

Name: Obot Mikpoob Obot

Matri No: 17/EN/G04/046

Course title: Servo Mechanism & Control Systems

Course code: EEE 441

Questions / Answers

① Briefly explain the Root locus technique

This is also known as Root locus plot in control system and is used for determining the stability of a given system. Now in order to determine the stability of the system using the root locus technique we find the range of value of k for which the complete performance of the system will be satisfactory and the operation is stable.

② Describe the use of Routh Hurwitz to find the stability of a close loop system when:

a) enter row is zero on the Routh table

normal layout for Routh's table

s^4	a_4	a_2	a_0
s^3	a_3	a_1	0
s^2	b_1	b_2	0
s^1	c_1	0	0
s^0	d_1	0	0

$$b_1 = - \frac{\begin{vmatrix} a_4 & a_2 \\ a_3 & a_1 \end{vmatrix}}{a_3}$$

$$b_2 = - \frac{\begin{vmatrix} a_4 & a_0 \\ a_3 & 0 \end{vmatrix}}{a_3}$$

$$b_3 = - \frac{\begin{vmatrix} a_4 & 0 \\ a_3 & 0 \end{vmatrix}}{a_3} = 0$$

In the same way

$$c_1 = \frac{\begin{vmatrix} a_3 & a_1 \\ b_1 & b_2 \end{vmatrix}}{b_1}$$

$$c_2 = - \frac{\begin{vmatrix} a_3 & 0 \\ b_1 & 0 \end{vmatrix}}{b_1} = 0$$

$$d_1 = - \frac{\begin{vmatrix} b_1 & b_2 \\ c_1 & 0 \end{vmatrix}}{c_1} = d_1$$

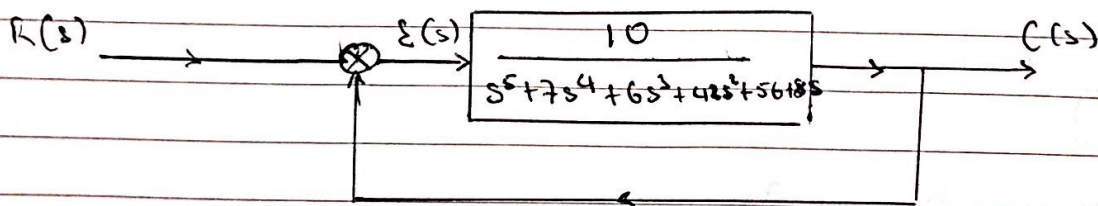
Therefore, standard equation will be

$$b_k = - \det \begin{vmatrix} a_n & a_{n-2k} \\ a_{n-1} & a_{n-2k-1} \end{vmatrix} / a_{n-1}$$

where $d(s) = a_n s^n + a_{n-1} s^{n-1} + \dots + a_1 s + a_0$

Example

in a case where a whole row becomes zero



$$T(s) = \frac{10}{s^5 + 7s^4 + 6s^3 + 4s^2 + 56s + 8}$$

$$\begin{array}{l}
 s^5 \quad | \quad 1 \quad \quad \quad | \quad 6 \quad \quad \quad | \quad 8 \\
 s^4 \quad | \quad 7 \quad \quad \quad | \quad 42 \quad \quad \quad | \quad 56 \\
 s^3 \quad | \quad - \frac{\begin{vmatrix} 1 & 6 \\ 7 & 42 \end{vmatrix}}{7} = 0 \quad - \frac{\begin{vmatrix} 1 & 8 \\ 7 & 56 \end{vmatrix}}{7} = 0 \quad - \frac{\begin{vmatrix} 1 & 0 \\ 7 & 0 \end{vmatrix}}{7} = 0 \leftarrow \text{Entire row is 0}
 \end{array}$$

When a row of zero appears, we derive an auxiliary polynomial from s^4 so we have:

$$P(s) = 7s^4 + 42s^2 + 56 \quad \text{--- (1)}$$

Differentiating (1), we will have

$$\frac{dP(s)}{ds} = 28s^3 + 84s \quad \text{--- (2)}$$

∴ we continue with auxiliary equation

$$\begin{array}{l}
 s^3 \\
 s^2 \quad - \quad \frac{\begin{vmatrix} 28 & 84 \\ 7 & 42 \end{vmatrix}}{28} \quad - \quad \frac{\begin{vmatrix} 84 & 0 \\ 7 & 56 \end{vmatrix}}{28} \quad - \quad \frac{\begin{vmatrix} 0 & 0 \\ 28 & 0 \end{vmatrix}}{28} \\
 = 21 \quad \quad \quad = 56 \quad \quad \quad = 0
 \end{array}$$

$$\begin{array}{l}
 s^1 \quad = \quad - \frac{\begin{vmatrix} 28 & 84 \\ 21 & 28 \end{vmatrix}}{21} \quad - \quad \frac{\begin{vmatrix} 28 & 0 \\ 21 & 0 \end{vmatrix}}{21} \quad \quad \quad 0 \\
 = \quad \quad \quad 28/3 \quad \quad \quad 0 \quad \quad \quad 0
 \end{array}$$

$$\begin{array}{l}
 s^0 \quad = \quad - \frac{\begin{vmatrix} 21 & 56 \\ 28/3 & 0 \end{vmatrix}}{28/3} \quad \quad \quad 0 \\
 = \quad \quad \quad 56
 \end{array}$$

There is no sign change therefore ~~the~~ the system is marginally stable.

b) To determine the poles on the $j\omega$ axis

Ans: when the entries from the row before the row of the zero to the last row are looking at the even polynomials and there are no sign change then all the poles there belong to the $j\omega$ axis.