

NAME: USORO ANDIDIONG INEMESTI
DEPT: MECHATRONICS ENGINEERING
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FEE # 1

① Root locus is a graphical presentation of the closed loop poles as a system parameter is varied. The root locus also gives a graphical representation of a system stability. Before presenting root locus.

The root locus technique can be used to analyse and design the effect of a loop gain upon system transient response and stability. The closed loop transfer function for system with a gain K is

$$T(s) = \frac{KG(s)}{1 + KG(s)H(s)}$$

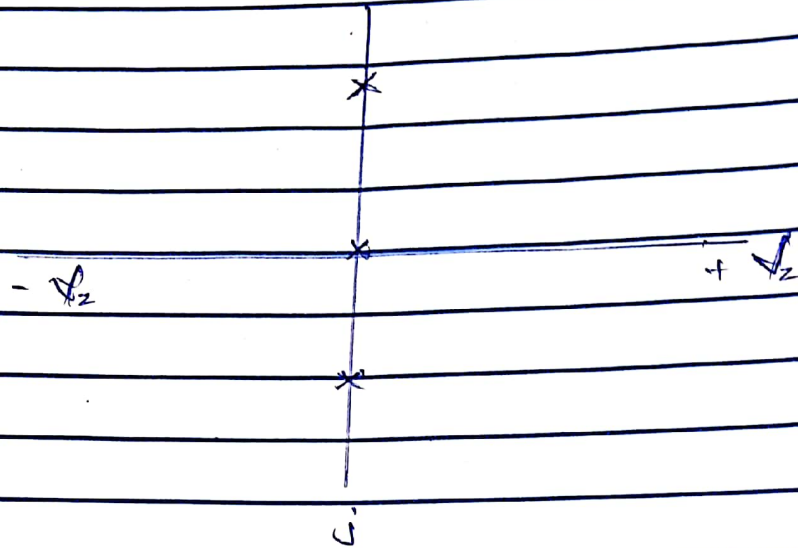
From this equation a pole exist when the characteristic polynomial in the denominator becomes zero or

$$KG(s)H(s) = -1 = K(2k+1)180^\circ$$

$$\text{where } K = 0, \pm 1, \pm 2, \pm 3, \pm 4, \dots$$

When -1 represented in Polar form as $K(2k+1)180^\circ$ alternatively a value of s is a closed loop pole of $|KG(s)H(s)|$ and $\angle KG(s)H(s) = (2k+1)180^\circ$

② The use of Routh's theorem to find stability of a closed loop system when entire row is zero on the Routh's array table to determine poles of the s axis.



This is the indication of roots on the imaginary axis.

This means or makes the system limitedly stable or marginally stable.

with the use of an example:
Consider the characteristic equation below

$$s^6 + 2s^5 + 8s^4 + 12s^3 + 20s^2 + 16s + 16 = 0$$

s^6	1	8	20	16
s^5	$\frac{2}{2} = 1$	$\frac{12}{2} = 6$	$\frac{16}{2} = 8$	
s^4	$\frac{2}{2} = 1$	$\frac{12}{2} = 6$	$\frac{16}{2} = 8$	
s^3	0	0	0	

Therefore
Application of Auxiliary Equation

$$S^4 = \text{even 1}$$

$$\text{Therefore} = S^4 + 6S^2 + 8S = 0$$

To get S^3

$$\frac{dA}{ds} = \frac{d}{ds} [S^4 + 6S^2 + 8S]$$

$$S^3 = 4S^3 + 12S + 8$$

$$S^3 = 4S^3 + 12S$$



S^6	1	8	20	16
S^5	1	6	8	
S^4	1	6	8	
S^3	$\frac{4}{1}=1$	$\frac{12}{4}=3$		
S^2	3	8		
S^1	0.33	0		
S^0	8			

No sign changes which means no positive poles

Due to the entire row of zeros means there are roots lying on the $j\omega$ axis

This means that the system is marginally stable or has limited stability.