

1. $x = 8t^3$, $y = 4t^3 - 7t$, $z = t + 3$ where t is time find the velocity

$$r = 24t^2 i + 12t^2 j + k$$

$$r = (8t^3) i + (4t^3 - 7t) j + (t + 3) k$$

$$\text{velocity} = \frac{dr}{dt} = 24t^2 i + (12t^2 - 7) j + k$$

$$\text{acceleration} = \frac{d^2 r}{dt^2} = 48t i + 24t j$$

2. Find the unit tangent vector to the space curve $x = 3t$, $y = t^3$, $z = t^2$ at $t = 1$.

$$z = t^2 \text{ at } t = 1$$

$$\text{using } T = \frac{dr/dt}{|dr/dt|}$$

$$r = 3t i + t^3 j + t^2 k$$

$$\frac{dr}{dt} = 3i + 3t^2 j + 2t k$$

$$\frac{dr}{dt} = 3i + 3j + 2k$$

$$\left| \frac{dr}{dt} \right| = \sqrt{(3)^2 + (3)^2 + (2)^2} = \sqrt{22}$$

$$T = \frac{3i + 3j + 2k}{\sqrt{22}}$$