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25 $S \rightarrow aS_a | bS_b | a | b | \lambda$ generates
 $PAL = \{w \in \{a, b\}^* \mid w = w^R\}$

- I) $S \rightarrow \lambda$
- II) $S \rightarrow a$
- III) $S \rightarrow b$
- IV) $S \rightarrow aS_a \rightarrow aa$
- V) $S \rightarrow bS_b \rightarrow bb$
- VI) $S \rightarrow aS_a \rightarrow ab$
- VII) $S \rightarrow bS_b \rightarrow ba$
- VIII) $S \rightarrow aS_a \rightarrow abS_ba \rightarrow abab$
- IX) $S \rightarrow aS_a \rightarrow abS_ba \rightarrow abba$
- X) $S \rightarrow aS_a \rightarrow abS_ba \rightarrow abba$
- XI) $S \rightarrow bS_b \rightarrow bbS_bb \rightarrow bbbb$
- XII) $S \rightarrow bS_b \rightarrow bbS_bb \rightarrow bbbb$
- XIII) $S \rightarrow bS_b \rightarrow bbS_bb \rightarrow bbabb$
- XIV) $S \rightarrow bS_b \rightarrow baS_ab \rightarrow ba\lambda ab \rightarrow baab$
- XV) $S \rightarrow bS_b \rightarrow baS_ab \rightarrow baaab$
- XVI) $S \rightarrow bS_b \rightarrow baS_ab \rightarrow babab$
- XVII) $S \rightarrow aS_a \rightarrow aaS_aa \rightarrow aabb$
- XVIII) $S \rightarrow aS_a \rightarrow aaS_aa \rightarrow aabbS_baa \rightarrow aabababa$
- XIX) $S \rightarrow aS_a \rightarrow aaS_aa \rightarrow aaaaS_aaa \rightarrow aaaaaaaa$
- XX) $S \rightarrow aS_a \rightarrow aaS_aa \rightarrow aabS_baa \rightarrow aabb\lambda baa \rightarrow aabbba$

26 I) $S \rightarrow aS | bS | a$
 $S \rightarrow a$
 $S \rightarrow aS \rightarrow aa$
 $S \rightarrow bS \rightarrow ba$

$S \rightarrow aS \rightarrow abS \rightarrow aba$

$S \rightarrow bS \rightarrow baS \rightarrow ba^2$

$S \rightarrow aS \rightarrow aaS \rightarrow a^3a$

$S \rightarrow bS \rightarrow bbS \rightarrow b^2a$

$L(G) = \{a, aa, ba, aba, baa, \dots\}$

ii) $S \rightarrow aSa | bSb | aSb | \lambda$

$S \rightarrow \lambda$

$S \rightarrow aSa \rightarrow aa$

$S \rightarrow bSb \rightarrow bb$

$S \rightarrow aSb \rightarrow a\lambda b \rightarrow ab$

$S \rightarrow aSa \rightarrow ab Sba \rightarrow ab\lambda ba \rightarrow aab^2$

