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 18/ENG06/024
 Mechanical Engineering

1. flow rate = $10 \text{ dm}^3/\text{min} = 0.01 \text{ m}^3/\text{min}$
 $Q = 1.67 \times 10^{-4} \text{ m}^3/\text{sec}$
 Speed = 1500 rev/min
 $= 25 \text{ rev/sec}$

$dP = 12 \text{ bar} = 12 \times 10^5 \text{ N/m}^2$

Normal displacement = $10 \text{ cm}^3/\text{rev}$
 $= 1 \times 10^{-5} \text{ m}^3/\text{rev}$

Ideal flow rate = nominal displacement \times speed
 $= 25 \times 1 \times 10^{-5}$
 $= 2.5 \times 10^{-4} \text{ m}^3/\text{sec}$

i) vol. efficiency = $\frac{\text{actual flow rate}}{\text{ideal flow rate}} \times 100 = \frac{1.67 \times 10^{-4}}{2.5 \times 10^{-4}} \times 100$

Fluid power = $Q \cdot dP$
 $= 1.67 \times 10^{-4} \times 12 \times 10^5$
 $= 200.4 \text{ W/sec}$

shaft power = $T \omega$

angular speed

$\omega = 2\pi N$ speed of rotation

$= 2 \times \frac{22}{7} \times 25 = 157.14 \text{ rad/sec}$

\therefore shaft power = 12.5×157.14
 $= 1964.25 \text{ W}$

Overall efficiency = $\frac{\text{fluid power}}{\text{shaft power}} \times 100$

$= \frac{200.4}{1964.25} \times 100$

$= 10.2\%$

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$$\begin{aligned} 2) \quad dp &= 100 \times 10^5 \text{ N/m}^2 \\ Q &= 35 \text{ dm}^3/\text{min} \\ &= \frac{0.035}{60} = 5.83 \times 10^{-4} \text{ m}^3/\text{sec} \end{aligned}$$

$$\begin{aligned} \text{fluid power} &= Q \cdot dp \\ &= 5.83 \times 10^{-4} \times 100 \times 10^5 \\ &= 5830 \text{ W} \end{aligned}$$

$$\begin{aligned} \text{Shaft power} &= \frac{\text{fluid power}}{\text{overall eff.}} \times 100 \\ &= \frac{5830}{87} \times 100 \\ &= 6701.15 \text{ W} \end{aligned}$$

$$\text{Nominal displacement} = 50 \text{ cm}^3/\text{rev} = 5 \times 10^{-5} \text{ m}^3/\text{rev}$$

$$dp = 100 \times 10^5 \text{ N/m}^2$$

$$\text{Shaft power} = 15 \text{ kW}$$

$$\text{Actual flow rate } [Q_a] = \frac{0.035}{60} = 5.83 \times 10^{-4} \text{ m}^3/\text{sec}$$

$$\begin{aligned} P_f &= Q \cdot dp \\ &= 5.83 \times 10^{-4} \times 100 \times 10^5 \\ &= 5830 \text{ W} \end{aligned}$$

$$\begin{aligned} \text{Overall efficiency} &= \frac{5830}{15000} \times 100 \\ &= 38.87\% \end{aligned}$$

$$\begin{aligned} \text{Ideal flow rate} &= \text{nominal displacement} \times \text{speed} \\ &= 5 \times 10^{-5} \times \frac{850}{60} = 7.08 \times 10^{-4} \text{ m}^3/\text{sec} \end{aligned}$$

$$\begin{aligned} \text{Vol efficiency} &= \frac{\text{actual flow rate}}{\text{Ideal flow rate}} \times 100 \\ &= \frac{5.83 \times 10^{-4}}{7.08 \times 10^{-4}} \times 100 \\ &= 82.34\% \end{aligned}$$

$$z = 240 \text{ m}$$

$$Q = 0.013 \text{ m}^3/\text{sec}$$

$$\rho = 1000 \text{ kg/m}^3 \text{ for water}$$

$$v_{\text{jet}} = 66 \text{ m/sec}; \quad p = 0 \text{ and } z = 0$$

$$\text{power} = \rho Q + \frac{\rho Q v^2}{2} + \rho g Q z$$

$$= \frac{\rho Q v^2}{2} = \frac{1000 \times 13 \times 10^{-3} \times (66)^2}{2}$$

$$P = 28.314 \text{ kW}$$

ii) power supplied from reservoir

Since reservoir operates at atmospheric pressure; $p = 0, v = 0$

$$P = 0 \cdot Q + \frac{\rho Q v^2}{2} + \rho g Q z$$

$$P = \rho g Q z = 1000 \times 9.81 \times 0.013 \times 240$$
$$= 30.61 \text{ kW}$$

power loss in transmission = Reservoir power - Jet power

$$= 30.61 - 28.314$$

$$= 2.296 \text{ kW}$$

$$\text{Head loss (H)} = \frac{\text{power loss}}{\rho g Q} = \frac{2.296 \times 10^3}{1000 \times 9.81 \times 0.013}$$

$$= 18 \text{ m}$$

$$\text{ii) } \xi = \frac{\text{power of jet}}{\text{power of reservoir}} \times 100$$

$$= \frac{28314}{30610} \times 100$$

$$= 92.45\%$$

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5) $z_2 = 300\text{m}$

$Q = 220\text{ l/sec} = 0.22\text{ m}^3/\text{s}$

$v_{\text{jet}} = 7\text{ m/sec}$; $P = 0$; $z = 0$

power of jet = $PQ + \frac{\rho Q v^2}{2} + \rho g Q z$

$P = \frac{\rho Q v^2}{2} = \frac{890 \times 0.22 \times (7)^2}{2}$

$= 4797.1\text{ W} = 4.7971\text{ kW}$

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ii) Power supplied from reservoir

