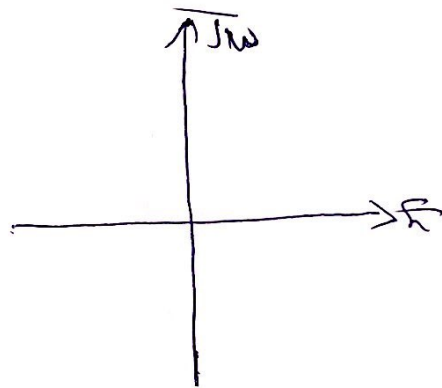


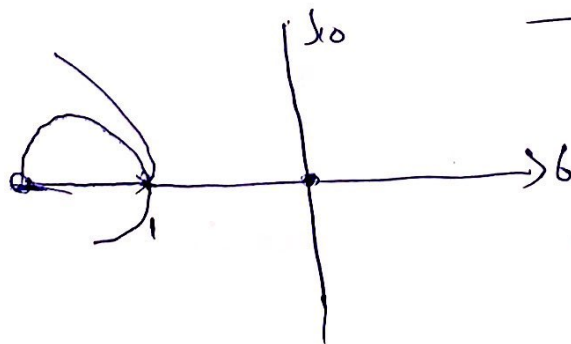
① Root locus is a graphical presentation of the closed loop poles as a system parameter is varied. The root locus gives a graphic presentation of a system stability.

Under the root locus there are various rules to be taken

① The root locus is always symmetrical about the axis
f.g



② The root locus ^{always} starts from the open loop poles & terminates on either finite open loop zero & infinity



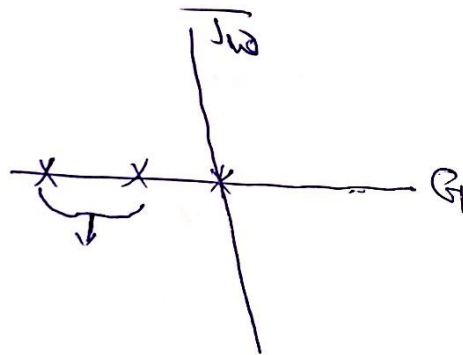
The point marked x are the poles as stated in rule 2. It may terminate at zero or infinity

③ The number of branches terminative on infinity = $P-2$
 where $P \rightarrow$ Number of Poles
 $Z \rightarrow$ Number of Zero's

f.g = $\frac{K}{s[s+1]}$ $Z = 0$ No of branches $2-0=2$
 $P = 2$

④ A point on the real axis lies on the locus if number of open (real) poles + zero's on their right half of s plane is **odd**.

f.g



That part won't be added because it must be on odd number sets 3 poles that is available these.

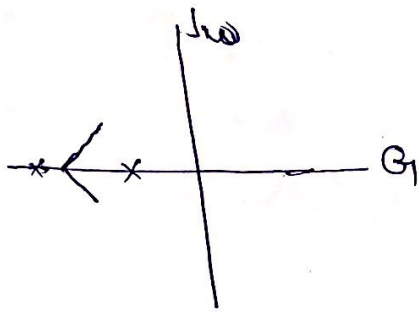
⑤ The angle of asymptotes:

~~$\phi = \frac{(P-Z) \times 180^\circ}{P-Z}$~~ $\phi = \frac{(P-Z) \times 180^\circ}{P-Z}$ $q = 0, 1, 2, \dots, P-Z-1$
 $\phi = \frac{(2q+1) \times 180^\circ}{P-Z}$ $q = 0, 1, 2, \dots, P-Z-1$
 $HZ > P$ $\phi = \frac{(2q+1) \times 180^\circ}{Z-P}$ $q = 0, 1, 2, \dots, P-Z-1$

⑥ Centroid + The asymptotes meet the Real axis at Centroid.

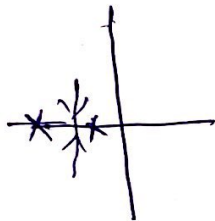
Centroid = $\frac{\text{Sum of Real part of Poles} - \text{Sum of Real parts of Zero's}}{\text{No of Poles} - \text{No of Zero's}}$

E.g



⑦ Break away & Break in Point is calculated by solving $\frac{dk}{ds} = 0$

E.g



Breaking Point

(Going into poles)



Breaking away

(Going away)

Whenever you have two poles you have break away but
 whenever you have two zeros you have breaking point.

