

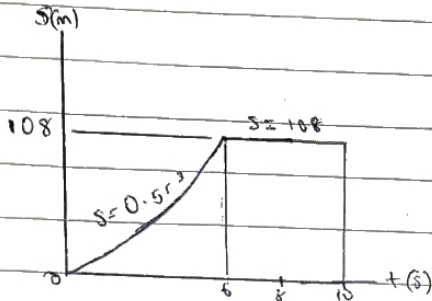
IBET VECTOR SODOMIOTNIKUU

16/EN606/027

ENG 234, ENGINEERING MECHANICS II

MECHANICAL ENGINEERING

(1)



$$v = \frac{ds}{dt}$$

$$v = 1.5t^2$$

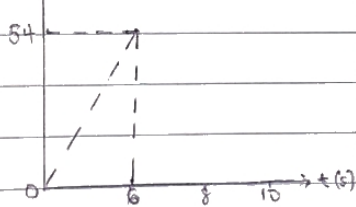
$$\text{at } t = 6s$$

$$v = 1.5 \times 6^2 = 54 \text{ m/s}$$

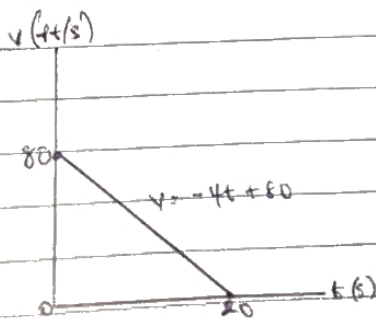
$$\text{From } t = 6s - 10s, s = 108$$

$$\therefore v = 0$$

v-t graph :- v(m/s)



(2)



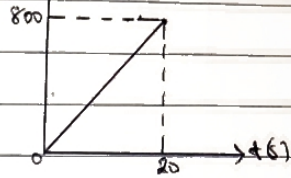
$$\begin{aligned} 1) \quad s &= \int v dt \\ &= \int (-4t + 80) \\ &= -2t^2 + 80t \end{aligned}$$

$$\text{at } t = 20s$$

$$s = -2(20)^2 + 80(20)$$

$$s = 1600 - 800 = 800 \text{ m}$$

s-t graph:- s(m)



ii) Acceleration

$$a = \frac{dv}{dt}$$

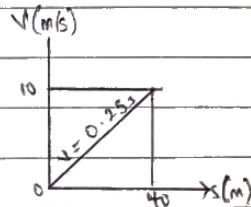
$$\therefore a = -4 \text{ m/s}^2$$

$$\text{at } t = 20s, a = -4 \text{ m/s}^2$$

a-t graph:- a(m/s^2)



3)



$$a = \left(\frac{dv}{ds}\right)v$$

$$v = 0.25s$$

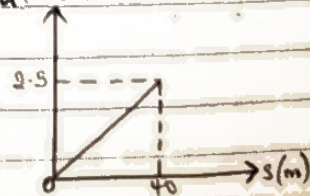
$$a = 10 \times (0.25s) / ds$$

$$a = 10 \times 0.25$$

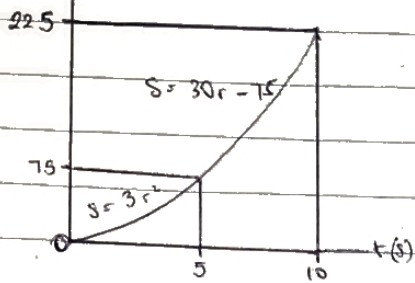
$$a = 2.5 \text{ m/s}^2$$

a-s graph:-

a(m/s^2)