$S \rightarrow bSb \rightarrow baSab \rightarrow ba\lambda ab \rightarrow baab$

$S \rightarrow aSb \rightarrow aa Sba \rightarrow aa\lambda ba \rightarrow aabb$

$S \rightarrow aSb \rightarrow aa Sab \rightarrow aa\lambda ab \rightarrow aaab$

$L(G) = \{\lambda, aa, bb, ab, abba, baab, \dots\}$

iii) $S \rightarrow aAb | aBb | aSb$

$A \rightarrow aA | a$

$B \rightarrow bB | b$

$S \rightarrow aAb \rightarrow a$

$S \rightarrow aAb \rightarrow aAAb \rightarrow aaab$

$S \rightarrow aBb \rightarrow abBb \rightarrow abb$

$S \rightarrow aBb \rightarrow abBbb \rightarrow abb$

$S \rightarrow aSb \rightarrow aaAbb \rightarrow aaabb$

$S \rightarrow aSb \rightarrow aaBbb \rightarrow aabb$

$L(G) = \{a, aaab, abbb, aabb, \dots\}$

27) $S \rightarrow aAb$

$A \rightarrow aA \mid bA \mid \lambda$

$S \rightarrow aAb \rightarrow a\lambda b \rightarrow ab$

$S \rightarrow aAb \rightarrow aaAb \rightarrow aab$

$S \rightarrow aAb \rightarrow abAb \rightarrow ab\lambda b \rightarrow abb$

$S \rightarrow aAb \rightarrow aaAb \rightarrow aabAb \rightarrow aab\lambda b \rightarrow aabb$

$S \rightarrow aAb \rightarrow abAb \rightarrow abaAb \rightarrow a\lambda baAb \rightarrow ababb$

$S \rightarrow aAb \rightarrow aaAb \rightarrow aabAb \rightarrow aabbAb \rightarrow aabb\lambda b \rightarrow aababb$

$a(ab)^m b \mid m \geq 0$

v) $S \rightarrow aSb \mid ab$

$S \rightarrow ab$

$S \rightarrow aSb \rightarrow aabb$

$a^n b^n \mid n > 0$

w) $S \rightarrow aSc \mid aAc$

$A \rightarrow aAb \mid ab$

$S \rightarrow aAc \rightarrow aabc$

$S \rightarrow aAc \rightarrow aaAbc \rightarrow aaaBBC$

$S \rightarrow aSc \rightarrow aaAcc \rightarrow aaabcc$

$S \rightarrow aSc \rightarrow aaAac \rightarrow aaaaBBC \rightarrow aaaaBBC$

$a^m a^n b^m c^n \mid m \geq 0, n \geq 0$

27) $S \rightarrow A B$

$B \rightarrow b B | b$

$A \rightarrow a A | a$

$S \rightarrow A B \rightarrow a B \rightarrow ab$

$S \rightarrow A B \rightarrow a A B \rightarrow a A b B \rightarrow a a b B \rightarrow a a b b$

$S \rightarrow A B \rightarrow a B \rightarrow a b B \rightarrow a b b$

$a^m b^n \mid m > 0, n > 0$ from part C of Q $\Rightarrow w$ (i)

if not then it's not L(G)

28) $L(G) = a^n b^m \mid n > m$ from part C of Q $\Rightarrow w$ (ii)

$S \rightarrow A B$

$A \rightarrow a A | a$

$B \rightarrow b B | b$

if not then it's not L(G) (ii)

29) $S \rightarrow aS | bS | a | b$

i) babbaq

$S \rightarrow bS \rightarrow baS \rightarrow babS \rightarrow babbS \rightarrow babbaS \rightarrow babbaq$

more than twice the previous part (i)

ii) babababa

$S \rightarrow bS \rightarrow baS \rightarrow babS \rightarrow babaS \rightarrow bababS \rightarrow bababaS \rightarrow babababa$

$\rightarrow babababa$

iii) aaqbbaq

$S \rightarrow aS \rightarrow aaS \rightarrow aaaS \rightarrow aaaaS \rightarrow aaqbaS \rightarrow aaqbbaq$

W) $baa\ baa\ a$

$S \rightarrow bS \rightarrow baS \rightarrow bbaaS \rightarrow baabS \rightarrow baabbaS \rightarrow baabbS \rightarrow baabbaaS$

30) $w \in \{a, b\}^* \mid |w| \bmod 2 = 0$

$S \rightarrow aSb \mid asa \mid bSb \mid ab \mid \epsilon$

i) $w \in \{ab\}^* \mid |w| \bmod 2 = 1$

$S \rightarrow aSb \mid asa \mid bSb \mid ab \mid b$

ii) $w \in \{a, b\}^* \mid |w| \bmod 3 = 0 \text{ or } 1 \text{ or } 2$

iv) $w \in \{a, b\}^* \mid |w| \bmod 3 = 2$

all strings with the same power

each string is starting and ending with the same symbol