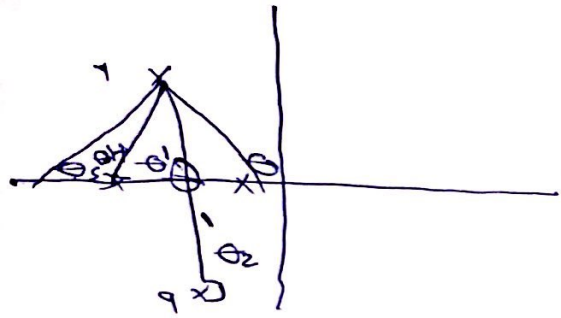
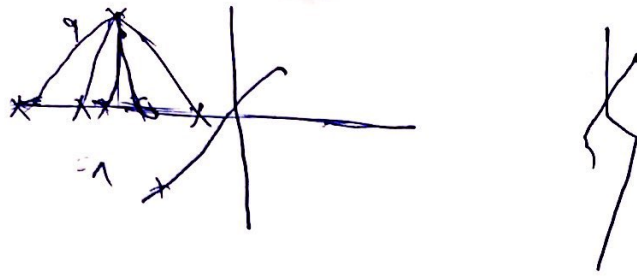
⑧ The angle of departure from an open loop fs Poles poles is given by $\phi_p = \pm 180^\circ (2q+1) + \phi$ $q=0,1,2, \dots$

This means when you have imaginary poles,
 where $\phi = \phi_2 - (\phi_1 + \phi_3 + \phi_4)$

⑨ The angle of arrival from an open zero's given by $\phi_z = \pm 180^\circ (2q+1) - \phi$; $q=0,1,2,3$

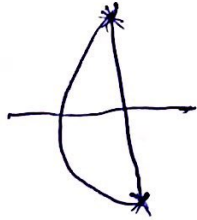
Whenever you have imaginary zero's

The e.o. $\phi = \theta = -(\theta_1 + \theta_3 + \theta_4)$ is given from.



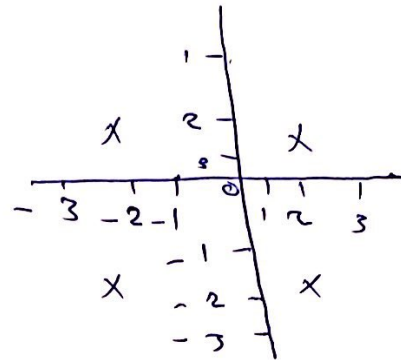
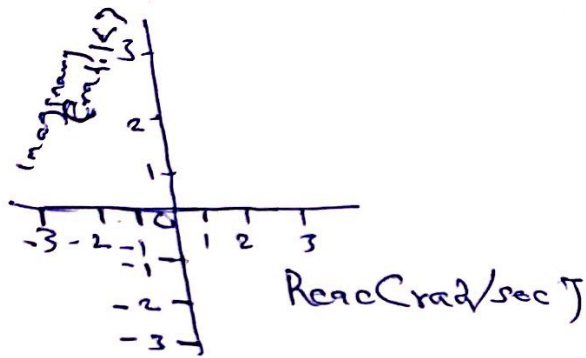
→ This is how to get $\text{ph.}[\phi]$

(c) The intersection of root locus branches \rightarrow the imaginary axis can be determined us of root criteria,



The intersection of the root locus on the ~~real~~ real axis is called breakaway but the intersection point of the root locus on imaginary axis is called the intersection point.

② A whole row of zero's indicate the presence of pairs of poles that are mirrored about imaginary axis



- At best, the system is marginally stable
- Use a Routh table to determine if it's unstable.
- If an entire row of zero's appears in a Routh table,
 - i) Create an auxiliary polynomial's form ~~of that~~ the row above the row of zero's other of s .
 - ii) Differentiate the auxiliary polynomial w.r.t s
 - iii) Replace the zero row ~~with~~ with the coefficients of the resulting polynomial
 - iv) Complete the Routh table as usual.
 - v) Evaluate the sign of the first column entries

⑥ To determine the poles on the $j\omega$ axis
 Determine the system poles for the Vanier's damper system the poles are

$$= \text{○} \begin{matrix} + \\ + j\omega \end{matrix}$$