main drive motor, having an output of 74.6 kW and running on full load at a power factor of 0.7 lagging with an efficiency of 85%. Identify the drive motor type & sketch the motor - supply circuit with a direct-online starter. Determine the capacitance per phase of a mesh-connected capacitor necessary to raise the power factor to i) Unity ii) 0.9 lagging. Sketch the phasor diagram using an appropriate scale showing the computed values of currents.

Soln.

Given parameters;

$V_{line} = 415 \text{ V}$; no of phase = 3 ; $f = 50 \text{ Hz}$
 $P_{out} = 74.6 \text{ kW} = 74.6 \times 10^3 \text{ W}$; $Pf = 0.7 \text{ lagging}$; Efficiency $\eta = 85\%$
 $V_{phase} = \frac{V_{line}}{\sqrt{3}} = \frac{415}{\sqrt{3}} = 239.6 \text{ V}$

Ans

b) i) The capacitance per phase of a mesh-connected capacitor to raise the pf to Unity, i.e.

$$C = \frac{KVAR}{2\pi f V^2}$$

\Rightarrow Motor running on full-load at P.f 0.7 lagging;

$$\cos \phi = 0.7$$

$$\phi = \cos^{-1}(0.7) = 45.573^\circ \quad \tan(45.573) = 1.02$$

At Unity, i.e.

$$\cos \theta = 1$$

$$\theta = \cos^{-1}(1) = 0$$

$$\tan(0) = 0$$

$$\text{Reactive power, KVAR} = 74.6 \times (1.02 - 0) = 76.092$$

① continuation

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$$C = \frac{\text{KVAR}}{2\pi f V_{\text{line}}^2} = \frac{76.092}{2 \times \pi \times 50 \times (239.6)^2}$$
$$= \frac{76.092}{18,035,305.37} = 4.22 \times 10^{-6} \text{ F} = \underline{\underline{4.22 \mu\text{F}}}$$

(i.) At 0.9 lagging;

from 0.7 lagging = $\cos \theta = 0.7$

$$\theta = \cos^{-1}(0.7) = 45.573^\circ$$

$$\tan \theta (45.73) = \underline{\underline{1.02}}$$

$$P_f = \cos \theta = 0.9$$

$$\theta = \cos^{-1}(0.9) = 25.84^\circ$$

$$\tan \theta (25.84) = 0.48$$

from $C = \frac{\text{KVAR}}{2\pi f V^2}$

$$\Rightarrow \text{KVAR} = 74.6 \times (1.02 - 0.48)$$

$$\therefore \text{KVAR} = \underline{\underline{40.284}}$$

$$\Rightarrow C = \frac{\text{KVAR}}{2\pi \times 50 \times 239.6^2} = \frac{40.284}{18,035,305.37} = 2.23 \times 10^{-6} \text{ F}$$

$$\therefore C = \underline{\underline{2.23 \mu\text{F}}}$$

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Carry-Over

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Question Number 2;

A 25 hp, 415 V (line-line), 6-Pole, 50 Hz star-star connected, 3-Phase induction motor has used in the production factory of PZ. Given Stator/rotor phase voltage ratio of 6/5. The stator & rotor impedances per phase are $(0.25 + j0.75)$ ohms & $(1.173 + j0.52)$ respectively. Using the approx. circuit version 2 referred to the rotor side at a slip of unity. Find the following;

- i) Draw the equivalent circuit diagram referred to the rotor side
- ii) Rotor (secondary) current, I_2 .

Solo

Given parameters;

25 hp. horsepower, hp = 25 hp.

V_{line} = 415 V.

Number of poles, P = 6 poles

Frequency, f = 50 Hz

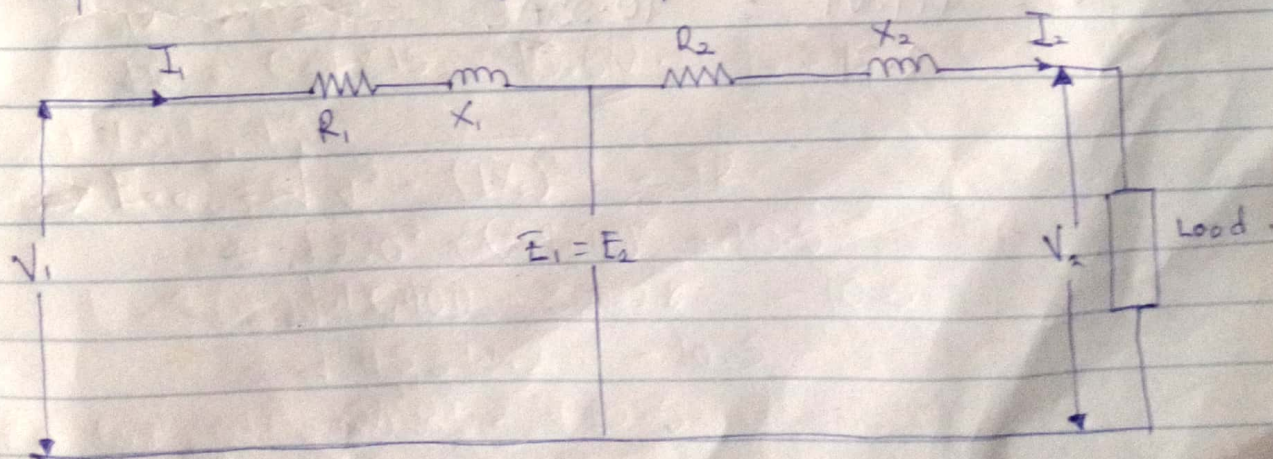
Voltage ratio, K = 6:5 = ~~6/5~~ 6/5 = 1.2.