4)  $s(m)$



i)  $v = \int a dt$

$v = \int 20 dt$

$v = 20t$

at  $t = 5s$

$v = 20 \times 5 = 100 m/s$

$5s < t \leq t'$

$\int_{100}^v dv = \int_5^{t'} -10 dt$

$v - 100 = -10t' + 50$

$v - 100 = -10t' + 10(5)$

$v - 100 = -10t' + 10(5)$

$v - 100 = -10t' + 10(5)$

$v - 100 = -10t' + 50$

at  $t'$ ,  $v = 0$

$0 - 100 = -10t' + 50$

$10t' = 150$

$t' = 15s$

i)  $v = \frac{ds}{dt}$

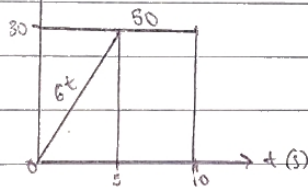
at  $t = 5s$

$v = 6t = 6 \times 5 = 30 m/s$

at  $t = 10s$

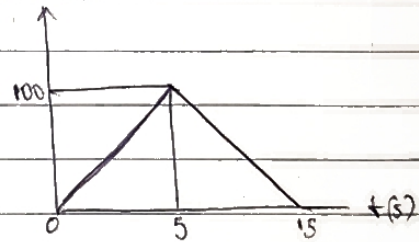
$v = 30 m/s$

$v-t$  graph:  $v(m/s)$



$v-t$  graph

$v(m/s)$



ii)  $a = \frac{dv}{dt}$

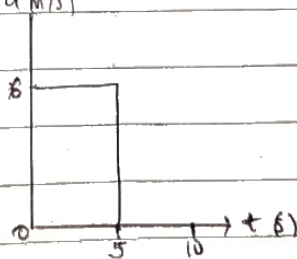
at  $t = 5s$

$a = 6 m/s^2$

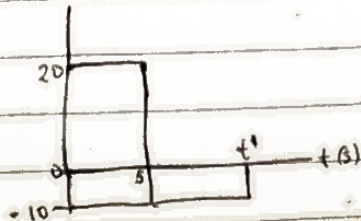
at  $t = 10s$

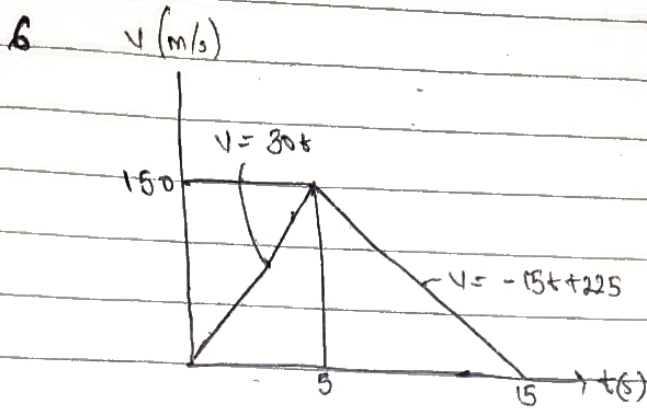
$a = 0 m/s^2$

$a-t$  graph:  $a(m/s^2)$



5)  $a(m/s^2)$





$$0 \leq t \leq 5$$

$$v = 30t$$

$$\int_0^5 ds = \int_0^5 30t dt$$

$$s = 15t^2 \Big|_0^5$$

$$s = 15(5)^2 - 15(0)^2$$

$$s = 15 \times 25$$

$$s = 375 \text{ m}$$

$$5 \leq t \leq 15$$

$$v = -15t + 225$$

$$\int_{375}^s ds = \int_5^{15} (-15t + 225) dt$$

$$s - 375 = \frac{-15t^2 + 225t}{2} \Big|_5^{15}$$

$$s - 375 = \left[ \frac{-15(15^2) + 225(15)}{2} \right] - \left[ \frac{-15(5^2) + 225(5)}{2} \right]$$

$$s - 375 = (-1687.5 + 3375) - (-187.5 + 1125)$$

$$s - 375 = 1687.5 - 937.5$$

$$s - 375 = 750$$

$$s = 1125 \text{ m}$$

s-t graph