$P = 0$; $v = 0$

$P = \rho g Q z$

$= 890 \times 9.81 \times 0.22 \times 300$

$= 576.239\text{ kW}$

Power loss in transmission = $576.239 - 4.7971$

$= 571.442\text{ kW}$

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power loss in transmission = $576.239 - 4.7971$

$= 571.442\text{ kW}$

Head loss (h) = $\frac{\text{power loss}}{\rho g Q} = \frac{571.442}{890 \times 9.81 \times 0.22}$

$= 297.50\text{ m}$

Efficiency = $\frac{4797.1}{576239} \times 100$

$= 0.83\%$

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6) $h_1 = 20\text{m}$

$d = 10\text{cm} = 0.1\text{m}$

$r = 0.05\text{m}$

$g = 9.8\text{m/s}^2$

Using conservation of energy

$v = \sqrt{2gh}$

$= \sqrt{392.4}$

$v = 19.8\text{m/s}$ at the base

$\rho = 1000\text{kg/m}^3$

$Q_{\text{base}} = \pi r^2 v$

$= \pi \times 0.05^2 \times 19.8$
 $= 0.156\text{m}^3/\text{sec}$

$\therefore 155.6\text{kg}$ of water leaves the fountain every second

$P = \frac{W}{t} = \frac{mgh}{t}$

$= \frac{\rho \pi r^2 v g h}{t} = 155.6 \times 9.81 \times 20$
 $= 30528.72\text{W}$

$= 30.53\text{kW}$

7) $C_d = 0.96$

$d_1 = 0.3\text{m}$

$d_2 = 0.2\text{m}$

$\rho_g = 19.62\text{N/m}^2$

$A_1 = \frac{\pi d_1^2}{4} = \frac{\pi \times 0.3^2}{4} = 0.0707\text{m}^2$

$A_2 = \frac{\pi \times 0.2^2}{4} = 0.0314\text{m}^2$

$Q = U_1 A_1 = U_2 A_2$

$U_1 = \frac{Q}{0.0717}$

$U_2 = \frac{Q}{0.0314}$

For manometer,

$P_1 + \rho_g g z_1 = P_2 + \rho_g g z_2 + \rho_g g (z_2 - R_1) + \rho_w g R_2$

$$P_1 - P_2 = 19.62 (Z_2 - Z_1) + 587.423$$

For venturimeter;

$$P_1 - P_2 = 19.62 (Z_2 - Z_1) + 0.803 U_2^2$$

Combining:

$$0.803 U_2^2 = 587.423$$

$$U_{ideal} = 27.047 \text{ m/s}$$

$$Q_{ideal} = 27.047 \times \pi \left(\frac{0.2}{2}\right)^2 = 0.85 \text{ m}^3/\text{s}$$

$$Q_{actual} = C_d \cdot Q_{ideal}$$

$$= 0.96 \times 0.85$$

$$= 0.816 \frac{\text{m}^3}{\text{sec}}$$

9) $d_1 = 300 \text{ mm} = 0.3 \text{ m}$

$$A_1 = \frac{\pi}{4} \times 0.3^2 = 0.0707 \text{ m}^2$$

$$P_1 = 400 \text{ kN/m}^2$$

Height above datum $Z_1 = 10 \text{ m}$

$$d_2 = 0.15 \text{ m}$$

$$A_2 = \frac{\pi \times 0.15^2}{4} = 0.01767 \text{ m}^2$$

height of tower and above datum $Z_2 = 6 \text{ m}$

$$Q = 40 \text{ l/sec} = \frac{40 \times 10^{-3}}{10^6} = 0.04 \text{ m}^3/\text{s}$$

$$Q = A_1 V_1 = A_2 V_2$$

$$V_1 = \frac{Q}{A_1} = \frac{0.04}{0.0707} = 0.566 \text{ m/s}$$

$$V_2 = \frac{0.04}{0.01767} = 2.264 \text{ m/s}$$

Using Bernoulli's eqn:

$$\frac{P_1}{\rho} + \frac{V_1^2}{2g} + Z_1 = \frac{P_2}{\rho} + \frac{V_2^2}{2g} + Z_2$$

$$\frac{P_2}{\rho} = \frac{400}{9.81} + \frac{1}{2 \times 9.81} (0.566^2 - 2.264^2) + (10 - 6)$$

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$$\frac{P_2}{w} = 44.525 \text{ m}$$

$$P_2 = 44.525 \times 9.81 = 436.8 \text{ kN/m}^2$$

(10) Manometre reading (y) = 170 mm Hg = 0.17 m Hg
 Specific gravity of heavy liquid (mercury) = 13.6
 S_g of sea water (S_w) = 1.026

$$h = 0.17 \left[\frac{13.6}{1.026} - 1 \right]$$

Velocity of the resistance

$$v = \sqrt{2gh}$$

$$= \sqrt{2 \times 9.81 \times 2.08}$$

$$= 6.39 \text{ m/s}$$

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