Stator Impedance, Z = $(0.25 + j0.75) \Omega$

Rotor Impedance, Z = $(1.173 + j0.52) \Omega$

Slip, s = Unity, 1.

i) Equivalent circuit diagram referred to the Rotor (secondary) side;



V_{phase} is given as = $\frac{415}{\sqrt{3}} = 239.600 \text{ V}$.

(2) continuation

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⇒ referring to the rotor (secondary) side

$$R_{02} = (R_2 + K^2 R_1)$$
$$= (1.173 + (6/5)^2 \times 0.25) (1.173 + (6/5)^2 \times 0.25)$$

$$\therefore R_{02} = \underline{1.53 \Omega}$$

$$X_{02} = j(X_2 + K^2 X_1)$$
$$= j(0.52 + (6/5)^2 \times 0.75)$$

$$X_{02} = j1.6$$

$$\Rightarrow Z_{02} = R_{02} + jX_{02}$$
$$= 1.53 + j1.6$$
$$= \sqrt{1.53^2 + 1.6^2}$$

$$\therefore Z_{02} = \underline{2.21 \Omega}$$

(ii) The Rotor Current, I_2 ;

$$I_2 = \frac{E_2}{Z_{02}}$$

$$\text{But } E_2 = KV_1$$
$$= 239.6 \times 0.83$$
$$= 199.67 \text{ V}$$

$$\therefore I_2 = \frac{199.67}{2.21} = 90.35 \text{ A}$$

$$\therefore I_2 = \underline{90.35 \text{ A}}$$

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Question 3:

A 50 Hz, 1/4 hp moto. runs at 2krpm and takes 0.7A when connected to a 220V Ac source. If the resistance & Inductance of the machine are given as 15Ω & 0.25H respectively. Determine the following when the motor is connected to a 220V, 50Hz Ac supply & is loaded to take 0.7A of current;

- i) Speed of the moto.
- ii) The P.f of the moto.
- iii) Torque developed by the moto.
- iv) What type of moto. could be used for this application?

Soln

Given Parameters;

$f = 50 \text{ Hz}, N_s = 2000 \text{ rpm (dc)}; R = 15 \Omega; L = 0.25 \text{ H}$
 $I = 0.7 \text{ A}; V = 220 \text{ V}.$

$E_{ac} = V - IR$
 $= 220 - 0.7 \text{ A} \times 15$

$E_{ac} = 209.5 \text{ V}.$

$E_{ac} = \sqrt{V^2 - (IX_L)^2} - IR$ *(Marking will suspect)*

finding ~~the~~ IX_L ; as $X_L = 2\pi fL$

~~X_L~~ $= IX_L = 0.7 \times 2\pi \times 50 \times 0.25$
 $= 54.98$

~~IR~~ $= I$

$IR = 0.7 \times 15 = 10.5 \text{ V}.$

$\Rightarrow E_{ac} = \sqrt{V^2 - (IX_L)^2} - IR$
 $= \sqrt{220^2 - (54.98)^2} - 10.5$
 $= \sqrt{48,400 - 3,022.8} - 10.5$
 $= \sqrt{45,377.2} - 10.5$
 $= 213.02 - 10.5$

$\therefore E_{ac} = 202.52 \text{ V}$

3 Continuation

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i.) The Speed of the motor (AC);

From the eqn.

$$\frac{N_{ac}}{2000} = \frac{E_{ac}}{E_{dc}}$$

$$\frac{N_{ac}}{2000} = \frac{202.52}{209.5}$$

$$N_{ac} = \frac{2000 \times 202.52}{209.5}$$

$$\therefore N_{ac} = \underline{\underline{1933.37 \text{ rpm.}}}$$

ii.) The power factor of the AC motor supply motor;

$$P.f = \frac{E_{ac} + IR}{V} = \frac{202.52 + 10.5}{220} = \frac{213.02}{220} = \underline{\underline{0.968.}}$$

iii.) The torque developed by the motor;

$$\tau = \frac{EI}{2\pi N_{ac}/60}$$

$$\Rightarrow \tau = \frac{202.52 \times 0.9}{2 \times \pi \times 1933.37/60} = \frac{141.764}{12,147.72} = \frac{141.764 \times 60}{12,147.72} = \frac{8,504.84}{12,147.72} = \underline{\underline{0.70 \text{ Nm.}}}$$

iv.) The type of motor that could be used for this application is a Universal motor because it's designed to be able to run on either DC or single phase AC supply.