

17/ENGG06/0824

MECHANICAL ENGINEERING

$V = 415V$ , 4-wire,  $f = 50Hz$ ,  $P = 74.6$  pf = 0.7,

% eff = 85%

1) unig = 1

$$C = \frac{kVAR}{2\pi f V^2}$$

$kVAR = P \times \tan \text{actual p.f.} \approx \tan \text{target p.f.}$

$$\text{actual p.f.} \Rightarrow \cos \theta = 0.7$$

$$\theta = \cos^{-1} 0.7$$

$$= 45.57$$

$$\tan(45.57) = 1.0201$$

$$\text{target pf} = \cos \theta = 1$$

$$\theta = \cos^{-1} 1 = 0$$

$$\tan \theta = 0$$

$$kVAR = 74.6 \times (1.0201 - 0) = 76.10$$

$$C = \frac{76.10}{2 \times \pi \times 50^2 \times 415^2}$$

$$= 0.0000014$$

$$= 1.4 \times 10^{-6} F$$

0.9 leading

$$\text{actual pf} = 1.0201$$

$$\text{target pf} = \cos = 0.9$$

$$\theta = \cos^{-1}(0.9)$$

$$= 26.10^\circ$$

$$\tan \theta = 0.48$$

$$kVAR = 74.6 \times (1.0201 - 0.48) = 39.8$$

$$= 11.2$$

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$$C = \frac{kVAR}{2\pi f V^2}$$

$$= \frac{11.2}{2 \times \pi \times 50^2 \times 415^2}$$

$$= 0.0000058$$

$$= 5.8 \times 10^{-6} F$$

$$= 0.000058$$

$$= 5.8 \times 10^{-6} F$$

17/EN606/084

MECHANICAL ~~ENGINEERING~~  
ENGINEERING

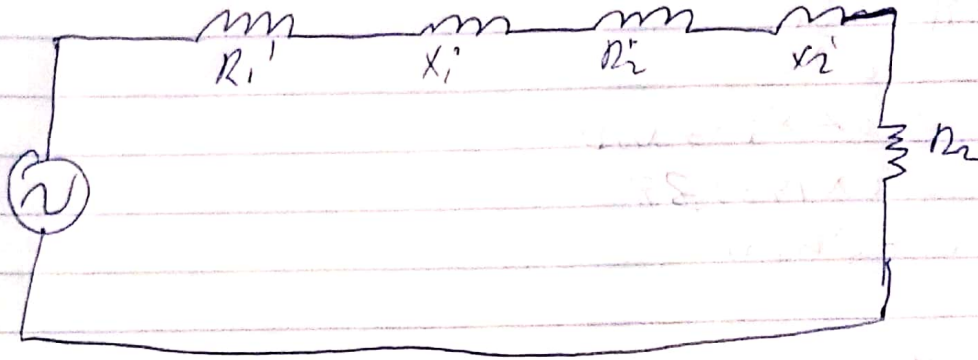
2) No. of poles = 6

$$f = 50 \text{ Hz}$$

$$k = \frac{5}{6} = 0.83$$

$$R_1 = 0.25 + j0.75 \text{ --- stator}$$

$$Z_2 = 1.73 + j0.52 \text{ --- rotor}$$



Supply voltage per phase @  $V = \frac{415}{\sqrt{3}}$

$$= 239.60 \text{ V}$$

Referring to rotor

$$R_{02} = (R_2 + k^2 R_1)$$
$$= (1.73 + (\frac{5}{6})^2 \times 0.25)$$

$$R_{02} = 1.347 \Omega$$

$$X_{02} = (X_2 + k^2 X_1)$$
$$= j(0.52 + (\frac{5}{6})^2 \times 0.75)$$
$$= 1.041$$

$$Z_{02} = R_{02} + X_{02}$$
$$= 1.347 + j1.041$$

$$Z_{02} = \sqrt{1.347^2 + 1.041^2}$$

$$Z_{02} = 1.7$$

To find rotor current

$$I_2 = \frac{E_2}{Z_{02}}$$

Recall that  $E_2 = kV_1$

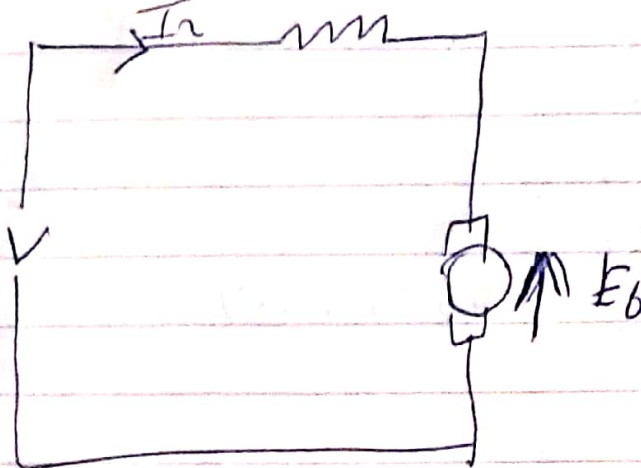
$$= 239.6 \times 0.85$$
$$= 199.67 \text{ V}$$

$$I_2 = \frac{199.67}{1.7} = 117.45 \text{ A}$$

12/EN6061084  
MECHANICAL ENGINEERING

3)  $f = 50 \text{ Hz}$   $\frac{1}{4} \text{ hp}$   $N_2 = 200 \text{ rpm}$ ,  $V = 220 \text{ V}$

On DC Supply  
Supply voltage = 220V  
Current drawn  $I = 0.7 \text{ A}$



$$V - E_b = I_L \times R$$

$$V - [I_2 \times R] = E_b$$

$$E_b = 220 - [0.7 \times 15]$$

$$= 209.5 \text{ V}$$

Speed on DC  
 $N_2 = 200 \text{ rpm}$

1) Recall Speed Constants equation

$$\frac{N_2}{N_1} = \frac{E_{b2}}{E_{b1}}$$

so  $\frac{E_{bac}}{E_{bdc}} = \frac{N_{ac}}{N_{dc}}$

making  $N_{ac}$  subject of the formula

$$N_{ac} = N_{dc} \times \frac{E_{bac}}{E_{bdc}}$$

$$= 200 \times \frac{202.52 \text{ V}}{209.5 \text{ V}}$$

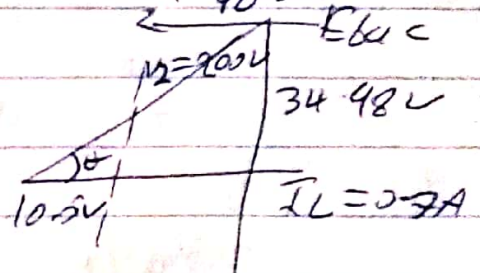
$$N_{ac} = 192.2 \text{ rpm}$$

on AC Supply

Resistance drop =  $I_L \times R = 0.7 \times 15 = 10.5 \text{ V}$

Reactance voltage drop =  $I_L \times X_L = 0.7 \times 2\pi f L$

where  $X_L = j\omega L = 2\pi f L$   
 $= 0.7 \times 2\pi \times 50 \times 0.25 = 54.98 \text{ V}$



$$E_{bac} = \sqrt{V^2 - (X_L)^2}$$

$$= \sqrt{(220)^2 - (54.98)^2} = 10.5 \text{ V}$$

$$= \underline{\underline{202.52 \text{ V}}}$$

$$T_{ac} = \frac{E_{bac} \times I}{\omega}$$

$\omega$  is speed in rad/s

$$\omega = 2\pi n, \text{ where } n \text{ is}$$

$$T_{ac} = E_{ac} \times I \times$$

$$\frac{2\pi \times \frac{A \times V_{ac}}{60}}$$

$$= \frac{202.52 \times 0.7 \times 60}{2\pi \times 1933.37}$$

$$= 0.700 \text{ Nm}$$

3iv) ~~universal~~ universal motor